

thm_2EASCIInumbers_2EtoString__inj
(TMZtvvH7GGBi19szub5KepMmo3Fg4y23sfX)

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Let $ty_2Estring_2Echar : \iota$ be given. Assume the following.

$$nonempty\ ty_2Estring_2Echar \tag{1}$$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. nonempty\ A \Rightarrow nonempty\ (ty_2Elist_2Elist\ A) \tag{2}$$

Let $c_2Ebool_2EARB : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. nonempty\ A \Rightarrow c_2Ebool_2EARB\ A \tag{3}$$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{4}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{5}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \tag{6}$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o\ (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \tag{7}$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \tag{8}$$

Definition 4 We define `c_2Ebool_2ET` to be $(\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 5 We define `c_2Ebool_2E_21` to be $\lambda A.27a : \iota.(\lambda V0P \in (2^{A-27a}).(\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^{A-27a}))))$

Definition 6 We define `c_2Enum_2ESUC` to be $\lambda V0m \in \text{ty_2Enum_2Enum}.(\text{ap } \text{c_2Enum_2EABS_num } (2^{A-27a}))$

Let `c_2Earithmetic_2E_2B` : ι be given. Assume the following.

$$\text{c_2Earithmetic_2E_2B} \in ((\text{ty_2Enum_2Enum}^{\text{ty_2Enum_2Enum}})^{\text{ty_2Enum_2Enum}}) \quad (9)$$

Definition 7 We define `c_2Earithmetic_2EBIT1` to be $\lambda V0n \in \text{ty_2Enum_2Enum}.(\text{ap } (\text{ap } \text{c_2Earithmetic_2E_2B } (V0n)))$

Definition 8 We define `c_2Earithmetic_2EBIT2` to be $\lambda V0n \in \text{ty_2Enum_2Enum}.(\text{ap } (\text{ap } \text{c_2Earithmetic_2E_2B } (V0n)))$

Definition 9 We define `c_2Earithmetic_2ENUMERAL` to be $\lambda V0x \in \text{ty_2Enum_2Enum}.V0x$.

Let `c_2Estring_2ECHR` : ι be given. Assume the following.

$$\text{c_2Estring_2ECHR} \in (\text{ty_2Estring_2Echar}^{\text{ty_2Enum_2Enum}}) \quad (10)$$

Definition 10 We define `c_2Ecombin_2EK` to be $\lambda A.27a : \iota.\lambda A.27b : \iota.(\lambda V0x \in A.27a.(\lambda V1y \in A.27b.V0x))$

Definition 11 We define `c_2Ecombin_2ES` to be $\lambda A.27a : \iota.\lambda A.27b : \iota.\lambda A.27c : \iota.(\lambda V0f \in ((A.27c^{A-27b})^{A-27a}))$

Definition 12 We define `c_2Ecombin_2EI` to be $\lambda A.27a : \iota.(\text{ap } (\text{ap } (\text{c_2Ecombin_2ES } A.27a (A.27a^{A-27a}))))$

Definition 13 We define `c_2Ebool_2EF` to be $(\text{ap } (\text{c_2Ebool_2E_21 } 2)) (\lambda V0t \in 2.V0t)$.

Definition 14 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2.\lambda Q \in 2.\text{inj_o } (p \Rightarrow q)$ of type ι .

Definition 15 We define `c_2Ebool_2E_2F_5C` to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(\text{ap } (\text{c_2Ebool_2E_21 } 2)) (\lambda V2t \in 2.V2t)))$

Definition 16 We define `c_2Emin_2E_40` to be $\lambda A.\lambda P \in 2^A.\text{if } (\exists x \in A.p (\text{ap } P x)) \text{ then } (\text{the } (\lambda x.x \in A \wedge P x))$ of type $\iota \Rightarrow \iota$.

Definition 17 We define `c_2Ebool_2ECOND` to be $\lambda A.27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A.27a.(\lambda V2t2 \in A.27a.(\text{ap } (\text{c_2Ebool_2E_21 } 2)) (\lambda V3t3 \in 2.V3t3))))$

Definition 18 We define `c_2Ebool_2Eliteral_case` to be $\lambda A.27a : \iota.\lambda A.27b : \iota.(\lambda V0f \in (A.27b^{A-27a}).(\lambda V1x \in A.27a.(\text{ap } f x)))$

Definition 19 We define `c_2Ebool_2E_7E` to be $(\lambda V0t \in 2.(\text{ap } (\text{ap } \text{c_2Emin_2E_3D_3D_3E } V0t) \text{ c_2Ebool_2E_21 } 2))$

Definition 20 We define `c_2Ebool_2E_3F` to be $\lambda A.27a : \iota.(\lambda V0P \in (2^{A-27a}).(\text{ap } V0P (\text{ap } (\text{c_2Emin_2E_40 } (2^{A-27a}))))$

Definition 21 We define `c_2Erelation_2EWF` to be $\lambda A.27a : \iota.\lambda V0R \in ((2^{A-27a})^{A-27a}).(\text{ap } (\text{c_2Ebool_2E_21 } 2) (V0R))$

Definition 22 We define `c_2Erelation_2ERESTRICT` to be $\lambda A.27a : \iota.\lambda A.27b : \iota.\lambda V0f \in (A.27b^{A-27a}).\lambda V1x \in A.27a.(\text{ap } f x)$

Definition 23 We define `c_2Erelation_2ETC` to be $\lambda A.27a : \iota.\lambda V0R \in ((2^{A-27a})^{A-27a}).\lambda V1a \in A.27a.\lambda V2b \in A.27a.(\text{ap } R a b)$

Definition 24 We define $c_2Erelation_2Eapprox$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M$

Definition 25 We define $c_2Erelation_2Ethe_fun$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M$

Definition 26 We define $c_2Erelation_2EWFREC$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M$

Definition 27 We define $c_2EASCIInumbers_2EHEX$ to be $(ap (ap (c_2Erelation_2EWFREC ty_2Eenum_2E$

Let $c_2Enumposrep_2En2l : \iota$ be given. Assume the following.

$$c_2Enumposrep_2En2l \in (((ty_2Elist_2Elist ty_2Eenum_2Eenum)^{ty_2Eenum_2Eenum})^{ty_2Eenum_2Eenum}) \quad (11)$$

Let $c_2Elist_2EMAP : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Elist_2EMAP \\ & A_27a\ A_27b \in (((ty_2Elist_2Elist\ A_27b)^{(ty_2Elist_2Elist\ A_27a)})^{(A_27b^{A_27a})}) \end{aligned} \quad (12)$$

Let $c_2Elist_2EREVERSE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2EREVERSE\ A_27a \in ((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)}) \quad (13)$$

Definition 28 We define $c_2EASCIInumbers_2En2s$ to be $\lambda V0b \in ty_2Eenum_2Eenum. \lambda V1f \in (ty_2Estring$

Definition 29 We define $c_2EASCIInumbers_2Eenum_to_dec_string$ to be $(ap (ap\ c_2EASCIInumbers_2En2s$

Definition 30 We define $c_2EASCIInumbers_2EUNHEX$ to be $(ap (ap (c_2Erelation_2EWFREC ty_2Estring$

Let $c_2Enumposrep_2El2n : \iota$ be given. Assume the following.

$$c_2Enumposrep_2El2n \in ((ty_2Eenum_2Eenum^{(ty_2Elist_2Elist\ ty_2Eenum_2Eenum)})^{ty_2Eenum_2Eenum}) \quad (14)$$

Definition 31 We define $c_2EASCIInumbers_2Es2n$ to be $\lambda V0b \in ty_2Eenum_2Eenum. \lambda V1f \in (ty_2Eenum_2E$

Definition 32 We define $c_2EASCIInumbers_2Eenum_from_dec_string$ to be $(ap (ap\ c_2EASCIInumbers_2Es$

Definition 33 We define $c_2Ebool_2E5C_2F$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_2Ebool_2E21\ 2) (\lambda V2t \in$

Assume the following.

$$\begin{aligned} & (\forall V0n \in ty_2Eenum_2Eenum. ((ap\ c_2EASCIInumbers_2Eenum_from_dec_string \\ & (ap\ c_2EASCIInumbers_2Eenum_to_dec_string\ V0n)) = V0n)) \end{aligned} \quad (15)$$

Assume the following.

$$True \quad (16)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (17)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge ((p V0t) \Rightarrow False) \Leftrightarrow \neg(p V0t)))))) \quad (18)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t)) \wedge ((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (19)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(V0x = V0x)) \quad (20)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow \neg(p V0t)) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow \neg(p V0t)))))) \quad (21)$$

Assume the following.

$$(\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \quad (22)$$

Assume the following.

$$(\forall V0A \in 2.((p V0A) \Rightarrow ((\neg(p V0A)) \Rightarrow False))) \quad (23)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p V0A) \vee (p V1B))) \Rightarrow False) \Leftrightarrow (((p V0A) \Rightarrow False) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))))) \quad (24)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg(\neg(p V0A) \vee (p V1B))) \Rightarrow False) \Leftrightarrow ((p V0A) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))))) \quad (25)$$

Assume the following.

$$(\forall V0A \in 2.(((\neg(p V0A)) \Rightarrow False) \Rightarrow (((p V0A) \Rightarrow False) \Rightarrow False))) \quad (26)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow ((p V1q) \Leftrightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee ((p V1q) \vee (p V2r))) \wedge (((p V0p) \vee (\neg(p V2r)) \vee \neg(p V1q))) \wedge (((p V1q) \vee (\neg(p V2r)) \vee \neg(p V0p))) \wedge ((p V2r) \vee ((\neg(p V1q)) \vee \neg(p V0p)))))))))) \quad (27)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \Rightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee \neg(p V2r))) \wedge (\neg(p V1q) \vee ((p V2r) \vee \neg(p V0p)))))))))) \quad (28)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (p V0p))) \quad (29)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow \neg(p V1q))) \quad (30)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \vee (p V1q))) \Rightarrow \neg(p V0p))) \quad (31)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \vee (p V1q))) \Rightarrow \neg(p V1q))) \quad (32)$$

Assume the following.

$$(\forall V0p \in 2. (\neg(\neg(p V0p))) \Rightarrow (p V0p)) \quad (33)$$

Theorem 1

$$(\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. ((ap\ c_2EASCIInumbers_2Enum_to_dec_string\ V0n) = (ap\ c_2EASCIInumbers_2Enum_to_dec_string\ V1m)) \Leftrightarrow (V0n = V1m))))$$