

thm_2EOmega_Automata_2BUECHI_TRANSLATION (TMdiKAdxkH4SCAkBzjtuXKV2QYtbG1MKZwx)

October 26, 2020

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A. \lambda a : \iota. (\lambda V0P \in (2^{A_27a}). (ap (ap (c_2Emin_2E_3D (2^{A_27a})) (\lambda V1P \in 2.V1P)) (\lambda V2P \in 2.V2P)))$

Definition 4 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2. \lambda Q \in 2. inj_o (p \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2. (ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2EF))$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \quad (1)$$

Definition 7 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2. (ap (c_2Ebool_2E_7E V2t) c_2Ebool_2EF))))))$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (2)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (3)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (4)$$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap c_2Enum_2EABS_num m)$

Definition 9 We define $c_2Emin_2E_40$ to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p (ap P x)) \text{ then } (\lambda x. x \in A \wedge p \text{ of type } \iota \Rightarrow \iota)$.

Definition 10 We define $c_2Ebool_2E_3F$ to be $\lambda A. \lambda a : \iota. (\lambda V0P \in (2^{A-27a}). (ap V0P (ap (c_2Emin_2E_40$

Definition 11 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum. \lambda V2t \in$

Definition 12 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_2Ebool_2E_21 2) (\lambda V2t \in$

Definition 13 We define $c_2Earithmetic_2E_3C_3D$ to be $\lambda V0m \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum. \lambda V2t \in$

Definition 14 We define $c_2EPast_Temporal_Logic_2EPBEFORE$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1b \in$

Definition 15 We define $c_2EPast_Temporal_Logic_2EPWHEN$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1b \in$

Definition 16 We define $c_2EPast_Temporal_Logic_2EPUNTIL$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1b \in$

Definition 17 We define $c_2EPast_Temporal_Logic_2EPSBEFORE$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1b \in$

Definition 18 We define $c_2EPast_Temporal_Logic_2EPSWHEN$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1b \in$

Definition 19 We define $c_2EPast_Temporal_Logic_2EPSUNTIL$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1b \in$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (5)$$

Definition 20 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP).$

Definition 21 We define c_2Ebool_2ECOND to be $\lambda A. \lambda a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A. 27a. (\lambda V2t2 \in A. 27a. ($

Definition 22 We define $c_2Eprim_rec_2EPRE$ to be $\lambda V0m \in ty_2Enum_2Enum. (ap (ap (ap (c_2Ebool_2E$

Definition 23 We define $c_2EPast_Temporal_Logic_2EPSNEXT$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1t0 \in$

Definition 24 We define $c_2EPast_Temporal_Logic_2EPEVENTUAL$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1t0 \in$

Definition 25 We define $c_2EPast_Temporal_Logic_2EPNEXT$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1t0 \in$

Definition 26 We define $c_2EPast_Temporal_Logic_2EPALWAYS$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}). \lambda V1t0 \in$

Definition 27 We define $c_2ETemporal_Logic_2ENEXT$ to be $\lambda V0P \in (2^{ty_2Enum_2Enum}). (\lambda V1t \in ty_2Enum_2Enum. \lambda V2t \in$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (6)$$

Definition 28 We define $c_2ETemporal_Logic_2EALWAYS$ to be $\lambda V0P \in (2^{ty_2Enum_2Enum}). \lambda V1t0 \in ty_2Enum_2Enum. \lambda V2t \in$

Definition 29 We define $c_2ETemporal_Logic_2EWATCH$ to be $\lambda V0q \in (2^{ty_2Enum_2Enum}). \lambda V1b \in (2^{ty_2Enum_2Enum}). \lambda V2t \in$

Definition 30 We define $c_2ETemporal_Logic_2ESBEFORE$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}).\lambda V1b \in (2^{ty_2Enum_2Enum})$

Definition 31 We define $c_2ETemporal_Logic_2EBEFORE$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}).\lambda V1b \in (2^{ty_2Enum_2Enum})$

Definition 32 We define $c_2ETemporal_Logic_2ESUNTIL$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}).\lambda V1b \in (2^{ty_2Enum_2Enum})$

Definition 33 We define $c_2ETemporal_Logic_2EUNTIL$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}).\lambda V1b \in (2^{ty_2Enum_2Enum})$

Definition 34 We define $c_2ETemporal_Logic_2EEVENTUAL$ to be $\lambda V0P \in (2^{ty_2Enum_2Enum}).\lambda V1t0 \in ty$

Definition 35 We define $c_2ETemporal_Logic_2ESWHEN$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}).\lambda V1b \in (2^{ty_2Enum_2Enum})$

Definition 36 We define $c_2ETemporal_Logic_2EWHEN$ to be $\lambda V0a \in (2^{ty_2Enum_2Enum}).\lambda V1b \in (2^{ty_2Enum_2Enum})$

Let $c_2Earithmetic_2EEVEN : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EEVEN \in (2^{ty_2Enum_2Enum}) \quad (7)$$

Let $c_2Earithmetic_2EODD : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EODD \in (2^{ty_2Enum_2Enum}) \quad (8)$$

Definition 37 We define $c_2Earithmetic_2E_3E$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 38 We define $c_2Earithmetic_2E_3E_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Let $c_2Earithmetic_2EXP : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (9)$$

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (10)$$

Let $c_2Earithmetic_2E_2A : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2A \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (11)$$

Definition 39 We define $c_2Enumeral_2EZ$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 40 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 41 We define $c_2Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2$

Definition 42 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2$

Definition 43 We define $c_2Earithmetic_2ZERO$ to be c_2Enum_2E0 .

Assume the following.

$$\begin{aligned}
& (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}). \\
& (((p (ap (ap c_2EPast_Temporal_Logic_2EPNEXT V0a) c_2Enum_2E0)) \Leftrightarrow \\
& True) \wedge (((p (ap (ap c_2EPast_Temporal_Logic_2EPSNEXT V0a) c_2Enum_2E0)) \Leftrightarrow \\
& False) \wedge (((p (ap (ap c_2EPast_Temporal_Logic_2EPALWAYS V0a) \\
& c_2Enum_2E0)) \Leftrightarrow (p (ap V0a c_2Enum_2E0))) \wedge (((p (ap (ap c_2EPast_Temporal_Logic_2EPEVENTUAL \\
& V0a) c_2Enum_2E0)) \Leftrightarrow (p (ap V0a c_2Enum_2E0))) \wedge (((p (ap (ap c_2EPast_Temporal_Logic_2EPSUNTIL \\
& V0a) V1b) c_2Enum_2E0)) \Leftrightarrow (p (ap V1b c_2Enum_2E0))) \wedge (((p (ap (ap \\
& (ap c_2EPast_Temporal_Logic_2EPSWHEN V0a) V1b) c_2Enum_2E0)) \Leftrightarrow \\
& ((p (ap V0a c_2Enum_2E0)) \wedge (p (ap V1b c_2Enum_2E0))) \wedge (((p (ap (\\
& ap (ap c_2EPast_Temporal_Logic_2EPSBEFORE V0a) V1b) c_2Enum_2E0)) \Leftrightarrow \\
& ((p (ap V0a c_2Enum_2E0)) \wedge (\neg(p (ap V1b c_2Enum_2E0)))) \wedge (((p (ap (\\
& ap (ap c_2EPast_Temporal_Logic_2EPUNTIL V0a) V1b) c_2Enum_2E0)) \Leftrightarrow \\
& ((p (ap V0a c_2Enum_2E0)) \vee (p (ap V1b c_2Enum_2E0))) \wedge (((p (ap (\\
& ap (ap c_2EPast_Temporal_Logic_2EPWHEN V0a) V1b) c_2Enum_2E0)) \Leftrightarrow \\
& ((p (ap V0a c_2Enum_2E0)) \vee (\neg(p (ap V1b c_2Enum_2E0)))) \wedge ((p (ap \\
& (ap (ap c_2EPast_Temporal_Logic_2EPBEFORE V0a) V1b) c_2Enum_2E0)) \Leftrightarrow \\
& (\neg(p (ap V1b c_2Enum_2E0)))))))))))))))))) \\
\end{aligned} \tag{12}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}). \\
& (((ap c_2ETemporal_Logic_2EALWAYS V0a) = (\lambda V2t \in ty_2Enum_2Enum. \\
& (ap (ap c_2Ebool_2E_2F_5C (ap V0a V2t)) (ap (ap c_2ETemporal_Logic_2ENEXT \\
& (ap c_2ETemporal_Logic_2EALWAYS V0a)) V2t)))) \wedge (((ap c_2ETemporal_Logic_2EEVENTUAL \\
& V0a) = (\lambda V3t \in ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_5C_2F (ap \\
& V0a V3t)) (ap (ap c_2ETemporal_Logic_2ENEXT (ap c_2ETemporal_Logic_2EEVENTUAL \\
& V0a)) V3t)))) \wedge (((ap (ap c_2ETemporal_Logic_2ESUNTIL V0a) V1b) = \\
& (\lambda V4t \in ty_2Enum_2Enum.(ap (ap c_2Emin_2E_3D_3D_3E (ap c_2Ebool_2E_7E \\
& (ap V1b V4t))) (ap (ap c_2Ebool_2E_2F_5C (ap V0a V4t)) (ap (ap c_2ETemporal_Logic_2ENEXT \\
& (ap (ap c_2ETemporal_Logic_2ESUNTIL V0a) V1b)) V4t)))) \wedge (((\\
& ap (ap c_2ETemporal_Logic_2ESWHEN V0a) V1b) = (\lambda V5t \in ty_2Enum_2Enum. \\
& (ap (ap (ap (c_2Ebool_2ECOND 2) (ap V1b V5t)) (ap V0a V5t)) (ap (ap \\
& c_2ETemporal_Logic_2ENEXT (ap (ap c_2ETemporal_Logic_2ESWHEN \\
& V0a) V1b)) V5t)))) \wedge (((ap (ap c_2ETemporal_Logic_2ESBEFORE V0a) \\
& V1b) = (\lambda V6t \in ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_2F_5C (ap \\
& c_2Ebool_2E_7E (ap V1b V6t))) (ap (ap c_2Ebool_2E_5C_2F (ap V0a \\
& V6t)) (ap (ap c_2ETemporal_Logic_2ENEXT (ap (ap c_2ETemporal_Logic_2ESBEFORE \\
& V0a) V1b)) V6t)))) \wedge (((ap (ap c_2ETemporal_Logic_2EUNTIL V0a) \\
& V1b) = (\lambda V7t \in ty_2Enum_2Enum.(ap (ap c_2Emin_2E_3D_3D_3E (\\
& ap c_2Ebool_2E_7E (ap V1b V7t))) (ap (ap c_2Ebool_2E_2F_5C (ap V0a \\
& V7t)) (ap (ap c_2ETemporal_Logic_2ENEXT (ap (ap c_2ETemporal_Logic_2EUNTIL \\
& V0a) V1b)) V7t)))) \wedge (((ap (ap c_2ETemporal_Logic_2EWHEN V0a) \\
& V1b) = (\lambda V8t \in ty_2Enum_2Enum.(ap (ap (ap (c_2Ebool_2ECOND 2) \\
& (ap V1b V8t)) (ap V0a V8t)) (ap (ap c_2ETemporal_Logic_2ENEXT (\\
& ap (ap c_2ETemporal_Logic_2EWHEN V0a) V1b)) V8t)))) \wedge (((ap (ap \\
& c_2ETemporal_Logic_2EBEFORE V0a) V1b) = (\lambda V9t \in ty_2Enum_2Enum. \\
& (ap (ap c_2Ebool_2E_2F_5C (ap c_2Ebool_2E_7E (ap V1b V9t))) (ap \\
& (ap c_2Ebool_2E_5C_2F (ap V0a V9t)) (ap (ap c_2ETemporal_Logic_2ENEXT \\
& (ap (ap c_2ETemporal_Logic_2EBEFORE V0a) V1b)) V9t)))) \wedge (((\\
& ap c_2EPast_Temporal_Logic_2EPALWAYS V0a) = (\lambda V10t \in ty_2Enum_2Enum. \\
& (ap (ap c_2Ebool_2E_2F_5C (ap V0a V10t)) (ap (ap c_2EPast_Temporal_Logic_2EPNEXT \\
& (ap c_2EPast_Temporal_Logic_2EPALWAYS V0a)) V10t)))) \wedge (((\\
& ap c_2EPast_Temporal_Logic_2EPEVENTUAL V0a) = (\lambda V11t \in ty_2Enum_2Enum. \\
& (ap (ap c_2Ebool_2E_5C_2F (ap V0a V11t)) (ap (ap c_2EPast_Temporal_Logic_2EPSNEXT \\
& (ap c_2EPast_Temporal_Logic_2EPEVENTUAL V0a)) V11t)))) \wedge \\
& (((ap (ap c_2EPast_Temporal_Logic_2EPSUNTIL V0a) V1b) = (\lambda V12t \in \\
& ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_5C_2F (ap V1b V12t)) (ap (ap \\
& c_2Ebool_2E_2F_5C (ap V0a V12t)) (ap (ap c_2EPast_Temporal_Logic_2EPSNEXT \\
& (ap (ap c_2EPast_Temporal_Logic_2EPSUNTIL V0a) V1b)) V12t)))) \wedge \\
& (((ap (ap c_2EPast_Temporal_Logic_2EPSWHEN V0a) V1b) = (\lambda V13t \in \\
& ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_5C_2F (ap (ap c_2Ebool_2E_2F_5C \\
& (ap V0a V13t)) (ap V1b V13t))) (ap (ap c_2Ebool_2E_2F_5C (ap c_2Ebool_2E_7E \\
& (ap V1b V13t))) (ap (ap c_2EPast_Temporal_Logic_2EPSNEXT (ap \\
& (ap c_2EPast_Temporal_Logic_2EPSWHEN V0a) V1b)) V13t)))) \wedge \\
& (((ap (ap c_2EPast_Temporal_Logic_2EPSBEFORE V0a) V1b) = (\lambda V14t \in \\
& ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_2F_5C (ap c_2Ebool_2E_7E \\
& (ap V1b V14t))) (ap (ap c_2Ebool_2E_5C_2F (ap V0a V14t)) (ap (ap \\
& c_2EPast_Temporal_Logic_2EPSBEFORE V0a) V1b)) V14t)))) \wedge \\
& (((ap (ap c_2EPast_Temporal_Logic_2EPUNTIL V0a) V1b) = (\lambda V15t \in \\
& ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_5C_2F (ap V1b V15t)) (ap (ap \\
& c_2Ebool_2E_2F_5C (ap V0a V15t)) (ap (ap c_2EPast_Temporal_Logic_2EPNEXT \\
& (ap (ap c_2EPast_Temporal_Logic_2EPUNTIL V0a) V1b)) V15t)))) \wedge \\
& (((ap (ap c_2EPast_Temporal_Logic_2EPWHEN V0a) V1b) = (\lambda V16t \in \\
& ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_5C_2F (ap (ap c_2Ebool_2E_2F_5C \\
& (ap V0a V16t)) (ap V1b V16t))) (ap (ap c_2Ebool_2E_2F_5C (ap c_2Ebool_2E_7E \\
& (ap V1b V16t))) (ap (ap c_2EPast_Temporal_Logic_2EPNEXT (ap \\
& (ap c_2EPast_Temporal_Logic_2EPWHEN V0a) V1b)) V16t)))) \wedge \\
& (((ap (ap c_2EPast_Temporal_Logic_2EPBEFORE V0a) V1b) = (\lambda V17t \in \\
& ty_2Enum_2Enum.(ap (ap c_2Ebool_2E_2F_5C (ap c_2Ebool_2E_7E \\
& (ap V1b V17t))) (ap (ap c_2EPast_Temporal_Logic_2EPNEXT (ap \\
& (ap c_2EPast_Temporal_Logic_2EPWHEN V0a) V1b)) V17t)))) \wedge
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0b \in (2^{ty_2Enum_2Enum}).(\forall V1t0 \in ty_2Enum_2Enum. \\
& ((\exists V2d \in ty_2Enum_2Enum.((\forall V3t \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Eprim_rec_2E_3C V3t) V2d)) \Rightarrow (\neg(p (ap V0b (ap (ap c_2Earithmetic_2E_2B \\
& V3t) V1t0))))))) \wedge (p (ap V0b (ap (ap c_2Earithmetic_2E_2B V2d) V1t0))))))) \vee \\
& (\forall V4d \in ty_2Enum_2Enum.(\neg(p (ap V0b (ap (ap c_2Earithmetic_2E_2B \\
& V4d) V1t0))))))) \\
\end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}. \\
& (\forall V2t0 \in ty_2Enum_2Enum.((p (ap (ap c_2ETemporal_Logic_2EWHEN \\
& V0a) V1b) V2t0)) \Leftrightarrow (\forall V3delta \in ty_2Enum_2Enum.((\forall V4t \in \\
& ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C V4t) V3delta)) \Rightarrow \\
& (\neg(p (ap V1b (ap (ap c_2Earithmetic_2E_2B V4t) V2t0))))))) \wedge (p (ap \\
& V1b (ap (ap c_2Earithmetic_2E_2B V3delta) V2t0))) \Rightarrow (p (ap V0a \\
& (ap (ap c_2Earithmetic_2E_2B V3delta) V2t0))))))) \\
\end{aligned} \tag{15}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}. \\
& (\forall V2t0 \in ty_2Enum_2Enum.((p (ap (ap c_2ETemporal_Logic_2ESWHEN \\
& V0a) V1b) V2t0)) \Leftrightarrow (\exists V3delta \in ty_2Enum_2Enum.((\forall V4t \in \\
& ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C V4t) V3delta)) \Rightarrow \\
& (\neg(p (ap V1b (ap (ap c_2Earithmetic_2E_2B V4t) V2t0))))))) \wedge ((p (\\
& ap V1b (ap (ap c_2Earithmetic_2E_2B V3delta) V2t0))) \wedge (p (ap V0a \\
& (ap (ap c_2Earithmetic_2E_2B V3delta) V2t0))))))) \\
\end{aligned} \tag{16}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}. \\
& ((ap (ap c_2ETemporal_Logic_2EUNTIL V0a) V1b) = (ap (ap c_2ETemporal_Logic_2EWHEN \\
& V1b) (\lambda V2t \in ty_2Enum_2Enum.(ap (ap c_2Emin_2E_3D_3D_3E (ap \\
& V0a V2t)) (ap V1b V2t))))))) \\
\end{aligned} \tag{17}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in (2^{ty_2Enum_2Enum}).((ap c_2ETemporal_Logic_2EALWAYS \\
& V0a) = (ap (ap c_2ETemporal_Logic_2EUNTIL V0a) (\lambda V1t \in ty_2Enum_2Enum. \\
& c_2Ebool_2EF)))) \\
\end{aligned} \tag{18}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}). \\
 & ((ap (ap c_2ETemporal_Logic_2ESBEFORE V0a) V1b) = (\lambda V2t0 \in \\
 & ty_2Enum_2Enum.(ap c_2Ebool_2E_7E (ap (ap (ap c_2ETemporal_Logic_2EUNTIL \\
 & (\lambda V3t \in ty_2Enum_2Enum.(ap c_2Ebool_2E_7E (ap V0a V3t)))) V1b) \\
 & V2t0))))))) \\
 \end{aligned} \tag{19}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}). \\
 & ((ap (ap c_2ETemporal_Logic_2ESUNTIL V0a) V1b) = (ap (ap c_2ETemporal_Logic_2ESWHEN \\
 & V1b) (\lambda V2t \in ty_2Enum_2Enum.(ap (ap c_2Emin_2E_3D_3D_3E (ap \\
 & V0a V2t)) (ap V1b V2t))))))) \\
 \end{aligned} \tag{20}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0a \in (2^{ty_2Enum_2Enum}).((ap c_2ETemporal_Logic_2EEVENTUAL \\
 & V0a) = (ap (ap c_2ETemporal_Logic_2ESUNTIL (\lambda V1t \in ty_2Enum_2Enum. \\
 & c_2Ebool_2ET)) V0a))) \\
 \end{aligned} \tag{21}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0a \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}). \\
 & ((ap (ap c_2ETemporal_Logic_2EBEFORE V0a) V1b) = (\lambda V2t \in ty_2Enum_2Enum. \\
 & (ap c_2Ebool_2E_7E (ap (ap c_2ETemporal_Logic_2ESUNTIL \\
 & (\lambda V3t \in ty_2Enum_2Enum.(ap c_2Ebool_2E_7E (ap V0a V3t)))) V1b) \\
 & V2t))))))) \\
 \end{aligned} \tag{22}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0b \in (2^{ty_2Enum_2Enum}).(\forall V1t0 \in ty_2Enum_2Enum. \\
 & (((p (ap (ap c_2ETemporal_Logic_2EEVENTUAL V0b) V1t0)) \Leftrightarrow (\forall V2a \in \\
 & (2^{ty_2Enum_2Enum}).((p (ap (ap (ap c_2ETemporal_Logic_2EWHEN \\
 & V2a) V0b) V1t0)) \Leftrightarrow (p (ap (ap (ap c_2ETemporal_Logic_2ESWHEN V2a) \\
 & V0b) V1t0))))))) \wedge (((p (ap (ap c_2ETemporal_Logic_2EEVENTUAL V0b) \\
 & V1t0)) \Leftrightarrow (\forall V3a \in (2^{ty_2Enum_2Enum}).((p (ap (ap (ap c_2ETemporal_Logic_2EUNTIL \\
 & V3a) V0b) V1t0)) \Leftrightarrow (p (ap (ap (ap c_2ETemporal_Logic_2ESUNTIL V3a) \\
 & V0b) V1t0))))))) \wedge (((p (ap (ap c_2ETemporal_Logic_2EEVENTUAL V0b) \\
 & V1t0)) \Leftrightarrow (\forall V4a \in (2^{ty_2Enum_2Enum}).((p (ap (ap (ap c_2ETemporal_Logic_2EBEFORE \\
 & V4a) V0b) V1t0)) \Leftrightarrow (p (ap (ap (ap c_2ETemporal_Logic_2ESBEFORE \\
 & V4a) V0b) V1t0))))))) \\
 \end{aligned} \tag{23}$$

Assume the following.

$$\begin{aligned}
& (\forall V0y \in (2^{ty_2Enum_2Enum}).(\forall V1b \in (2^{ty_2Enum_2Enum}). \\
& (\forall V2a \in (2^{ty_2Enum_2Enum}).((V0y = (\lambda V3t \in ty_2Enum_2Enum. \\
& (ap (ap (ap (c_2Ebool_2ECOND 2) (ap V1b V3t)) (ap V2a V3t)) (ap V0y \\
& (ap (ap c_2Earithmetic_2E_2B V3t) (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))))))) \Leftrightarrow ((\\
& V0y = (ap (ap c_2ETemporal_Logic_2EWHEN V2a) V1b)) \vee (V0y = (ap (\\
& ap c_2ETemporal_Logic_2ESWHEN V2a) V1b))))))) \\
\end{aligned} \tag{24}$$

Assume the following.

$$\begin{aligned}
& ((ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)) = \\
& (ap c_2Enum_2ESUC c_2Enum_2E0)) \\
\end{aligned} \tag{25}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\\
& ((ap (ap c_2Earithmetic_2E_2B c_2Enum_2E0) V0m) = V0m) \wedge (((ap (\\
& ap c_2Earithmetic_2E_2B V0m) c_2Enum_2E0) = V0m) \wedge (((ap (ap c_2Earithmetic_2E_2B \\
& (ap c_2Enum_2ESUC V0m)) V1n) = (ap c_2Enum_2ESUC (ap (ap c_2Earithmetic_2E_2B \\
& V0m) V1n))) \wedge ((ap (ap c_2Earithmetic_2E_2B V0m) (ap c_2Enum_2ESUC \\
& V1n)) = (ap c_2Enum_2ESUC (ap (ap c_2Earithmetic_2E_2B V0m) V1n))))))) \\
\end{aligned} \tag{26}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\\
& (ap (ap c_2Earithmetic_2E_2B V0m) V1n) = (ap (ap c_2Earithmetic_2E_2B \\
& V1n) V0m))) \\
\end{aligned} \tag{27}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\\
& \forall V2p \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B V0m) \\
& (ap (ap c_2Earithmetic_2E_2B V1n) V2p)) = (ap (ap c_2Earithmetic_2E_2B \\
& (ap (ap c_2Earithmetic_2E_2B V0m) V1n)) V2p)))))) \\
\end{aligned} \tag{28}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\\
& (p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n)) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& (ap c_2Enum_2ESUC V0m)) V1n)))))) \\
\end{aligned} \tag{29}$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.(p (ap (ap c_2Earithmetic_2E_3C_3D \\
c_2Enum_2E0) V0n))) \tag{30}$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\ & (\neg(p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\ & V1n) V0m)))))) \end{aligned} \quad (31)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. ((ap c_2Enum_2ESUC V0m) = (ap (ap \\ & c_2Earithmetic_2E_2B V0m) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\ & c_2Earithmetic_2EZERO)))))) \end{aligned} \quad (32)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\ & ((ap (ap c_2Earithmetic_2E_2A c_2Enum_2E0) V0m) = c_2Enum_2E0) \wedge \\ & (((ap (ap c_2Earithmetic_2E_2A V0m) c_2Enum_2E0) = c_2Enum_2E0) \wedge \\ & (((ap (ap c_2Earithmetic_2E_2A (ap c_2Earithmetic_2ENUMERAL \\ & (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))) V0m) = V0m) \wedge \\ & (((ap (ap c_2Earithmetic_2E_2A V0m) (ap c_2Earithmetic_2ENUMERAL \\ & (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))) = V0m) \wedge \\ & ((ap (ap c_2Earithmetic_2E_2A (ap c_2Enum_2ESUC V0m)) V1n) = (ap \\ & (ap c_2Earithmetic_2E_2B (ap (ap c_2Earithmetic_2E_2A V0m) V1n)) \\ & V1n)) \wedge ((ap (ap c_2Earithmetic_2E_2A V0m) (ap c_2Enum_2ESUC V1n)) = \\ & (ap (ap c_2Earithmetic_2E_2B V0m) (ap (ap c_2Earithmetic_2E_2A \\ & V0m) V1n)))))))))) \end{aligned} \quad (33)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\ & \forall V2p \in ty_2Enum_2Enum. (((p (ap (ap c_2Earithmetic_2E_3C_3D \\ & V0m) V1n)) \wedge (p (ap (ap c_2Earithmetic_2E_3C_3D V1n) V2p))) \Rightarrow (p (\\ & ap (ap c_2Earithmetic_2E_3C_3D V0m) V2p)))))) \end{aligned} \quad (34)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\ & (p (ap (ap c_2Eprim_rec_2E_3C V1n) V0m)) \Rightarrow (\exists V2p \in ty_2Enum_2Enum. \\ & (V0m = (ap (ap c_2Earithmetic_2E_2B V1n) (ap (ap c_2Earithmetic_2E_2B \\ & V2p) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\ & c_2Earithmetic_2EZERO)))))))))) \end{aligned} \quad (35)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\ & (V0m = V1n) \Leftrightarrow ((p (ap (ap c_2Earithmetic_2E_3C_3D V0m) V1n)) \wedge (p (\\ & ap (ap c_2Earithmetic_2E_3C_3D V1n) V0m)))))) \end{aligned} \quad (36)$$

Assume the following.

$$\begin{aligned}
 & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
 & \forall V2p \in ty_2Enum_2Enum. ((p (ap (ap c_2Earithmetic_2E_3C_3D \\
 & (ap (ap c_2Earithmetic_2E_2B V0m) V1n)) (ap (ap c_2Earithmetic_2E_2B \\
 & V0m) V2p))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D V1n) V2p)))))) \\
 \end{aligned} \tag{37}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
 & (\neg(V0m = V1n)) \Leftrightarrow ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Enum_2ESUC \\
 & V0m)) V1n)) \vee (p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Enum_2ESUC \\
 & V1n)) V0m)))))) \\
 \end{aligned} \tag{38}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0n \in ty_2Enum_2Enum. ((ap c_2Enum_2ESUC V0n) = (ap (ap \\
 & c_2Earithmetic_2E_2B (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
 & c_2Earithmetic_2EZERO)) V0n))) \\
 \end{aligned} \tag{39}$$

Assume the following.

$$True \tag{40}$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p \\
 V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2))))) \tag{41}$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \tag{42}$$

Assume the following.

$$(\forall V0t \in 2. ((p V0t) \vee (\neg(p V0t)))) \tag{43}$$

Assume the following.

$$\begin{aligned}
 & \forall A_27a. nonempty A_27a \Rightarrow \forall A_27b. nonempty A_27b \Rightarrow (\\
 & \forall V0t1 \in A_27a. (\forall V1t2 \in A_27b. ((ap (\lambda V2x \in A_27b. \\
 & V0t1) V1t2) = V0t1))) \\
 \end{aligned} \tag{44}$$

Assume the following.

$$\begin{aligned}
 & \forall A_27a. nonempty A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in \\
 & A_27a. (p V0t)) \Leftrightarrow (p V0t))) \\
 \end{aligned} \tag{45}$$

Assume the following.

$$\begin{aligned}
 & \forall A_27a. nonempty A_27a \Rightarrow (\forall V0t \in 2. ((\exists V1x \in \\
 & A_27a. (p V0t)) \Leftrightarrow (p V0t))) \\
 \end{aligned} \tag{46}$$

Assume the following.

$$(\forall V0t \in 2.(((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))))) \quad (47)$$

Assume the following.

$$(\forall V0t \in 2.(((True \vee (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \vee True) \Leftrightarrow True) \wedge (((False \vee (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee False) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee (p V0t)) \Leftrightarrow (p V0t)))))) \quad (48)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (49)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t)) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True)))) \quad (50)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (51)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (52)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (53)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p V0A) \wedge (p V1B))) \Leftrightarrow ((\neg(p V0A) \vee (\neg(p V1B)))) \wedge ((\neg((p V0A) \vee (p V1B))) \Leftrightarrow ((\neg(p V0A) \wedge (\neg(p V1B)))))))))) \quad (54)$$

Assume the following.

$$(\forall V0t \in 2.((p V0t) \Rightarrow False) \Leftrightarrow ((p V0t) \Leftrightarrow False)) \quad (55)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (56)$$

Assume the following.

$$\begin{aligned} & (\forall V0P \in (2^{ty_2Enum_2Enum}).(((p (ap V0P c_2Enum_2E0)) \wedge \\ & (\forall V1n \in ty_2Enum_2Enum.((p (ap V0P V1n)) \Rightarrow (p (ap V0P (ap c_2Enum_2ESUC \\ & V1n))))))) \Rightarrow (\forall V2n \in ty_2Enum_2Enum.(p (ap V0P V2n)))) \end{aligned} \quad (57)$$

Assume the following.

$$\begin{aligned}
& ((\forall V0n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B \\
& c_2Enum_2E0) V0n) = V0n)) \wedge ((\forall V1n \in ty_2Enum_2Enum.((ap \\
& (ap c_2Earithmetic_2E_2B V1n) c_2Enum_2E0) = V1n)) \wedge ((\forall V2n \in \\
ty_2Enum_2Enum.(\forall V3m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B \\
& (ap c_2Earithmetic_2ENUMERAL V2n)) (ap c_2Earithmetic_2ENUMERAL \\
V3m)) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Enum_2EiZ (ap \\
& (ap c_2Earithmetic_2E_2B V2n) V3m))))))) \wedge ((\forall V4n \in ty_2Enum_2Enum. \\
& ((ap (ap c_2Earithmetic_2E_2A c_2Enum_2E0) V4n) = c_2Enum_2E0)) \wedge \\
& ((\forall V5n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A \\
V5n) c_2Enum_2E0) = c_2Enum_2E0)) \wedge ((\forall V6n \in ty_2Enum_2Enum. \\
& ((\forall V7m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A \\
& ap c_2Earithmetic_2ENUMERAL V6n)) (ap c_2Earithmetic_2ENUMERAL \\
V7m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2E_2A \\
V6n) V7m)))))) \wedge ((\forall V8n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D \\
c_2Enum_2E0) V8n) = c_2Enum_2E0)) \wedge ((\forall V9n \in ty_2Enum_2Enum. \\
& ((ap (ap c_2Earithmetic_2E_2D V9n) c_2Enum_2E0) = V9n)) \wedge ((\forall V10n \in \\
ty_2Enum_2Enum.(\forall V11m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D \\
& (ap c_2Earithmetic_2ENUMERAL V10n)) (ap c_2Earithmetic_2ENUMERAL \\
V11m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2E_2D \\
V10n) V11m)))))) \wedge ((\forall V12n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEXP \\
c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
V12n))) = c_2Enum_2E0)) \wedge ((\forall V13n \in ty_2Enum_2Enum.((ap \\
& (ap c_2Earithmetic_2EEXP c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL \\
(ap c_2Earithmetic_2EBIT2 V13n))) = c_2Enum_2E0)) \wedge ((\forall V14n \in \\
ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEXP V14n) c_2Enum_2E0) = \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))))) \wedge \\
& ((\forall V15n \in ty_2Enum_2Enum.(\forall V16m \in ty_2Enum_2Enum. \\
& ((ap (ap c_2Earithmetic_2EEXP (ap c_2Earithmetic_2ENUMERAL V15n)) \\
(ap c_2Earithmetic_2ENUMERAL V16m)) = (ap c_2Earithmetic_2ENUMERAL \\
(ap (ap c_2Earithmetic_2EEXP V15n) V16m)))))) \wedge (((ap c_2Enum_2ESUC \\
c_2Enum_2E0) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
c_2Earithmetic_2EZERO)))) \wedge ((\forall V17n \in ty_2Enum_2Enum. \\
& (ap c_2Enum_2ESUC (ap c_2Earithmetic_2ENUMERAL V17n)) = (ap c_2Earithmetic_2ENUMERAL \\
(ap c_2Enum_2ESUC V17n)))) \wedge (((ap c_2Eprim_rec_2EPRE c_2Enum_2E0) = \\
c_2Enum_2E0) \wedge ((\forall V18n \in ty_2Enum_2Enum.((ap c_2Eprim_rec_2EPRE \\
(ap c_2Earithmetic_2ENUMERAL V18n)) = (ap c_2Earithmetic_2ENUMERAL \\
(ap c_2Eprim_rec_2EPRE V18n)))))) \wedge ((\forall V19n \in ty_2Enum_2Enum. \\
& (((ap c_2Earithmetic_2ENUMERAL V19n) = c_2Enum_2E0) \Leftrightarrow (V19n = c_2Earithmetic_2EZERO))) \wedge \\
& ((\forall V20n \in ty_2Enum_2Enum.((c_2Enum_2E0) = (ap c_2Earithmetic_2ENUMERAL \\
V20n)) \Leftrightarrow (V20n = c_2Earithmetic_2EZERO))) \wedge ((\forall V21n \in ty_2Enum_2Enum. \\
& ((\forall V22m \in ty_2Enum_2Enum.(((ap c_2Earithmetic_2ENUMERAL \\
V21n) = (ap c_2Earithmetic_2ENUMERAL V22m)) \Leftrightarrow (V21n = V22m)))) \wedge \\
& ((\forall V23n \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C \\
V23n) c_2Enum_2E0)) \Leftrightarrow False)) \wedge ((\forall V24n \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL \\
V24n))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) \\
V24n)))) \wedge ((\forall V25n \in ty_2Enum_2Enum.(\forall V26m \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Eprim_rec_2E_3C (ap c_2Earithmetic_2ENUMERAL \\
V25n)) (ap c_2Earithmetic_2ENUMERAL V26m))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C \\
V25n) V26m)))))) \wedge ((\forall V27n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3E \\
c_2Enum_2E0) V27n)) \Leftrightarrow False)) \wedge ((\forall V28n \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Earithmetic_2E_3E (ap c_2Earithmetic_2ENUMERAL \\
V28n)) c_2Enum_2E0)) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) \\
V28n)))) \wedge ((\forall V29n \in ty_2Enum_2Enum.(\forall V30m \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Earithmetic_2E_3E (ap c_2Earithmetic_2ENUMERAL \\
V29n)) (ap c_2Earithmetic_2ENUMERAL V30m))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C \\
V30m) V29n)))) \wedge ((\forall V31n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3C_3D \\
c_2Enum_2E0) V31n)) \Leftrightarrow True)) \wedge ((\forall V32n \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2ENUMERAL \\
V32n)))) \wedge ((\forall V33n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3C_3D \\
c_2Enum_2E0) V33n)) \Leftrightarrow False)) \wedge ((\forall V34n \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2ENUMERAL \\
V34n)) \Leftrightarrow False)))))))
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. \\
& ((p (ap (ap c_2Earithmetic_2E_3C_3D c_2Earithmetic_2EZERO) V0n)) \Leftrightarrow \\
& True) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT1 \\
& V0n)) c_2Earithmetic_2EZERO) \Leftrightarrow False) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& (ap c_2Earithmetic_2EBIT2 V0n)) c_2Earithmetic_2EZERO) \Leftrightarrow False) \wedge \\
& (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT1 \\
& V0n)) (ap c_2Earithmetic_2EBIT1 V1m))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V0n) V1m))) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT1 \\
& V0n)) (ap c_2Earithmetic_2EBIT2 V1m))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V0n) V1m))) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT2 \\
& V0n)) (ap c_2Earithmetic_2EBIT1 V1m))) \Leftrightarrow (\neg(p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V1m) V0n))) \wedge ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT2 \\
& V0n)) (ap c_2Earithmetic_2EBIT2 V1m))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V0n) V1m))))))))))) \\
\end{aligned} \tag{59}$$

Assume the following.

$$\begin{aligned}
& (((ap c_2Eprim_rec_2EPRE c_2Enum_2E0) = c_2Enum_2E0) \wedge (\forall V0m \in \\
& ty_2Enum_2Enum. ((ap c_2Eprim_rec_2EPRE (ap c_2Enum_2ESUC V0m)) = \\
& V0m)))
\end{aligned} \tag{60}$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum. (\neg(p (ap (ap c_2Eprim_rec_2E_3C \\
V0n) V0n)))) \tag{61}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) \\
& (ap c_2Enum_2ESUC V0n))))
\end{aligned} \tag{62}$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \tag{63}$$

Assume the following.

$$(\forall V0A \in 2. ((p V0A) \Rightarrow ((\neg(p V0A)) \Rightarrow False))) \tag{64}$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((p V0A) \vee (p V1B))) \Rightarrow False) \Leftrightarrow \\
& ((p V0A) \Rightarrow False) \Rightarrow ((\neg(p V1B)) \Rightarrow False))))
\end{aligned} \tag{65}$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((\neg(p V0A)) \vee (p V1B))) \Rightarrow False) \Leftrightarrow \\
& ((p V0A) \Rightarrow ((\neg(p V1B)) \Rightarrow False))))
\end{aligned} \tag{66}$$

Assume the following.

$$(\forall V0A \in 2.(((\neg(p V0A)) \Rightarrow False) \Rightarrow (((p V0A) \Rightarrow False) \Rightarrow False))) \quad (67)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow \\ & (p V1q) \Leftrightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee ((p V1q) \vee (p V2r))) \wedge (((p V0p) \vee ((\neg(p V2r)) \vee (\neg(p V1q)))) \wedge (((p V1q) \vee ((\neg(p V2r)) \vee (\neg(p V0p)))) \wedge ((p V2r) \vee \\ & ((\neg(p V1q)) \vee (\neg(p V0p))))))))))) \end{aligned} \quad (68)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow \\ & (p V1q) \wedge (p V2r))) \Leftrightarrow (((p V0p) \vee ((\neg(p V1q)) \vee (\neg(p V2r)))) \wedge (((p V1q) \vee \\ & ((\neg(p V0p)) \wedge ((p V2r) \vee (\neg(p V0p))))))))))) \end{aligned} \quad (69)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow \\ & (p V1q) \vee (p V2r))) \Leftrightarrow (((p V0p) \vee ((\neg(p V1q)) \wedge ((p V0p) \vee (\neg(p V2r)))) \wedge \\ & ((p V1q) \vee ((p V2r) \vee (\neg(p V0p))))))))))) \end{aligned} \quad (70)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow \\ & (p V1q) \Rightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge \\ & ((\neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p))))))))))) \end{aligned} \quad (71)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((p V0p) \Leftrightarrow (\neg(p V1q))) \Leftrightarrow (((p V0p) \vee \\ (p V1q)) \wedge ((\neg(p V1q)) \vee (\neg(p V0p))))))) \quad (72)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(\forall V3s \in \\ & 2.(((p V0p) \Leftrightarrow (p (ap (ap (ap (c_2Ebool_2ECOND 2) V1q) V2r) V3s))) \Leftrightarrow \\ & (((p V0p) \vee ((p V1q) \vee (\neg(p V3s)))) \wedge (((p V0p) \vee ((\neg(p V2r)) \vee (\neg(p V1q)))) \wedge \\ & (((p V0p) \vee ((\neg(p V2r)) \vee (\neg(p V3s)))) \wedge (((\neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p)))) \wedge \\ & ((p V1q) \vee ((p V3s) \vee (\neg(p V0p))))))))))))))) \end{aligned} \quad (73)$$

Theorem 1

$$\begin{aligned}
& (\forall V0Phi \in (2^{(2^{ty_2Enum_2Enum})}).(\forall V1phi \in (2^{ty_2Enum_2Enum}). \\
& \quad (\forall V2a \in (2^{ty_2Enum_2Enum}).(\forall V3b \in (2^{ty_2Enum_2Enum}. \\
& \quad (((p (ap V0Phi (ap c_2ETemporal_Logic_2ENEXT V1phi))) \Leftrightarrow (\exists V4q0 \in \\
& \quad \quad (2^{ty_2Enum_2Enum}).(\exists V5q1 \in (2^{ty_2Enum_2Enum}).(True \wedge \\
& \quad \quad ((\forall V6t \in ty_2Enum_2Enum.((p (ap V4q0 V6t)) \Leftrightarrow (p (ap V1phi \\
& \quad \quad V6t))) \wedge ((p (ap V5q1 V6t)) \Leftrightarrow (p (ap V4q0 (ap (ap c_2Earithmetic_2E_2B \\
& \quad \quad V6t) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad \quad c_2Earithmetic_2EZERO))))))) \wedge (p (ap V0Phi V5q1))))))) \wedge (((\\
& \quad p (ap V0Phi (ap c_2ETemporal_Logic_2EALWAYS V2a))) \Leftrightarrow (\exists V7q \in \\
& \quad \quad (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V8t \in ty_2Enum_2Enum.((\\
& \quad \quad p (ap V7q V8t)) \Leftrightarrow ((p (ap V2a V8t)) \wedge (p (ap V7q (ap (ap c_2Earithmetic_2E_2B \\
& \quad \quad V8t) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad \quad c_2Earithmetic_2EZERO))))))) \wedge ((\forall V9t1 \in ty_2Enum_2Enum. \\
& \quad \quad (\exists V10t2 \in ty_2Enum_2Enum.((p (ap V2a (ap (ap c_2Earithmetic_2E_2B \\
& \quad \quad V9t1) V10t2))) \Rightarrow (p (ap V7q (ap (ap c_2Earithmetic_2E_2B V9t1) V10t2))))))) \wedge \\
& \quad (p (ap V0Phi V7q))))))) \wedge (((p (ap V0Phi (ap c_2ETemporal_Logic_2EEVENTUAL \\
& \quad V2a))) \Leftrightarrow (\exists V11q \in (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V12t \in \\
& \quad ty_2Enum_2Enum.((p (ap V11q V12t)) \Leftrightarrow ((p (ap V2a V12t)) \vee (p (ap V11q \\
& \quad (ap (ap c_2Earithmetic_2E_2B V12t) (ap c_2Earithmetic_2ENUMERAL \\
& \quad \quad (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))))))) \wedge \\
& \quad (\forall V13t1 \in ty_2Enum_2Enum.(\exists V14t2 \in ty_2Enum_2Enum. \\
& \quad \quad ((p (ap V11q (ap (ap c_2Earithmetic_2E_2B V13t1) V14t2))) \Rightarrow (p (ap \\
& \quad \quad V2a (ap (ap c_2Earithmetic_2E_2B V13t1) V14t2))))))) \wedge (p (ap V0Phi \\
& \quad \quad V11q))))))) \wedge (((p (ap V0Phi (ap (ap c_2ETemporal_Logic_2ESUNTIL \\
& \quad V2a) V3b))) \Leftrightarrow (\exists V15q \in (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V16t \in \\
& \quad ty_2Enum_2Enum.((p (ap V15q V16t)) \Leftrightarrow ((p (ap V3b V16t)) \vee ((p (ap V2a \\
& \quad V16t)) \wedge (p (ap V15q (ap (ap c_2Earithmetic_2E_2B V16t) (ap c_2Earithmetic_2ENUMERAL \\
& \quad \quad (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))))))) \wedge \\
& \quad ((\forall V17t1 \in ty_2Enum_2Enum.(\exists V18t2 \in ty_2Enum_2Enum. \\
& \quad \quad ((p (ap V15q (ap (ap c_2Earithmetic_2E_2B V17t1) V18t2))) \Rightarrow ((\neg(\\
& \quad \quad p (ap V2a (ap (ap c_2Earithmetic_2E_2B V17t1) V18t2))) \vee (p (ap V3b \\
& \quad \quad (ap (ap c_2Earithmetic_2E_2B V17t1) V18t2))))))) \wedge (p (ap V0Phi \\
& \quad \quad V15q))))))) \wedge (((p (ap V0Phi (ap (ap c_2ETemporal_Logic_2EUNTIL \\
& \quad V2a) V3b))) \Leftrightarrow (\exists V19q \in (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V20t \in \\
& \quad ty_2Enum_2Enum.((p (ap V19q V20t)) \Leftrightarrow ((p (ap V3b V20t)) \vee ((p (ap V2a \\
& \quad V20t)) \wedge (p (ap V19q (ap (ap c_2Earithmetic_2E_2B V20t) (ap c_2Earithmetic_2ENUMERAL \\
& \quad \quad (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))))))) \wedge \\
& \quad ((\forall V21t1 \in ty_2Enum_2Enum.(\exists V22t2 \in ty_2Enum_2Enum. \\
& \quad \quad ((\neg(p (ap V19q (ap (ap c_2Earithmetic_2E_2B V21t1) V22t2))) \Rightarrow (\\
& \quad \quad (\neg(p (ap V2a (ap (ap c_2Earithmetic_2E_2B V21t1) V22t2))) \vee (p (ap \\
& \quad \quad V3b (ap (ap c_2Earithmetic_2E_2B V21t1) V22t2))))))) \wedge (p (ap \\
& \quad V0Phi V19q))))))) \wedge (((p (ap V0Phi (ap (ap c_2ETemporal_Logic_2ESWHEN \\
& \quad V2a) V3b))) \Leftrightarrow (\exists V23q \in (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V24t \in \\
& \quad ty_2Enum_2Enum.((p (ap V23q V24t)) \Leftrightarrow (p (ap (ap (c_2Ebool_2ECOND \\
& \quad 2) (ap V3b V24t)) (ap V2a V24t)) (ap V23q (ap (ap c_2Earithmetic_2E_2B \\
& \quad V24t) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad c_2Earithmetic_2EZERO))))))) \wedge ((\forall V25t1 \in ty_2Enum_2Enum. \\
& \quad (\exists V26t2 \in ty_2Enum_2Enum.((p (ap V23q (ap (ap c_2Earithmetic_2E_2B \\
& \quad V25t1) V26t2))) \Rightarrow (p (ap V3b (ap (ap c_2Earithmetic_2E_2B V25t1) \\
& \quad V26t2))))))) \wedge (p (ap V0Phi V23q))))))) \wedge (((p (ap V0Phi (ap (ap c_2ETemporal_Logic_2EWHEN \\
& \quad V2a) V3b))) \Leftrightarrow (\exists V27q \in (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V28t \in \\
& \quad ty_2Enum_2Enum.((p (ap V27q V28t)) \Leftrightarrow (p (ap (ap (c_2Ebool_2ECOND \\
& \quad 2) (ap V3b V28t)) (ap V2a V28t)) (ap V27q (ap (ap c_2Earithmetic_2E_2B \\
& \quad V28t) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad c_2Earithmetic_2EZERO))))))) \wedge ((\forall V29t1 \in ty_2Enum_2Enum. \\
& \quad (\exists V30t2 \in ty_2Enum_2Enum.((p (ap V27q (ap (ap c_2Earithmetic_2E_2B V29t1) \\
& \quad V30t2))))))) \wedge (p (ap V0Phi V27q))))))) \wedge (((p (ap V0Phi (ap (ap c_2ETemporal_Logic_2ESBEFORE \\
& \quad V2a) V3b))) \Leftrightarrow (\exists V31a \in (2^{ty_2Enum_2Enum}).(True \wedge ((\forall V32t \in
\end{aligned}$$