

thm_2Ebag_2Emove__BAG__UNION__over__eq
(TMTmFmUZDJ5ySE6bakdjq9aorN1sHvX5Jza)

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Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

nonempty *ty_2Enum_2Enum* (1)

Let $c_2E\text{arithmetic}_2E\text{B} : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (2)$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o(x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A.27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ ap\ (ap\ (c_2Emin_2E_3D\ (2^{A-27a}\ P)\ V)\ 0)\ P))$

Definition 4 We define $c_2EBag_2EBAG_UNION$ to be $\lambda A.\lambda 27a : \iota.\lambda V0b \in (ty_2Enum_2Enum^A_{27a}).\lambda V1c$

Let c_2 be given. Assume the following.

$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum} \dots$

(3)

Definition 6 We define $c \in \text{Ebool} \cap \text{EE}$ to be (an $(c \in \text{Ebool} \cap \text{EE}, 21, 2)$, $(\lambda V0t \in V0t)$)

Definition 7 We define \subseteq 2Emin , 2E , 3D , 3D , 3E to be $\lambda P \in \text{2} \cdot \lambda Q \in \text{2}$ in $i \in o(n)$, $P \rightarrowtail Q$

Definition 8. We define \subset , 2Ebool , 2E , 5C to be $(\lambda V_0 t_1 \in 2) (\lambda V_1 t_2 \in 2)$ (\in) $(\subset$, 2Ebool ,

Definition 9. We define a 2Ehol-2E-ZE to be $(\forall V \in 2^{\omega} : (\exists n \in \omega : (\forall m \in \omega : 2E_{min}(2E_3D_3D_3E, V) \in 2Ehol(2E_3D_3D_3E)))$

D-6-Me-10-W-1-S = 2EI + 1CE-EG-2E-1-1-(NU101-2-(NU110-2-((c-2EI + 1CE-21-2)-(NU1-

Assume the following.

$$(\forall V0a \in ty_2Enum_2Enum. (\forall V1c \in ty_2Enum_2Enum. (ap (ap (ap c_2Earithmetic_2E_2D (ap (ap c_2Earithmetic_2E_2B V0a) V1c)) V1c) = V0a))) \quad (4)$$

Assume the following.

$$True \quad (5)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_27a. (p V0t) \Leftrightarrow (p V0t)))) \quad (6)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (7)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (8)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))) \quad (9)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (((p V0A) \Rightarrow (p V1B)) \Leftrightarrow ((\neg(p V0A)) \vee (p V1B)))) \quad (10)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0f \in (2^{A_27a}). (\forall V1v \in A_27a. ((\forall V2x \in A_27a. ((V2x = V1v) \Rightarrow (p (ap V0f V2x)))) \Leftrightarrow (p (ap V0f V1v))))) \quad (11)$$

Theorem 1

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0X \in (ty_2Enum_2Enum^{A_27a}). \\ & (\forall V1Y \in (ty_2Enum_2Enum^{A_27a}). (\forall V2Z \in (ty_2Enum_2Enum^{A_27a}). \\ & (((ap (ap (c_2Ebag_2EBAG_UNION A_27a) V0X) V1Y) = V2Z) \Rightarrow (V0X = (\\ & \quad ap (ap (c_2Ebag_2EBAG_DIFF A_27a) V2Z) V1Y))))))) \end{aligned}$$