

thm\_2ETemporal\_\_Logic\_2EIMP\_\_NEXT (TM-MaftzjckzSQR8kynRRWDUDgxpsR1KJXXH)

October 26, 2020

**Definition 1** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p \Rightarrow p \ Q)$  of type  $\iota$ .

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Enum\_2Enum \quad (1)$$

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \quad (2)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega}) \quad (3)$$

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{\omega}) \quad (4)$$

**Definition 2** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define  $c\_2Ebool\_2ET$  to be  $(ap (ap (c\_2Emin\_2E\_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

**Definition 4** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A\_27a : \iota.(\lambda V0P \in (2^{A\_27a}).(ap (ap (c\_2Emin\_2E\_3D (2^{A\_27a})) (\lambda V1x \in 2.V1x)) (\lambda V2x \in 2.V2x)))$

**Definition 5** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.(ap c\_2Enum\_2EABS\_num (m))$

**Definition 6** We define  $c\_2ETemporal__Logic_2ENEXT$  to be  $\lambda V0P \in (2^{ty\_2Enum\_2Enum}).(\lambda V1t \in ty\_2Enum\_2Enum.(ap c\_2Ebool\_2ET (V1t)))$

Assume the following.

$$True \quad (5)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow True)) \quad (6)$$

**Theorem 1**

$$\begin{aligned} & (\forall V0Q \in (2^{ty\_2Enum\_2Enum}).(\forall V1P \in (2^{ty\_2Enum\_2Enum}). \\ & ((ap\ c\_2ETemporal\_Logic\_2ENEXT\ (\lambda V2t \in ty\_2Enum\_2Enum.\( \\ & ap\ (ap\ c\_2Emin\_2E\_3D\_3D\_3E\ (ap\ V1P\ V2t))\ (ap\ V0Q\ V2t)))) = (\lambda V3t \in \\ & ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Emin\_2E\_3D\_3D\_3E\ (ap\ (ap\ c\_2ETemporal\_Logic\_2ENEXT\ V1P)\ V3t))\ (ap\ (ap\ c\_2ETemporal\_Logic\_2ENEXT\ V0Q)\ V3t)))))) \end{aligned}$$