

thm_2Earithmetic_2EDIV_LESS
 (TMQA1jWy39cLTzPRY7qBpdQBGbBuPkiKztB)

October 26, 2020

Definition 1 We define $c_2Emin_2E_40$ to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p (ap P x)) \text{ then } (\text{the } (\lambda x. x \in A \wedge p \text{ of type } \iota \Rightarrow \iota))$

Definition 2 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y) \text{ of type } \iota \Rightarrow \iota$.

Definition 3 We define $c_2Ebool_2E_3F$ to be $\lambda A. \lambda a : \iota. (\lambda V0P \in (2^{A-27a}). (ap V0P (ap (c_2Emin_2E_40 A) (c_2Emin_2E_3D A))))$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$\text{nonempty } ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (3)$$

Definition 4 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 5 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (4)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (5)$$

Definition 6 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2. V0x)) (\lambda V1x \in 2. V1x)))$

Definition 7 We define $c_2Ebool_2E_21$ to be $\lambda A. \lambda a : \iota. (\lambda V0P \in (2^{A-27a}). (ap (ap (c_2Emin_2E_3D (2^{A-27a})) (c_2Emin_2E_40 A)))$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num\ 0)$

Let c_2 be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum ty_2Enum_2Enum_2Enum) ty_2Enum_2Enum) \quad (6)$$

Definition 9 We define `c_2Earithmetic_2EBIT1` to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earithmetic_2EBIT1\ n)\ V0)$

Definition 10 We define `c_2Earithmetic_2ENUMERAL` to be $\lambda V0x \in ty_2Enum_2Enum. V0x$.

Let c_2 be given. Assume the following.

$c_2Earithmetic_2EMOD \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum}^{ty_2Enum_2Enum})^*$

Let c_2 be given. Assume the following.

$c : \text{Earithmetic} \rightarrow ((tu : \text{Enum}) \rightarrow (\text{ty_enum_enum} : \text{Enum}))$

Let $c_2Earithmetic_2EDIV : \iota$ be given. Assume the following. (8)

$$2E_{\text{kin}}(t) = t \cdot \langle \partial E D W \rangle \approx \langle (t - 2E_{\text{kin}})^2 \rangle / 2E_{\text{kin}}^2$$

of type ι .

Definition 15 We define $\mathbb{Z}_{\text{LEDDER}}[x]$ to be $\{x^k \mid k \in \mathbb{Z}\}$, $\mathbb{Z}_{\text{LEDDER}}[x_1, x_2] \subseteq \mathbb{Z}[x_1, x_2]$, $\mathbb{Z}_{\text{LEDDER}}[x_1, x_2, x_3] \subseteq \mathbb{Z}[x_1, x_2, x_3]$, etc.

Definition 14 We define $C_{\leq LBBG1-2COND}$ to be $\lambda X.2\lambda a.\lambda i.(\lambda V.3i \in \mathbb{Z}.(\lambda V.4i \in A.2\lambda a.(\lambda V.5i \in A.2\lambda a.))$

Definition 19 We define $\mathcal{C}_2\text{-Eprim}\text{-rec}_2\text{-ETRE}$ to be $\lambda V\;Sm \in \nu g_\mathcal{C}_2\text{-ETRE}.\;nam_\mathcal{C}_2\text{-ETRE}.\;(ap\;(ap\;(ap\;(ap\;(\mathcal{C}_2\text{-EBOU2}\;Sm\;V)\;Sm\;G)\;Sm\;H)\;Sm\;I)\;Sm\;J)$

Definition 16 We define $c_{\text{ZEBB01-ZE-5C-2F}}$ to be $(\forall v \in \mathbb{Z}. (\forall t_1 \in \mathbb{Z}. (\forall t_2 \in \mathbb{Z}. (ap(c_{\text{ZEBB01-ZE-21-2}}) (\forall z \in \mathbb{Z}.$

Definition 17 We define $c_2EBpool_2E_7E$ to be $(\lambda V \; Ut \in 2.(ap \; (ap \; c_2Emin_2E_3D_3D_3E \; V \; Ut) \; c_2EBpool_2E))$

Definition 18 We define $c_2\text{Eprim_rec_}2E3C$ to be $\lambda V 0 m \in ty_2Enum_2Enum.\lambda V 1 n \in ty_2Enum_2Enum.$

Assume the following.

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Assume the following.

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (ap (ap c_2Earithmetic_2E_2B V0m) V1n) = (ap (ap c_2Earithmetic_2E_2B V1n) V0m)))) \quad (12)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\forall V2p \in ty_2Enum_2Enum. ((ap (ap c_2Earithmetic_2E_2B V0m) (ap (ap c_2Earithmetic_2E_2B V1n) V2p)) = (ap (ap c_2Earithmetic_2E_2B (ap (ap c_2Earithmetic_2E_2B V0m) V1n)) V2p)))))) \quad (13)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.((V0m = c_2Enum_2E0) \vee (\exists V1n \in ty_2Enum_2Enum.(V0m = (ap\ c_2Enum_2ESUC\ V1n))))) \quad (14)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (p (ap (ap c_2Eprim_rec_2E_3C (ap c_2Enum_2ESUC V0m)) (ap c_2Enum_2ESUC V1n))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n)))) \quad (15)$$

Assume the following.

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$$(\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\forall V2p \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n)) \Rightarrow (p (ap (ap c_2Eprim_rec_2E_3C (ap (ap c_2Earithmetic_2E_2B V0m) V2p)) (ap (ap c_2Earithmetic_2E_2B V1n) V2p))))))) \quad (17)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) V0n)) \Rightarrow (\forall V1k \in ty_2Enum_2Enum. ((V1k = (ap (ap c_2Earithmetic_2E_2B (ap (ap c_2Earithmetic_2E_2A (ap (ap c_2Earithmetic_2EDIV V1k) V0n)) (ap (ap c_2Earithmetic_2EMOD V1k) V0n))) \wedge (p (ap (ap c_2Eprim_rec_2E_3C (ap (ap c_2Earithmetic_2EMOD V1k) V0n)) V0n))))))) \quad (18)$$

Assume the following.

$$(\forall V0r \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C V0r) V1n)) \Rightarrow ((ap (ap c_2Earithmetic_2EDIV V0r) V1n) = c_2Enum_2E0)))) \quad (19)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) V0n)) \Rightarrow (\forall V1x \in ty_2Enum_2Enum. (\forall V2r \in ty_2Enum_2Enum. ((ap (ap c_2Earithmetic_2EDIV (ap (ap c_2Earithmetic_2E_2B (ap (ap c_2Earithmetic_2E_2A V1x) V0n)) V2r)) V0n) = (ap (ap c_2Earithmetic_2E_2B V1x) (ap (ap c_2Earithmetic_2EDIV V2r) V0n))))))) \quad (20)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) V0m)) \Leftrightarrow ((ap c_2Enum_2ESUC (ap c_2Eprim_rec_2EPRE V0m)) = V0m))) \quad (21)$$

Assume the following.

$$True \quad (22)$$

Assume the following.

$$(\forall V0t \in 2. (((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))) \quad (23)$$

Assume the following.

$$(\forall V0t \in 2. (((True \vee (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \vee True) \Leftrightarrow True) \wedge (((False \vee (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee False) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee (p V0t)) \Leftrightarrow (p V0t)))) \quad (24)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (25)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (26)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (27)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (28)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(p (ap (ap c_2Eprim_rec_2E_3C (ap c_2Enum_2ESUC V0m)) V1n)) \Rightarrow (p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n))))) \quad (29)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.(p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Enum_2ESUC V0n)))) \quad (30)$$

Theorem 1

$$(\forall V0n \in ty_2Enum_2Enum.(\forall V1d \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) V0n)) \wedge (p (ap (ap c_2Eprim_rec_2E_3C (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)) V1d)) \Rightarrow (p (ap (ap c_2Eprim_rec_2E_3C (ap (ap c_2Earithmetic_2EDIV V0n) V1d)) V0n)))))))$$