

thm_2Ebinary_ieee_2Efloat_compare_EQ_float_compare (TMWeGsdsMc8zVEktt4FcM5vPAbd26W4683)

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Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{1}$$

Let $ty_2Ebinary_ieee_2Efloat_compare : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ebinary_ieee_2Efloat_compare \tag{2}$$

Let $c_2Ebinary_ieee_2Efloat_compare2num : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Efloat_compare2num \in (ty_2Enum_2Enum^{ty_2Ebinary_ieee_2Efloat_compare}) \tag{3}$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define c_2Ebool_2E21 to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E3D (2^{A_27a})))$

Assume the following.

$$\begin{aligned} & (\forall V0a \in ty_2Ebinary_ieee_2Efloat_compare.(\forall V1a_27 \in \\ & ty_2Ebinary_ieee_2Efloat_compare.(((ap\ c_2Ebinary_ieee_2Efloat_compare2num \\ & V0a) = (ap\ c_2Ebinary_ieee_2Efloat_compare2num\ V1a_27)) \Leftrightarrow (\\ & V0a = V1a_27)))) \end{aligned} \tag{4}$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \tag{5}$$

Theorem 1

$$\begin{aligned} & (\forall V0a \in ty_2Ebinary_ieee_2Efloat_compare.(\forall V1a_27 \in \\ & ty_2Ebinary_ieee_2Efloat_compare.((V0a = V1a_27) \Leftrightarrow ((ap\ c_2Ebinary_ieee_2Efloat_compare2num \\ & V0a) = (ap\ c_2Ebinary_ieee_2Efloat_compare2num\ V1a_27)))) \end{aligned}$$