

thm_2EASCIInumbers_2ESTRCAT__toString__inj
 (TMcfreizHE1Hk8edH4uoU3ZpmAMJcJCFYDus)

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Let $ty_2Estring_2Echar : \iota$ be given. Assume the following.

$$nonempty\ ty_2Estring_2Echar \quad (1)$$

Let $c_2Ebool_2EARB : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A.27a.nonempty\ A.27a \Rightarrow c_2Ebool_2EARB\ A.27a \in A.27a \quad (2)$$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (3)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \quad (4)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (5)$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o\ (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Earithmic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (6)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (7)$$

Definition 4 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 5 We define $c_Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_Emin_2E_3D (2^{A_27a})))$

Definition 6 We define c_Eenum_2ESUC to be $\lambda V0m \in ty_2Eenum_2Eenum.(ap c_Eenum_2EABS_num ($

Let $c_Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_Earithmetic_2E_2B \in ((ty_2Eenum_2Eenum^{ty_2Eenum_2Eenum})ty_2Eenum_2Eenum) \quad (8)$$

Definition 7 We define $c_Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Eenum_2Eenum.(ap (ap c_Earithmetic_2E_2B$

Definition 8 We define $c_Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Eenum_2Eenum.(ap (ap c_Earithmetic_2E_2B$

Definition 9 We define $c_Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Eenum_2Eenum.V0x$.

Let $c_Estring_2ECHR : \iota$ be given. Assume the following.

$$c_Estring_2ECHR \in (ty_2Estring_2Echar^{ty_2Eenum_2Eenum}) \quad (9)$$

Definition 10 We define $c_Ecombin_2EK$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0x \in A_27a.(\lambda V1y \in A_27b.V0x)$

Definition 11 We define $c_Ecombin_2ES$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.(\lambda V0f \in ((A_27c^{A_27b})^{A_27a})$

Definition 12 We define $c_Ecombin_2EI$ to be $\lambda A_27a : \iota.(ap (ap (c_Ecombin_2ES A_27a (A_27a^{A_27a}) A$

Definition 13 We define c_Ebool_2EF to be $(ap (c_Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 14 We define $c_Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 15 We define $c_Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_Ebool_2E_21 2) (\lambda V2t \in 2.V0t2$

Definition 16 We define $c_Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x)) \text{ then } (the (\lambda x.x \in A \wedge P x))$ of type $\iota \Rightarrow \iota$.

Definition 17 We define c_Ebool_2ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.V0t2$

Definition 18 We define $c_Ebool_2Eliteral_case$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0f \in (A_27b^{A_27a}).(\lambda V1x \in A_27a.V0f x$

Definition 19 We define $c_Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_Emin_2E_3D_3D_3E V0t) c_Ebool_2E_21$

Definition 20 We define $c_Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_Emin_2E_40$

Definition 21 We define $c_Erelation_2EWF$ to be $\lambda A_27a : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).(ap (c_Ebool_2E_21$

Definition 22 We define $c_Erelation_2ERESTRICT$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b^{A_27a}).\lambda V1M \in A_27a.V0f M$

Definition 23 We define $c_Erelation_2ETC$ to be $\lambda A_27a : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1a \in A_27a.\lambda V2b \in A_27a.V0R a b$

Definition 24 We define $c_Erelation_2Eapprox$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1M \in A_27a.V0R M$

Definition 25 We define $c_2Erelation_2Ethe_fun$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M$

Definition 26 We define $c_2Erelation_2EWFREC$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M$

Definition 27 We define $c_2EASCIInumbers_2EHEX$ to be $(ap (ap (c_2Erelation_2EWFREC ty_2Enum_2E$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty A0 \Rightarrow nonempty (ty_2Elist_2Elist A0) \quad (10)$$

Let $c_2Enumposrep_2En2l : \iota$ be given. Assume the following.

$$c_2Enumposrep_2En2l \in (((ty_2Elist_2Elist ty_2Enum_2Eenum)^{ty_2Enum_2Eenum})^{ty_2Enum_2Eenum}) \quad (11)$$

Let $c_2Elist_2EMAP : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a. nonempty A_27a \Rightarrow \forall A_27b. nonempty A_27b \Rightarrow c_2Elist_2EMAP \\ & A_27a A_27b \in (((ty_2Elist_2Elist A_27b)^{(ty_2Elist_2Elist A_27a)})^{(A_27b)^{A_27a}}) \end{aligned} \quad (12)$$

Let $c_2Elist_2EREVERSE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_2Elist_2EREVERSE A_27a \in ((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)}) \quad (13)$$

Definition 28 We define $c_2EASCIInumbers_2En2s$ to be $\lambda V0b \in ty_2Enum_2Eenum. \lambda V1f \in (ty_2Estring$

Definition 29 We define $c_2EASCIInumbers_2Enum_to_dec_string$ to be $(ap (ap c_2EASCIInumbers_2En2s$

Let $c_2Elist_2EAPPEND : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_2Elist_2EAPPEND A_27a \in (((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)})^{(ty_2Elist_2Elist A_27a)}) \quad (14)$$

Assume the following.

$$\begin{aligned} & (\forall V0n \in ty_2Enum_2Eenum. (\forall V1m \in ty_2Enum_2Eenum. (\\ & ((ap c_2EASCIInumbers_2Enum_to_dec_string V0n) = (ap c_2EASCIInumbers_2Enum_to_dec_string \\ & V1m)) \Leftrightarrow (V0n = V1m)))) \end{aligned} \quad (15)$$

Assume the following.

$$True \quad (16)$$

Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (17)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow ((\forall V0l1 \in (ty_2Elist_2Elist \\
& \quad A_27a).(\forall V1l2 \in (ty_2Elist_2Elist\ A_27a).(\forall V2l3 \in \\
& \quad (ty_2Elist_2Elist\ A_27a).(((ap\ (ap\ (c_2Elist_2EAPPEND\ A_27a) \\
& \quad V0l1)\ V1l2) = (ap\ (ap\ (c_2Elist_2EAPPEND\ A_27a)\ V0l1)\ V2l3)) \Leftrightarrow (V1l2 = \\
& \quad V2l3)))))) \wedge (\forall V3l1 \in (ty_2Elist_2Elist\ A_27a).(\forall V4l2 \in \\
& \quad (ty_2Elist_2Elist\ A_27a).(\forall V5l3 \in (ty_2Elist_2Elist\ A_27a). \\
& \quad (((ap\ (ap\ (c_2Elist_2EAPPEND\ A_27a)\ V4l2)\ V3l1) = (ap\ (ap\ (c_2Elist_2EAPPEND \\
& \quad A_27a)\ V5l3)\ V3l1)) \Leftrightarrow (V4l2 = V5l3))))))
\end{aligned} \tag{18}$$

Theorem 1

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum.(\forall V1m \in ty_2Enum_2Enum.(\\
& \quad \forall V2s \in (ty_2Elist_2Elist\ ty_2Estring_2Echar).(((ap\ (ap \\
& \quad (c_2Elist_2EAPPEND\ ty_2Estring_2Echar)\ V2s)\ (ap\ c_2EASCIInumbers_2Enum_to_dec_string \\
& \quad V0n)) = (ap\ (ap\ (c_2Elist_2EAPPEND\ ty_2Estring_2Echar)\ V2s)\ (ap \\
& \quad c_2EASCIInumbers_2Enum_to_dec_string\ V1m))) \Leftrightarrow (V0n = V1m))))))
\end{aligned}$$