

thm_2Ebag_2ESET_OF_EL_BAG

(TMLaXqhrnaV7Sq5ZhzE5b1dvrzpg4ovjVMQ)

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Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$\text{nonempty } ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (3)$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Ecombin_2EK$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. (\lambda V0x \in A_27a. (\lambda V1y \in A_27b. V0x))$

Definition 4 We define $c_2Ebag_2EEMPTY_BAG$ to be $\lambda A_27a : \iota. (ap\ (c_2Ecombin_2EK\ ty_2Enum_2Enum\ A_27a))$

Definition 5 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (4)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (5)$$

Definition 6 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2. V0x))\ (\lambda V1x \in 2. V1x))$

Definition 7 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap\ (ap\ (c_2Emin_2E_3D\ (2^{A_27a}))\ P)))$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap\ c_2Enum_2EABS_num\ m)$

Let c_2 be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (6)$$

Definition 9 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap (ap c_2Earithmetic_2EBIT1$

Definition 10 We define $\text{c_2Earthmetic_2ENUMERAL}$ to be $\lambda V0x \in \text{ty_2Enum_2Enum}.V0x.$

Definition 11 We define $c_2Ebool_2E\text{EF}$ to be $(ap\ (c_2Ebool_2E\text{21}\ 2)\ (\lambda V0t \in 2.V0t))$.

Definition 12 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2. \lambda Q \in 2. inj_o(p \ P \Rightarrow p \ Q)$

Definition 13 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_2F_5C)\ t1\ t2)))$

Definition 14. We define \in 2Emin 2E 40 to be $\lambda A \lambda P \in 2^A$ if $(\exists x \in A) p(an(P, x))$ then $(\forall x \in A) x \in P$.

D. Saito, 16 Weeks, 25L = 25RAG, INSERT (4, 1) 4.27, NO. 5, 4.27, NV11 = (4, 2E), 25

Definition 19 We define $\text{C}_\infty^{\text{LBBM}}(A, B)$ to be $\text{X}_\infty^{\text{LBBM}}(A, B) \cap \{x \in A \otimes B \mid (\forall i, j \in \omega)(ap_i \vee b_j \vee \psi_i x)\}$.

Definition 26 We define $C_{2LBB001-2L-SC-21}$ to be $(\forall x \exists y \in Z. (\forall z \exists t \in Z. up(C_{2LBB001-2L-21}) z) (\forall v \in$

$$\forall A0.\text{nonempty } A0 \Rightarrow \forall A1.\text{nonempty } A1 \Rightarrow \text{nonempty } (\text{ty_}2\text{Epair_}2\text{Eprod } A0 \text{ } A1) \quad (7)$$

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_{_27a}.nonempty\ A_{_27a} \Rightarrow \forall A_{_27b}.nonempty\ A_{_27b} \Rightarrow c_{_2Epair_2EABS_prod}\ A_{_27a}\ A_{_27b} \in ((ty_{_2Epair_2Eprod}\ A_{_27a}\ A_{_27b})^{((2^{A_{_27b}})^{A_{_27a}})}) \quad (8)$$

Definition 21 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in A_27a.\lambda V1y \in A_27b.(ap\ (c_2Epair\ A_27a\ A_27b)\ V0\ V1)$

Let $c_2Epred_set_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow \forall A_27b.\text{nonempty } A_27b \Rightarrow c_2E\text{pred_set_2EGSPEC}_A_27a \ A_27b \in ((2^{A_27a})^{((ty_2E\text{pair_2Eprod } A_27a \ 2)^{A_27b})}) \quad (9)$$

Definition 22 We define $c_2E_{\text{pred_set_2E}}\text{INSERT}$ to be $\lambda A.\lambda 27a:\iota.\lambda V0x\in A.\lambda V1s\in(2^{A\cdot 27a}).(ap(c_\cdot$

Definition 23 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2E))$

Definition 24 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_40)))$

Definition 25 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (c_2Eprim_rec_2E_3C V0m) V1n)$

Definition 26 We define $c_2Earithmetic_2E_3E$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (c_2Earithmetic_2E_3E V0m) V1n)$

Definition 27 We define $c_2Earithmetic_2E_3E_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (c_2Earithmetic_2E_3E_3D V0m) V1n)$

Definition 28 We define $c_2Ebag_2EBAG_INN$ to be $\lambda A_27a : \iota.\lambda V0e \in A_27a.\lambda V1n \in ty_2Enum_2Enum.(ap (c_2Ebag_2EBAG_INN A_27a) V1n)$

Definition 29 We define $c_2Ebag_2EBAG_IN$ to be $\lambda A_27a : \iota.\lambda V0e \in A_27a.\lambda V1b \in (ty_2Enum_2Enum^A).(\lambda V1b \in (ty_2Enum_2Enum^A).ap (c_2Ebag_2EBAG_IN A_27a) V1b))$

Definition 30 We define $c_2Ebag_2ESET_OF_BAG$ to be $\lambda A_27a : \iota.\lambda V0b \in (ty_2Enum_2Enum^A).(\lambda V0b \in (ty_2Enum_2Enum^A).ap (c_2Ebag_2ESET_OF_BAG A_27a) V0b))$

Assume the following.

$$\begin{aligned} \forall A_27a. nonempty A_27a \Rightarrow & ((ap (c_2Ebag_2ESET_OF_BAG A_27a) \\ & (c_2Ebag_2EEMPTY_BAG A_27a)) = (c_2Epred_set_2EEMPTY A_27a)) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} \forall A_27a. nonempty A_27a \Rightarrow & (\forall V0e \in A_27a.(\forall V1b \in \\ & (ty_2Enum_2Enum^A).((ap (c_2Ebag_2ESET_OF_BAG A_27a) \\ & (ap (ap (c_2Ebag_2EBAG_INSERT A_27a) V0e) V1b)) = (ap (ap (c_2Epred_set_2EINSERT \\ & A_27a) V0e) (ap (c_2Ebag_2ESET_OF_BAG A_27a) V1b)))))) \end{aligned} \quad (11)$$

Assume the following.

$$True \quad (12)$$

Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in \\ A_27a.(p V0t)) \Leftrightarrow (p V0t))) \quad (13)$$

Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow \\ True)) \quad (14)$$

Theorem 1

$$\begin{aligned} \forall A_27a. nonempty A_27a \Rightarrow & (\forall V0e \in A_27a.((ap (c_2Ebag_2ESET_OF_BAG \\ A_27a) (ap (c_2Ebag_2EEL_BAG A_27a) V0e)) = (ap (ap (c_2Epred_set_2EINSERT \\ A_27a) V0e) (c_2Epred_set_2EEMPTY A_27a)))) \end{aligned}$$