

thm_2Ebag_2EEMPTY__BAG__alt
(TMaVTWfcBPsVP6vkPrRJYaN9VKYywAd4ZG8)

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Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{1}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{2}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega\omega}) \tag{3}$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Ecombin_2EK$ to be $\lambda A.\lambda a : \iota.\lambda A.\lambda b : \iota.(\lambda V0x \in A.\lambda V1y \in A.\lambda V0x \in A.\lambda V1y \in A.V0x)$

Definition 4 We define $c_2Ebag_2EEMPTY_BAG$ to be $\lambda A.\lambda a : \iota.(ap\ (c_2Ecombin_2EK\ ty_2Enum_2Enum\ a))$

Definition 5 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 6 We define $c_2Ebool_2E_21$ to be $\lambda A.\lambda a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c_2Emin_2E_3D\ (2^{A-27a}))\ P))\ a))$

Assume the following.

$$True \tag{4}$$

Assume the following.

$$\forall A.\lambda a.nonempty\ A.\lambda a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A.\lambda a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \tag{5}$$

Assume the following.

$$\forall A.\lambda a.nonempty\ A.\lambda a \Rightarrow (\forall V0x \in A.\lambda a.((V0x = V0x) \Leftrightarrow True)) \tag{6}$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0f \in (A_27b^{A_27a}).(\forall V1g \in (A_27b^{A_27a}).((V0f = \\ V1g) \Leftrightarrow (\forall V2x \in A_27a.((ap\ V0f\ V2x) = (ap\ V1g\ V2x)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0x \in A_27a.(\forall V1y \in A_27b.((ap\ (ap\ (c_2Ecombin_2EK \\ A_27a\ A_27b)\ V0x)\ V1y) = V0x))) \end{aligned} \quad (8)$$

Theorem 1

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow ((c_2Ebag_2EEMPTY_BAG\ A_27a) = \\ (\lambda V0x \in A_27a.c_2Enum_2E0)) \end{aligned}$$