

thm_2Ebag_2Emlt__INSERT__CANCEL_I
 (TMYTNCVU-
 TEUSgVBaqpPa7nuc2kgHbETBj1Z)

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Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$\text{nonempty } ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (3)$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (4)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (5)$$

Definition 4 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 5 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap\ (ap\ (c_2Emin_2E_3D\ (2^{A_27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V2y \in 2.V2y)))$

Definition 6 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap\ c_2Enum_2EABS_num\ m)$

Let c_2 be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (6)$$

Definition 7 We define $c_2Earthmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earthmetic_2EBIT1 n) V)$

Definition 8 We define `c_2Earthmetic_2ENUMERAL` to be $\lambda V0x \in ty_2Enum_2Enum. V0x.$

Definition 9 We define c_2Ebool_2EF to be $(ap(c_2Ebool_2E_21\ 2)(\lambda V0t\ t \in 2.V0t))$.

Definition 10 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o(p\ P \Rightarrow p\ Q)$

Definition 11 We define $c_{\text{Ebool_7E}}$ to be $(\lambda V0t \in 2.(ap\ (ap\ c_{\text{Emin_3D_3D_3E}}\ V\ 0)\ t))$

Definition 12 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in$

Definition 13 We define $\mathcal{C} \in \text{Emin } \text{EF}$ to be $\lambda A. \lambda P \in \text{E}^A$, if $(\exists x \in A) p_1(ap_1 P, x))$, then (the $(\lambda x. x \in A \wedge$

Definition 14. We define a 2Ebool, 2E, 3E to be $\lambda V0R \in (2^A \rightarrow 2^B)$ s.t. $V0R$ is 2Emin, 3E.

Definition 15. We say Σ is a $\Sigma_2\Sigma_3$ type if $N\Sigma = \pi_1(\Sigma)$, $N\Sigma = \Sigma$, $N\Sigma = N\Sigma_1 = \pi_1(\Sigma)$, and $N\Sigma = \Sigma$.

D. S. Wilson, 12 Weeks, 25 March 25, 25 April 25, 25 May 25, 25 June 25, 25 July 25, 25 August 25, 25 September 25, 25 October 25, 25 November 25, 25 December 25.

Definition 16 We define $\text{G}_{\text{max}}(\text{G}_1, \dots, \text{G}_n)$ to be $\text{G}_1 \times \text{G}_2 \times \dots \times \text{G}_n$. In $\text{G}_{\text{max}}(\text{G}_1, \dots, \text{G}_n)$, the elements are pairs (g_1, g_2, \dots, g_n) where $g_i \in \text{G}_i$ for all $i = 1, \dots, n$.

Definition 15 We define $\text{C}_\infty^{\text{alg}}$ to be $\text{R}\text{Hom}_{\mathcal{A}}(\mathcal{X}, \mathcal{X})$ in $\text{dgAlg}_{\text{chain}}$.

Definition 26 We define $\mathcal{C}_{\text{ZEBAG-ZEBAG-EN}}$ to be $\lambda A \cdot \lambda t \cdot \lambda V \; \text{de} \in A \cdot \lambda t \cdot \lambda V \; \text{to} \in (\text{ig-ZEBAG-ZEBAG})$

Definition 21 We define $C_2Ecombin_2EK$ to be $\lambda A_2Id : t.\lambda A_2Id : t.(\lambda V\ 0x \in A_2Id.(\lambda V\ 1y \in A_2Id.0x))$

Definition 22 We define $c_2Ebag_2EEEMPTY_2BAG$ to be $\lambda A_27a : \iota.(ap\ (c_2Ecombin_2EK\ ty_2Enum_2En)$

Definition 23 We define $c.2Ebool_2ECOND$ to be $\lambda A.27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A.27a.(\lambda V2t2 \in A.27a.($

Definition 24 We define $c_2EBag_2EBAG_INSERT$ to be $\lambda A_27a : \iota. \lambda V0e \in A_27a. \lambda V1b \in (ty_2Enum_2E$

Definition 25 We define $c_2EBag_2EBAG_UNION$ to be $\lambda A_27a : \iota.\lambda V0b \in (ty_2Enum_2Enum^A_{27a}).\lambda V1$

Definition 26 We define $c_2.Ebag_2EFINITE_BAG$ to be $\lambda A.\lambda 27a : \iota.\lambda V0b \in (ty_2Enum_2Enum^A_{27a}).(ap$

Definition 27 We define $\mathbf{c} \in \mathbf{Ebag} \cap \mathbf{Emlt1}$ to be $\lambda A \exists 27a : \iota \cdot \lambda V0r \in ((2^{A \cdot 27a})^A)^{A \cdot 27a}, \lambda V1b \in (tu \cdot \mathbf{Enum} \cdot \mathbf{Ebag})^A$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. nonempty A_{27a} \Rightarrow (\forall V0e \in A_{27a}. (\forall V1b1 \in \\
& (ty_2Enum_2Enum^{A_{27a}}). (\forall V2b2 \in (ty_2Enum_2Enum^{A_{27a}}). \\
& ((ap (ap (c_2Ebag_2EBAG_UNION A_{27a}) (ap (ap (c_2Ebag_2EBAG_INSERT \\
& A_{27a}) V0e) V1b1)) V2b2) = (ap (ap (c_2Ebag_2EBAG_INSERT A_{27a}) \\
& V0e) (ap (ap (c_2Ebag_2EBAG_UNION A_{27a}) V1b1) V2b2))) \wedge ((ap (\\
& ap (c_2Ebag_2EBAG_UNION A_{27a}) V1b1) (ap (ap (c_2Ebag_2EBAG_INSERT \\
& A_{27a}) V0e) V2b2)) = (ap (ap (c_2Ebag_2EBAG_INSERT A_{27a}) V0e) \\
& (ap (ap (c_2Ebag_2EBAG_UNION A_{27a}) V1b1) V2b2))))))) \\
& (7)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. nonempty A_{27a} \Rightarrow (\forall V0x \in A_{27a}. (\forall V1y \in \\
& A_{27a}. (\forall V2b \in (ty_2Enum_2Enum^{A_{27a}}). ((ap (ap (c_2Ebag_2EBAG_INSERT \\
& A_{27a}) V0x) V2b) = (ap (ap (c_2Ebag_2EBAG_INSERT A_{27a}) V1y) V2b)) \Leftrightarrow \\
& (V0x = V1y)))))) \\
& (8)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. nonempty A_{27a} \Rightarrow \forall A_{27b}. nonempty A_{27b} \Rightarrow \forall A_{27c}. \\
& nonempty A_{27c} \Rightarrow ((\forall V0b \in (ty_2Enum_2Enum^{A_{27a}}). ((ap (ap \\
& (c_2Ebag_2EBAG_UNION A_{27a}) V0b) (c_2Ebag_2EEMPTY_BAG A_{27a})) = \\
& V0b) \wedge ((\forall V1b \in (ty_2Enum_2Enum^{A_{27b}}). ((ap (ap (c_2Ebag_2EBAG_UNION \\
& A_{27b}) (c_2Ebag_2EEMPTY_BAG A_{27b})) V1b) = V1b)) \wedge (\forall V2b1 \in \\
& (ty_2Enum_2Enum^{A_{27c}}). (\forall V3b2 \in (ty_2Enum_2Enum^{A_{27c}}). \\
& (((ap (ap (c_2Ebag_2EBAG_UNION A_{27c}) V2b1) V3b2) = (c_2Ebag_2EEMPTY_BAG \\
& A_{27c})) \Leftrightarrow ((V2b1 = (c_2Ebag_2EEMPTY_BAG A_{27c})) \wedge (V3b2 = (c_2Ebag_2EEMPTY_BAG \\
& A_{27c})))))))))) \\
& (9)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. nonempty A_{27a} \Rightarrow ((p (ap (c_2Ebag_2EFINITE_BAG \\
& A_{27a}) (c_2Ebag_2EEMPTY_BAG A_{27a}))) \wedge (\forall V0e \in A_{27a}. (\\
& \forall V1b \in (ty_2Enum_2Enum^{A_{27a}}). ((p (ap (c_2Ebag_2EFINITE_BAG \\
& A_{27a}) (ap (ap (c_2Ebag_2EBAG_INSERT A_{27a}) V0e) V1b))) \Leftrightarrow (p (ap \\
& (c_2Ebag_2EFINITE_BAG A_{27a}) V1b))))))) \\
& (10)
\end{aligned}$$

Assume the following.

$$True \quad (11)$$

Assume the following.

$$\forall A_{27a}. nonempty A_{27a} \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_{27a}. (p V0t)) \Leftrightarrow (p V0t))) \quad (12)$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2. (((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow \\
& (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge \\
& (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))))) \\
& (13)
\end{aligned}$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (14)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (15)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (16)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (17)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (18)$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1x_27 \in 2.(\forall V2y \in 2.(\forall V3y_27 \in 2.(((p V0x) \Leftrightarrow (p V1x_27)) \wedge ((p V1x_27) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_27)))) \Rightarrow (((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_27) \Rightarrow (p V3y_27))))))) \quad (19)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0R \in ((2^{A_27a})^{A_27a}). \\ & \quad (\forall V1f \in (A_27a^{A_27a}).(\forall V2x \in A_27a.(\forall V3y \in A_27a.((p (ap (ap V0R V2x) V3y)) \Rightarrow (p (ap (ap V0R (ap V1f V2x)) (ap V1f V3y)))))) \Rightarrow (\forall V4x \in A_27a.(\forall V5y \in A_27a.((p (ap (ap (ap (c_2Erelation_2ETC A_27a) V0R) V4x) V5y)) \Rightarrow (p (ap (ap (ap (c_2Erelation_2ETC A_27a) V0R) (ap V1f V4x)) (ap V1f V5y)))))))))) \quad (20) \end{aligned}$$

Theorem 1

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0R \in ((2^{A_27a})^{A_27a}). \\ & \quad (\forall V1e \in A_27a.(\forall V2a \in (ty_2Enum_2Enum^{A_27a}).(\forall V3b \in (ty_2Enum_2Enum^{A_27a}).((p (ap (ap (ap (c_2Erelation_2ETC (ty_2Enum_2Enum^{A_27a})) (ap (c_2Ebag_2Emlt1 A_27a) V0R)) V2a) V3b)) \Rightarrow (p (ap (ap (ap (c_2Erelation_2ETC (ty_2Enum_2Enum^{A_27a})) (ap (c_2Ebag_2Emlt1 A_27a) V0R)) (ap (ap (c_2Ebag_2EBAG_INSERT A_27a) V1e) V2a)) (ap (ap (c_2Ebag_2EBAG_INSERT A_27a) V1e) V3b)))))))))) \quad (21) \end{aligned}$$