

thm\_2Ebinary\_ieee\_2Efloat\_infinity\_negate\_abs  
 (TM-  
 PhejX1WMUzvRoPWjevHZeYoarY8eBMm5D)

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Let  $ty\_2Efc\_2Ecart : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty\_2Efc\_2Ecart\ A0\ A1) \quad (1)$$

Let  $ty\_2Ebinary\_ieee\_2Efloat : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty\_2Ebinary\_ieee\_2Efloat\ A0\ A1) \quad (2)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Significand : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Significand\ A\_27t\ A\_27w \in ((ty\_2Efc\_2Ecart\ 2\ A\_27t)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)}) \quad (3)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Exponent : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Exponent\ A\_27t\ A\_27w \in ((ty\_2Efc\_2Ecart\ 2\ A\_27w)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)}) \quad (4)$$

Let  $ty\_2Eone\_2Eone : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Eone\_2Eone \quad (5)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Sign : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Sign\ A\_27t\ A\_27w \in ((ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)}) \quad (6)$$

Let  $c\_2Enum\_2EZERO\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2EZERO\_REP \in \omega \quad (7)$$

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Enum\_2Enum \quad (8)$$

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{omega}) \quad (9)$$

**Definition 1** We define  $c\_2Emin\_2E3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 2** We define  $c\_2Enum\_2E0$  to be  $(ap\ c\_2Enum\_2EABS\_num\ c\_2Enum\_2EZERO\_REP)$ .

**Definition 3** We define  $c\_2Earithmetic\_2EZERO$  to be  $c\_2Enum\_2E0$ .

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (omega^{ty\_2Enum\_2Enum}) \quad (10)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (omega^{omega}) \quad (11)$$

**Definition 4** We define  $c\_2Ebool\_2ET$  to be  $(ap\ (ap\ (c\_2Emin\_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

**Definition 5** We define  $c\_2Ebool\_2E21$  to be  $\lambda A.\lambda \tau a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c\_2Emin\_2E3D\ (2^{A-27a}))\ (\lambda V1P \in 2.V1P))\ (\lambda V0Q \in 2.V0Q))\ (\lambda V1Q \in 2.V1Q))$

**Definition 6** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.(ap\ c\_2Enum\_2EABS\_num\ (c\_2Enum\_2ESUC\_REP\ m))$

Let  $c\_2Earithmetic\_2E2B : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2E2B \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (12)$$

**Definition 7** We define  $c\_2Earithmetic\_2EBIT1$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Earithmetic\_2E2B\ (V0n))\ (V0n))$

**Definition 8** We define  $c\_2Earithmetic\_2ENUMERAL$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.V0x$ .

**Definition 9** We define  $c\_2Earithmetic\_2EBIT2$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Earithmetic\_2E2B\ (V0n))\ (V0n))$

Let  $c\_2Earithmetic\_2EEXP : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2EEXP \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (13)$$

Let  $c\_2Earithmetic\_2EDIV : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2EDIV \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (14)$$

**Definition 10** We define  $c\_2Ebit\_2EDIV\_2EXP$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Earithmetic\_2EDIV\ (V0x))\ (V1n))$

Let  $c\_2Earithmetic\_2E\_2D : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2E\_2D \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (15)$$

Let  $c\_2Earithmetic\_2EMOD : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2EMOD \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (16)$$

**Definition 11** We define  $c\_2Ebit\_2EMOD\_2EXP$  to be  $\lambda V0x \in ty\_2Enum\_2Enum. \lambda V1n \in ty\_2Enum\_2Enum$

**Definition 12** We define  $c\_2Ebit\_2EBITS$  to be  $\lambda V0h \in ty\_2Enum\_2Enum. \lambda V1l \in ty\_2Enum\_2Enum. \lambda V$

**Definition 13** We define  $c\_2Ebit\_2EBIT$  to be  $\lambda V0b \in ty\_2Enum\_2Enum. \lambda V1n \in ty\_2Enum\_2Enum. (ap$

Let  $ty\_2EfcP\_2Efinite\_image : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0. nonempty A0 \Rightarrow nonempty (ty\_2EfcP\_2Efinite\_image A0) \quad (17)$$

Let  $ty\_2Ebool\_2Eitself : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0. nonempty A0 \Rightarrow nonempty (ty\_2Ebool\_2Eitself A0) \quad (18)$$

Let  $c\_2Ebool\_2Ethe\_value : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a. nonempty A\_27a \Rightarrow c\_2Ebool\_2Ethe\_value A\_27a \in (ty\_2Ebool\_2Eitself A\_27a) \quad (19)$$

Let  $c\_2EfcP\_2Edimindex : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a. nonempty A\_27a \Rightarrow c\_2EfcP\_2Edimindex A\_27a \in (ty\_2Enum\_2Enum^{(ty\_2Ebool\_2Eitself A\_27a)}) \quad (20)$$

**Definition 14** We define  $c\_2Ebool\_2EF$  to be  $(ap (c\_2Ebool\_2E\_21 2) (\lambda V0t \in 2. V0t))$ .

**Definition 15** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2. \lambda Q \in 2. inj\_o (p P \Rightarrow p Q)$  of type  $\iota$ .

**Definition 16** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2. (ap (ap c\_2Emin\_2E\_3D\_3D\_3E V0t) c\_2Ebool\_2E\_21 2))$

**Definition 17** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in 2. V2t))))$

**Definition 18** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A. \lambda P \in 2^A. if (\exists x \in A. p (ap P x)) then (the (\lambda x. x \in A \wedge p (ap P x)))$  of type  $\iota \Rightarrow \iota$ .

**Definition 19** We define  $c\_2Ebool\_2E\_3F$  to be  $\lambda A\_27a : \iota. (\lambda V0P \in (2^{A\_27a}). (ap V0P (ap (c\_2Emin\_2E\_40 A\_27a) P)))$

**Definition 20** We define  $c\_2Eprim\_rec\_2E\_3C$  to be  $\lambda V0m \in ty\_2Enum\_2Enum. \lambda V1n \in ty\_2Enum\_2Enum$

**Definition 21** We define  $c\_2Ebool\_2E\_3F\_21$  to be  $\lambda A\_27a : \iota. (\lambda V0P \in (2^{A\_27a}). (ap (ap c\_2Ebool\_2E\_2F\_5C A\_27a) P)))$

**Definition 22** We define  $c\_2Efc\_2Efinite\_index$  to be  $\lambda A\_27a : \iota.(ap (c\_2Emin\_2E40 (A\_27a^{ty\_2Enum\_2Enum}$

Let  $c\_2Efc\_2Edest\_cart : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Efc\_2Edest\_cart \\ & A\_27a A\_27b \in ((A\_27a^{(ty\_2Efc\_2Efinite\_image A\_27b)})^{(ty\_2Efc\_2Ecart A\_27a A\_27b)}) \end{aligned} \quad (21)$$

**Definition 23** We define  $c\_2Efc\_2Efc\_index$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0x \in (ty\_2Efc\_2Ecart A\_27a$

**Definition 24** We define  $c\_2Efc\_2EFCP$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.(\lambda V0g \in (A\_27a^{ty\_2Enum\_2Enum}).(ap$

**Definition 25** We define  $c\_2Ewords\_2En2w$  to be  $\lambda A\_27a : \iota.\lambda V0n \in ty\_2Enum\_2Enum.(ap (c\_2Efc\_2EFC$

**Definition 26** We define  $c\_2Ecombin\_2EK$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.(\lambda V0x \in A\_27a.(\lambda V1y \in A\_27b.V0x)$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Sign\_fupd : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty A\_27t \Rightarrow \forall A\_27w.nonempty A\_27w \Rightarrow c\_2Ebinary\_ieee\_ \\ & A\_27t A\_27w \in (((ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27w)^{(ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27w)})^{(ty\_2Efc\_2Ecart A\_27t A\_27w)}) \end{aligned} \quad (22)$$

**Definition 27** We define  $c\_2Ebinary\_ieee\_2Efloat\_abs$  to be  $\lambda A\_27t : \iota.\lambda A\_27w : \iota.\lambda V0x \in (ty\_2Ebinary\_i$

Let  $c\_2Ebool\_2EARB : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Ebool\_2EARB A\_27a \in A\_27a \quad (23)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Significand\_fupd : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty A\_27t \Rightarrow \forall A\_27u.nonempty A\_27u \Rightarrow \forall A\_27w.nonempty A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Significand\_fupd \\ & A\_27t A\_27u A\_27w \in (((ty\_2Ebinary\_ieee\_2Efloat A\_27u A\_27w)^{(ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27w)})^{(ty\_2Efc\_2Ecart A\_27t A\_27w)}) \end{aligned} \quad (24)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty A\_27t \Rightarrow \forall A\_27w.nonempty A\_27w \Rightarrow \forall A\_27x.nonempty A\_27x \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd \\ & A\_27w A\_27x \in (((ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27x)^{(ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27w)})^{(ty\_2Efc\_2Ecart A\_27t A\_27w)}) \end{aligned} \quad (25)$$

Let  $ty\_2Epair\_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty\_2Epair\_2Eprod A0 A1) \quad (26)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty A\_27t \Rightarrow \forall A\_27w.nonempty A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity \\ & A\_27t A\_27w \in ((ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27w)^{(ty\_2Ebool\_2Eitself (ty\_2Epair\_2Eprod A\_27t A\_27w)}) \end{aligned} \quad (27)$$



**Definition 39** We define  $c\_Ewords\_2Ew2n$  to be  $\lambda A\_27a : \iota.\lambda V0w \in (ty\_2EfcP\_2Ecart\ 2\ A\_27a).(ap\ (ap\ c\_Ew2n\ V0w\ w))$

**Definition 40** We define  $c\_Ewords\_2Eword\_2comp$  to be  $\lambda A\_27a : \iota.\lambda V0w \in (ty\_2EfcP\_2Ecart\ 2\ A\_27a).$

**Definition 41** We define  $c\_Ewords\_2Eword\_2add$  to be  $\lambda A\_27a : \iota.\lambda V0v \in (ty\_2EfcP\_2Ecart\ 2\ A\_27a).\lambda V1w$

**Definition 42** We define  $c\_Ewords\_2Eword\_2sub$  to be  $\lambda A\_27a : \iota.\lambda V0v \in (ty\_2EfcP\_2Ecart\ 2\ A\_27a).\lambda V1w$

Let  $c\_Ewords\_2EUINT\_2MAX : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_Ewords\_2EUINT\_2MAX\ A\_27a \in ( ty\_2Enum\_2Enum^{(ty\_2Ebool\_2Eitself\ A\_27a)} ) \quad (34)$$

**Definition 43** We define  $c\_Ewords\_2Eword\_2T$  to be  $\lambda A\_27a : \iota.(ap\ (c\_Ewords\_2En2w\ A\_27a)\ (ap\ (c\_Ew2n\ V0w\ w)))$

**Definition 44** We define  $c\_2Earithmetic\_2E\_23C\_23D$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum.$

Assume the following.

$$((ap\ c\_2Earithmetic\_2ENUMERAL\ c\_2Earithmetic\_2EZERO) = c\_2Enum\_2E0) \quad (35)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty\_2Enum\_2Enum.(\forall V1n \in ty\_2Enum\_2Enum.( \\ & \forall V2p \in ty\_2Enum\_2Enum.((ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0m) \\ & (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V1n)\ V2p)) = (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\ & (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0m)\ V1n))\ V2p)))))) \end{aligned} \quad (36)$$

Assume the following.

$$(\forall V0n \in ty\_2Enum\_2Enum.(p\ (ap\ (ap\ c\_2Earithmetic\_2E\_23C\_23D\ c\_2Enum\_2E0)\ V0n))) \quad (37)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty\_2Enum\_2Enum.((ap\ (ap\ c\_2Earithmetic\_2E\_2D\ ( \\ & ap\ c\_2Enum\_2ESUC\ V0m))\ (ap\ c\_2Earithmetic\_2ENUMERAL\ (ap\ c\_2Earithmetic\_2EBIT1 \\ & c\_2Earithmetic\_2EZERO)))) = V0m)) \end{aligned} \quad (38)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty\_2Enum\_2Enum.((ap\ c\_2Eprim\_2rec\_2EPRE\ V0m) = \\ & (ap\ (ap\ c\_2Earithmetic\_2E\_2D\ V0m)\ (ap\ c\_2Earithmetic\_2ENUMERAL \\ & (ap\ c\_2Earithmetic\_2EBIT1\ c\_2Earithmetic\_2EZERO)))))) \end{aligned} \quad (39)$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty\_2Enum\_2Enum. (\forall V1n \in ty\_2Enum\_2Enum. ( \\
& ((ap (ap c\_2Earithmetic\_2E\_2A c\_2Enum\_2E0) V0m) = c\_2Enum\_2E0) \wedge \\
& (((ap (ap c\_2Earithmetic\_2E\_2A V0m) c\_2Enum\_2E0) = c\_2Enum\_2E0) \wedge \\
& (((ap (ap c\_2Earithmetic\_2E\_2A (ap c\_2Earithmetic\_2ENUMERAL \\
& (ap c\_2Earithmetic\_2EBIT1 c\_2Earithmetic\_2EZERO))) V0m) = V0m) \wedge \\
& (((ap (ap c\_2Earithmetic\_2E\_2A V0m) (ap c\_2Earithmetic\_2ENUMERAL \\
& (ap c\_2Earithmetic\_2EBIT1 c\_2Earithmetic\_2EZERO))) = V0m) \wedge ( \\
& ((ap (ap c\_2Earithmetic\_2E\_2A (ap c\_2Enum\_2ESUC V0m)) V1n) = (ap \\
& (ap c\_2Earithmetic\_2E\_2B (ap (ap c\_2Earithmetic\_2E\_2A V0m) V1n)) \\
& V1n)) \wedge ((ap (ap c\_2Earithmetic\_2E\_2A V0m) (ap c\_2Enum\_2ESUC V1n)) = \\
& (ap (ap c\_2Earithmetic\_2E\_2B V0m) (ap (ap c\_2Earithmetic\_2E\_2A \\
& V0m) V1n))))))))))
\end{aligned} \tag{40}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty\_2Enum\_2Enum. (\forall V1n \in ty\_2Enum\_2Enum. ( \\
& \forall V2p \in ty\_2Enum\_2Enum. (((p (ap (ap c\_2Earithmetic\_2E\_3C\_3D \\
& V0m) V1n)) \wedge (p (ap (ap c\_2Earithmetic\_2E\_3C\_3D V1n) V2p))) \Rightarrow (p ( \\
& ap (ap c\_2Earithmetic\_2E\_3C\_3D V0m) V2p))))))
\end{aligned} \tag{41}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty\_2Enum\_2Enum. (\forall V1n \in ty\_2Enum\_2Enum. ( \\
& \forall V2p \in ty\_2Enum\_2Enum. ((p (ap (ap c\_2Earithmetic\_2E\_3C\_3D \\
& (ap (ap c\_2Earithmetic\_2E\_2B V0m) V1n)) (ap (ap c\_2Earithmetic\_2E\_2B \\
& V0m) V2p))) \Leftrightarrow (p (ap (ap c\_2Earithmetic\_2E\_3C\_3D V1n) V2p))))))
\end{aligned} \tag{42}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty\_2Enum\_2Enum. (\forall V1n \in ty\_2Enum\_2Enum. ( \\
& (\neg (p (ap (ap c\_2Earithmetic\_2E\_3C\_3D V0m) V1n))) \Leftrightarrow (p (ap (ap c\_2Earithmetic\_2E\_3C\_3D \\
& (ap c\_2Enum\_2ESUC V1n)) V0m))))))
\end{aligned} \tag{43}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty\_2Enum\_2Enum. ((ap c\_2Enum\_2ESUC V0n) = (ap (ap \\
& c\_2Earithmetic\_2E\_2B (ap c\_2Earithmetic\_2ENUMERAL (ap c\_2Earithmetic\_2EBIT1 \\
& c\_2Earithmetic\_2EZERO))) V0n)))
\end{aligned} \tag{44}$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0f \in ((A\_27a^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}). \\
& \quad (\forall V1g \in (A\_27a^{ty\_2Enum\_2Enum}). (\forall V2n \in ty\_2Enum\_2Enum. \\
& \quad ((ap\ V1g\ (ap\ c\_2Enum\_2ESUC\ V2n)) = (ap\ (ap\ V0f\ V2n)\ (ap\ c\_2Enum\_2ESUC \\
& \quad V2n)))) \Leftrightarrow ((\forall V3n \in ty\_2Enum\_2Enum. ((ap\ V1g\ (ap\ c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap\ c\_2Earithmetic\_2EBIT1\ V3n))) = (ap\ (ap\ V0f\ (ap\ (ap\ c\_2Earithmetic\_2E\_2D \\
& \quad (ap\ c\_2Earithmetic\_2ENUMERAL\ (ap\ c\_2Earithmetic\_2EBIT1\ V3n))) \\
& \quad (ap\ c\_2Earithmetic\_2ENUMERAL\ (ap\ c\_2Earithmetic\_2EBIT1\ c\_2Earithmetic\_2EZERO)))))) \\
& \quad (ap\ c\_2Earithmetic\_2ENUMERAL\ (ap\ c\_2Earithmetic\_2EBIT1\ V3n)))))) \wedge \\
& \quad (\forall V4n \in ty\_2Enum\_2Enum. ((ap\ V1g\ (ap\ c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap\ c\_2Earithmetic\_2EBIT2\ V4n))) = (ap\ (ap\ V0f\ (ap\ c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap\ c\_2Earithmetic\_2EBIT1\ V4n)))\ (ap\ c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap\ c\_2Earithmetic\_2EBIT2\ V4n))))))))))
\end{aligned} \tag{45}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27t}.nonempty\ A_{.27t} \Rightarrow \forall A_{.27u}.nonempty\ A_{.27u} \Rightarrow \forall A_{.27w}. \\
& \quad nonempty\ A_{.27w} \Rightarrow \forall A_{.27x}.nonempty\ A_{.27x} \Rightarrow ((\forall V0f0 \in \\
& \quad ((ty\_2EfcP\_2Ecart\ 2\ A_{.27x})^{(ty\_2EfcP\_2Ecart\ 2\ A_{.27w})}).(\forall V1f \in \\
& \quad (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Sign \\
& \quad A_{.27t}\ A_{.27x})\ (ap\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Exponent\_fupd \\
& \quad A_{.27t}\ A_{.27w}\ A_{.27x})\ V0f0)\ V1f)) = (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Sign \\
& \quad A_{.27t}\ A_{.27w})\ V1f)))) \wedge ((\forall V2f0 \in ((ty\_2EfcP\_2Ecart\ 2\ A_{.27u})^{(ty\_2EfcP\_2Ecart\ 2\ A_{.27t})}). \\
& \quad (\forall V3f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ ( \\
& \quad c\_2EbinaRy\_ieee\_2Efloat\_Sign\ A_{.27u}\ A_{.27w})\ (ap\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A_{.27t}\ A_{.27u}\ A_{.27w})\ V2f0)\ V3f)) = (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Sign \\
& \quad A_{.27t}\ A_{.27w})\ V3f)))) \wedge ((\forall V4f0 \in ((ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)^{(ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)}. \\
& \quad (\forall V5f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ ( \\
& \quad c\_2EbinaRy\_ieee\_2Efloat\_Exponent\ A_{.27t}\ A_{.27w})\ (ap\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Sign\_fupd \\
& \quad A_{.27t}\ A_{.27w})\ V4f0)\ V5f)) = (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Exponent \\
& \quad A_{.27t}\ A_{.27w})\ V5f)))) \wedge ((\forall V6f0 \in ((ty\_2EfcP\_2Ecart\ 2\ A_{.27u})^{(ty\_2EfcP\_2Ecart\ 2\ A_{.27t})}). \\
& \quad (\forall V7f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ ( \\
& \quad c\_2EbinaRy\_ieee\_2Efloat\_Exponent\ A_{.27u}\ A_{.27w})\ (ap\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A_{.27t}\ A_{.27u}\ A_{.27w})\ V6f0)\ V7f)) = (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Exponent \\
& \quad A_{.27t}\ A_{.27w})\ V7f)))) \wedge ((\forall V8f0 \in ((ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)^{(ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)}. \\
& \quad (\forall V9f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ ( \\
& \quad c\_2EbinaRy\_ieee\_2Efloat\_Significand\ A_{.27t}\ A_{.27w})\ (ap\ (ap\ ( \\
& \quad c\_2EbinaRy\_ieee\_2Efloat\_Sign\_fupd\ A_{.27t}\ A_{.27w})\ V8f0)\ V9f)) = \\
& \quad (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Significand\ A_{.27t}\ A_{.27w})\ V9f)))) \wedge \\
& \quad ((\forall V10f0 \in ((ty\_2EfcP\_2Ecart\ 2\ A_{.27x})^{(ty\_2EfcP\_2Ecart\ 2\ A_{.27w})}). \\
& \quad (\forall V11f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ \\
& \quad (c\_2EbinaRy\_ieee\_2Efloat\_Significand\ A_{.27t}\ A_{.27x})\ (ap\ (ap \\
& \quad (c\_2EbinaRy\_ieee\_2Efloat\_Exponent\_fupd\ A_{.27t}\ A_{.27w}\ A_{.27x}) \\
& \quad V10f0)\ V11f)) = (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Significand\ A_{.27t} \\
& \quad A_{.27w})\ V11f)))) \wedge ((\forall V12f0 \in ((ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)^{(ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)}. \\
& \quad (\forall V13f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ \\
& \quad (c\_2EbinaRy\_ieee\_2Efloat\_Sign\ A_{.27t}\ A_{.27w})\ (ap\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Sign\_fupd \\
& \quad A_{.27t}\ A_{.27w})\ V12f0)\ V13f)) = (ap\ V12f0\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Sign \\
& \quad A_{.27t}\ A_{.27w})\ V13f)))) \wedge ((\forall V14f0 \in ((ty\_2EfcP\_2Ecart\ 2 \\
& \quad A_{.27x})^{(ty\_2EfcP\_2Ecart\ 2\ A_{.27w})}).(\forall V15f \in (ty\_2EbinaRy\_ieee\_2Efloat \\
& \quad A_{.27t}\ A_{.27w}).((ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Exponent\ A_{.27t} \\
& \quad A_{.27x})\ (ap\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Exponent\_fupd\ A_{.27t} \\
& \quad A_{.27w}\ A_{.27x})\ V14f0)\ V15f)) = (ap\ V14f0\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Exponent \\
& \quad A_{.27t}\ A_{.27w})\ V15f)))) \wedge ((\forall V16f0 \in ((ty\_2EfcP\_2Ecart\ 2\ A_{.27u})^{(ty\_2EfcP\_2Ecart\ 2\ A_{.27t})}). \\
& \quad (\forall V17f \in (ty\_2EbinaRy\_ieee\_2Efloat\ A_{.27t}\ A_{.27w}).((ap\ \\
& \quad (c\_2EbinaRy\_ieee\_2Efloat\_Significand\ A_{.27u}\ A_{.27w})\ (ap\ (ap \\
& \quad (c\_2EbinaRy\_ieee\_2Efloat\_Significand\_fupd\ A_{.27t}\ A_{.27u}\ A_{.27w}) \\
& \quad V16f0)\ V17f)) = (ap\ V16f0\ (ap\ (c\_2EbinaRy\_ieee\_2Efloat\_Significand \\
& \quad A_{.27t}\ A_{.27w})\ V17f))))))))))
\end{aligned} \tag{46}$$

Assume the following.

$$\begin{aligned}
& \forall A.27t.nonempty\ A.27t \Rightarrow \forall A.27u.nonempty\ A.27u \Rightarrow \forall A.27v. \\
& nonempty\ A.27v \Rightarrow \forall A.27w.nonempty\ A.27w \Rightarrow \forall A.27x.nonempty \\
& A.27x \Rightarrow \forall A.27y.nonempty\ A.27y \Rightarrow ((\forall V0g \in ((ty\_2Efc\_2Ecart \\
& \quad 2\ ty\_2Eone\_2Eone)^{(ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)}), (\forall V1f0 \in \\
& ((ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)^{(ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)}), \\
& \quad (\forall V2f \in (ty\_2Ebinary\_ieee\_2Efloat\ A.27t\ A.27w)).((ap\ ( \\
& \quad ap\ (c.2Ebinary\_ieee\_2Efloat\_Sign\_fupd\ A.27t\ A.27w)\ V1f0) \\
& \quad (ap\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_Sign\_fupd\ A.27t\ A.27w)\ V0g) \\
& \quad V2f))) = (ap\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_Sign\_fupd\ A.27t\ A.27w) \\
& \quad (ap\ (ap\ (c.2Ecombin\_2Eo\ (ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)\ ( \\
& \quad ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)\ (ty\_2Efc\_2Ecart\ 2\ ty\_2Eone\_2Eone)) \\
& \quad V1f0)\ V0g))\ V2f)))) \wedge ((\forall V3g \in ((ty\_2Efc\_2Ecart\ 2\ A.27x)^{(ty\_2Efc\_2Ecart\ 2\ A.27w)}), \\
& \quad (\forall V4f0 \in ((ty\_2Efc\_2Ecart\ 2\ A.27y)^{(ty\_2Efc\_2Ecart\ 2\ A.27x)}), \\
& \quad (\forall V5f \in (ty\_2Ebinary\_ieee\_2Efloat\ A.27t\ A.27w)).((ap\ ( \\
& \quad ap\ (c.2Ebinary\_ieee\_2Efloat\_Exponent\_fupd\ A.27t\ A.27x\ A.27y) \\
& \quad V4f0)\ (ap\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_Exponent\_fupd\ A.27t \\
& \quad A.27w\ A.27x)\ V3g)\ V5f))) = (ap\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_Exponent\_fupd \\
& \quad A.27t\ A.27w\ A.27y)\ (ap\ (ap\ (c.2Ecombin\_2Eo\ (ty\_2Efc\_2Ecart\ 2 \\
& \quad A.27w)\ (ty\_2Efc\_2Ecart\ 2\ A.27y)\ (ty\_2Efc\_2Ecart\ 2\ A.27x)) \\
& \quad V4f0)\ V3g))\ V5f)))) \wedge ((\forall V6g \in ((ty\_2Efc\_2Ecart\ 2\ A.27u)^{(ty\_2Efc\_2Ecart\ 2\ A.27t)}), \\
& \quad (\forall V7f0 \in ((ty\_2Efc\_2Ecart\ 2\ A.27v)^{(ty\_2Efc\_2Ecart\ 2\ A.27u)}), \\
& \quad (\forall V8f \in (ty\_2Ebinary\_ieee\_2Efloat\ A.27t\ A.27w)).((ap\ ( \\
& \quad ap\ (c.2Ebinary\_ieee\_2Efloat\_Significand\_fupd\ A.27u\ A.27v \\
& \quad A.27w)\ V7f0)\ (ap\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A.27t\ A.27u\ A.27w)\ V6g)\ V8f))) = (ap\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A.27t\ A.27v\ A.27w)\ (ap\ (ap\ (c.2Ecombin\_2Eo\ (ty\_2Efc\_2Ecart\ 2 \\
& \quad A.27t)\ (ty\_2Efc\_2Ecart\ 2\ A.27v)\ (ty\_2Efc\_2Ecart\ 2\ A.27u)) \\
& \quad V7f0)\ V6g))\ V8f))))))
\end{aligned}
\tag{47}$$

Assume the following.

$$\begin{aligned}
& \forall A.27t.nonempty A.27t \Rightarrow \forall A.27u.nonempty A.27u \Rightarrow \forall A.27w. \\
& \quad nonempty A.27w \Rightarrow \forall A.27x.nonempty A.27x \Rightarrow (\forall V0c11 \in \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone).(\forall V1c01 \in (ty\_2EfcP\_2Ecart \\
& \quad 2\ A.27x).(\forall V2c1 \in (ty\_2EfcP\_2Ecart\ 2\ A.27u).(\forall V3c12 \in \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone).(\forall V4c02 \in (ty\_2EfcP\_2Ecart \\
& \quad 2\ A.27x).(\forall V5c2 \in (ty\_2EfcP\_2Ecart\ 2\ A.27u).(((ap\ (ap \\
& \quad (c\_2Ebinary\_ieee\_2Efloat\_Sign\_fupd\ A.27u\ A.27x)\ (ap\ (c\_2Ecombin\_2EK \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)\ (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)) \\
& \quad V0c11))\ (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd\ A.27u \\
& \quad A.27w\ A.27x)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ A.27x)\ (ty\_2EfcP\_2Ecart \\
& \quad 2\ A.27w))\ V1c01))\ (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A.27t\ A.27u\ A.27w)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ A.27u) \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ A.27t))\ V2c1))\ (c\_2Ebool\_2EARB\ (ty\_2Ebinary\_ieee\_2Efloat \\
& \quad A.27t\ A.27w)))))) = (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Sign\_fupd \\
& \quad A.27u\ A.27x)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone) \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone))\ V3c12))\ (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd \\
& \quad A.27u\ A.27w\ A.27x)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ A.27x) \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ A.27w))\ V4c02))\ (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A.27t\ A.27u\ A.27w)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ A.27u) \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ A.27t))\ V5c2))\ (c\_2Ebool\_2EARB\ (ty\_2Ebinary\_ieee\_2Efloat \\
& \quad A.27t\ A.27w)))))) \Leftrightarrow ((V0c11 = V3c12) \wedge ((V1c01 = V4c02) \wedge (V2c1 = V5c2))))))))) \\
& \hspace{15em} (48)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A.27t.nonempty A.27t \Rightarrow \forall A.27w.nonempty A.27w \Rightarrow ( \\
& \quad (ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity\ A.27t\ A.27w) \\
& \quad (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A.27t\ A.27w))) = (ap \\
& \quad (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Sign\_fupd\ A.27t\ A.27w)\ (ap\ ( \\
& \quad c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ ty\_2Eone\_2Eone)\ (ty\_2EfcP\_2Ecart \\
& \quad 2\ ty\_2Eone\_2Eone))\ (ap\ (c\_2Ewords\_2En2w\ ty\_2Eone\_2Eone)\ c\_2Enum\_2E0))) \\
& \quad (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd\ A.27t\ A.27w \\
& \quad A.27w)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ A.27w)\ (ty\_2EfcP\_2Ecart \\
& \quad 2\ A.27w))\ (c\_2Ewords\_2Eword\_T\ A.27w)))\ (ap\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_Significand\_fupd \\
& \quad A.27t\ A.27t\ A.27w)\ (ap\ (c\_2Ecombin\_2EK\ (ty\_2EfcP\_2Ecart\ 2\ A.27t) \\
& \quad (ty\_2EfcP\_2Ecart\ 2\ A.27t))\ (ap\ (c\_2Ewords\_2En2w\ A.27t)\ c\_2Enum\_2E0))) \\
& \quad (c\_2Ebool\_2EARB\ (ty\_2Ebinary\_ieee\_2Efloat\ A.27t\ A.27w)))))) \\
& \hspace{15em} (49)
\end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow ( \\ & \quad (ap\ (c\_2Ebinary\_ieee\_2Efloat\_minus\_infinity\ A\_27t\ A\_27w) \\ & \quad (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t\ A\_27w))) = (ap \\ & \quad (c\_2Ebinary\_ieee\_2Efloat\_negate\ A\_27t\ A\_27w)\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity \\ & \quad A\_27t\ A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t \\ & \quad A\_27w)))))) \end{aligned} \tag{50}$$

Assume the following.

$$True \tag{51}$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A\_27a.(p\ V0t) \Leftrightarrow (p\ V0t))) \tag{52}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \tag{53}$$

Assume the following.

$$\begin{aligned} & ((\forall V0t \in 2.((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge \\ & ((\neg False) \Leftrightarrow True))) \end{aligned} \tag{54}$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow True)) \tag{55}$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.(\forall V1y \in A\_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \tag{56}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow (\neg(p\ V0t))) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow (\neg \\ & p\ V0t)))))) \end{aligned} \tag{57}$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0t1 \in A\_27a.(\forall V1t2 \in \\ & A\_27a.(((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ c\_2Ebool\_2ET)\ V0t1) \\ & V1t2) = V0t1) \wedge ((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ c\_2Ebool\_2EF) \\ & V0t1)\ V1t2) = V1t2)))) \end{aligned} \tag{58}$$

Assume the following.

$$(\forall V0t \in 2.(((p V0t) \Rightarrow False) \Leftrightarrow ((p V0t) \Leftrightarrow False))) \quad (59)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (60)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty \ A\_27a \Rightarrow (\forall V0P \in 2.(\forall V1Q \in 2. \\ & (\forall V2x \in A\_27a.(\forall V3x\_27 \in A\_27a.(\forall V4y \in A\_27a. \\ & (\forall V5y\_27 \in A\_27a.(((p V0P) \Leftrightarrow (p V1Q)) \wedge ((p V1Q) \Rightarrow (V2x = V3x\_27)) \wedge \\ & ((\neg(p V1Q)) \Rightarrow (V4y = V5y\_27)))))) \Rightarrow ((ap (ap (ap (c\_2Ebool\_2ECOND A\_27a) \\ & V0P) V2x) V4y) = (ap (ap (ap (c\_2Ebool\_2ECOND A\_27a) V1Q) V3x\_27) \\ & V5y\_27))))))))) \end{aligned} \quad (61)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty \ A\_27a \Rightarrow \forall A\_27b.nonempty \ A\_27b \Rightarrow ( \\ & \forall V0x \in A\_27a.(\forall V1y \in A\_27b.((ap (ap (c\_2Ecombin\_2EK \\ & A\_27a \ A\_27b) V0x) V1y) = V0x))) \end{aligned} \quad (62)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty \ A\_27a \Rightarrow \forall A\_27b.nonempty \ A\_27b \Rightarrow \forall A\_27c. \\ & nonempty \ A\_27c \Rightarrow \forall A\_27d.nonempty \ A\_27d \Rightarrow \forall A\_27e.nonempty \\ & A\_27e \Rightarrow \forall A\_27f.nonempty \ A\_27f \Rightarrow ((\forall V0f \in (A\_27b^{A\_27a}). \\ & (\forall V1v \in A\_27c.((ap (ap (c\_2Ecombin\_2Eo A\_27a \ A\_27c \ A\_27b) \\ & (ap (c\_2Ecombin\_2EK A\_27c \ A\_27b) V1v)) V0f) = (ap (c\_2Ecombin\_2EK \\ & A\_27c \ A\_27a) V1v)))) \wedge (\forall V2f \in (A\_27e^{A\_27d}).(\forall V3v \in \\ & A\_27d.((ap (ap (c\_2Ecombin\_2Eo A\_27f \ A\_27e \ A\_27d) V2f) (ap (c\_2Ecombin\_2EK \\ & A\_27d \ A\_27f) V3v)) = (ap (c\_2Ecombin\_2EK A\_27e \ A\_27f) (ap V2f V3v)))))) \end{aligned} \quad (63)$$

Assume the following.

$$\begin{aligned}
& ((\forall V0n \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2E\_2B \\
& \quad c\_2Enum\_2E0) V0n) = V0n)) \wedge ((\forall V1n \in ty\_2Enum\_2Enum.((ap \\
& \quad (ap c\_2Earithmetic\_2E\_2B V1n) c\_2Enum\_2E0) = V1n)) \wedge ((\forall V2n \in \\
& \quad ty\_2Enum\_2Enum.(\forall V3m \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2E\_2B \\
& \quad (ap c\_2Earithmetic\_2ENUMERAL V2n)) (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V3m)) = (ap c\_2Earithmetic\_2ENUMERAL (ap c\_2Enumeral\_2EiZ (ap \\
& \quad (ap c\_2Earithmetic\_2E\_2B V2n) V3m)))))) \wedge ((\forall V4n \in ty\_2Enum\_2Enum. \\
& \quad ((ap (ap c\_2Earithmetic\_2E\_2A c\_2Enum\_2E0) V4n) = c\_2Enum\_2E0)) \wedge \\
& \quad ((\forall V5n \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2E\_2A \\
& \quad V5n) c\_2Enum\_2E0) = c\_2Enum\_2E0)) \wedge ((\forall V6n \in ty\_2Enum\_2Enum. \\
& \quad (\forall V7m \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2E\_2A ( \\
& \quad ap c\_2Earithmetic\_2ENUMERAL V6n)) (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V7m)) = (ap c\_2Earithmetic\_2ENUMERAL (ap (ap c\_2Earithmetic\_2E\_2A \\
& \quad V6n) V7m)))))) \wedge ((\forall V8n \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2E\_2D \\
& \quad c\_2Enum\_2E0) V8n) = c\_2Enum\_2E0)) \wedge ((\forall V9n \in ty\_2Enum\_2Enum. \\
& \quad ((ap (ap c\_2Earithmetic\_2E\_2D V9n) c\_2Enum\_2E0) = V9n)) \wedge ((\forall V10n \in \\
& \quad ty\_2Enum\_2Enum.(\forall V11m \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2E\_2D \\
& \quad (ap c\_2Earithmetic\_2ENUMERAL V10n)) (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V11m)) = (ap c\_2Earithmetic\_2ENUMERAL (ap (ap c\_2Earithmetic\_2E\_2D \\
& \quad V10n) V11m)))))) \wedge ((\forall V12n \in ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2EEXP \\
& \quad c\_2Enum\_2E0) (ap c\_2Earithmetic\_2ENUMERAL (ap c\_2Earithmetic\_2EBIT1 \\
& \quad V12n))) = c\_2Enum\_2E0)) \wedge ((\forall V13n \in ty\_2Enum\_2Enum.((ap \\
& \quad (ap c\_2Earithmetic\_2EEXP c\_2Enum\_2E0) (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap c\_2Earithmetic\_2EBIT2 V13n))) = c\_2Enum\_2E0)) \wedge ((\forall V14n \in \\
& \quad ty\_2Enum\_2Enum.((ap (ap c\_2Earithmetic\_2EEXP V14n) c\_2Enum\_2E0) = \\
& \quad (ap c\_2Earithmetic\_2ENUMERAL (ap c\_2Earithmetic\_2EBIT1 c\_2Earithmetic\_2EZERO)))))) \wedge \\
& \quad ((\forall V15n \in ty\_2Enum\_2Enum.(\forall V16m \in ty\_2Enum\_2Enum. \\
& \quad ((ap (ap c\_2Earithmetic\_2EEXP (ap c\_2Earithmetic\_2ENUMERAL V15n)) \\
& \quad (ap c\_2Earithmetic\_2ENUMERAL V16m)) = (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap (ap c\_2Earithmetic\_2EEXP V15n) V16m)))))) \wedge ((ap c\_2Enum\_2ESUC \\
& \quad c\_2Enum\_2E0) = (ap c\_2Earithmetic\_2ENUMERAL (ap c\_2Earithmetic\_2EBIT1 \\
& \quad c\_2Earithmetic\_2EZERO))) \wedge ((\forall V17n \in ty\_2Enum\_2Enum. ( \\
& \quad (ap c\_2Enum\_2ESUC (ap c\_2Earithmetic\_2ENUMERAL V17n)) = (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap c\_2Enum\_2ESUC V17n)))))) \wedge ((ap c\_2Eprim\_rec\_2EPRE c\_2Enum\_2E0) = \\
& \quad c\_2Enum\_2E0) \wedge ((\forall V18n \in ty\_2Enum\_2Enum.((ap c\_2Eprim\_rec\_2EPRE \\
& \quad (ap c\_2Earithmetic\_2ENUMERAL V18n)) = (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad (ap c\_2Eprim\_rec\_2EPRE V18n)))))) \wedge ((\forall V19n \in ty\_2Enum\_2Enum. \\
& \quad (((ap c\_2Earithmetic\_2ENUMERAL V19n) = c\_2Enum\_2E0) \Leftrightarrow (V19n = c\_2Earithmetic\_2EZERO))) \wedge \\
& \quad ((\forall V20n \in ty\_2Enum\_2Enum.((c\_2Enum\_2E0 = (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V20n)) \Leftrightarrow (V20n = c\_2Earithmetic\_2EZERO))) \wedge ((\forall V21n \in ty\_2Enum\_2Enum. \\
& \quad (\forall V22m \in ty\_2Enum\_2Enum.(((ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V21n) = (ap c\_2Earithmetic\_2ENUMERAL V22m)) \Leftrightarrow (V21n = V22m)))))) \wedge \\
& \quad ((\forall V23n \in ty\_2Enum\_2Enum.((p (ap (ap c\_2Eprim\_rec\_2E\_3C \\
& \quad V23n) c\_2Enum\_2E0)) \Leftrightarrow False)) \wedge ((\forall V24n \in ty\_2Enum\_2Enum. \\
& \quad ((p (ap (ap c\_2Eprim\_rec\_2E\_3C c\_2Enum\_2E0) (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V24n))) \Leftrightarrow (p (ap (ap c\_2Eprim\_rec\_2E\_3C c\_2Earithmetic\_2EZERO) \\
& \quad V24n)))))) \wedge ((\forall V25n \in ty\_2Enum\_2Enum.(\forall V26m \in ty\_2Enum\_2Enum. \\
& \quad ((p (ap (ap c\_2Eprim\_rec\_2E\_3C (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V25n)) (ap c\_2Earithmetic\_2ENUMERAL V26m))) \Leftrightarrow (p (ap (ap c\_2Eprim\_rec\_2E\_3C \\
& \quad V25n) V26m)))))) \wedge ((\forall V27n \in ty\_2Enum\_2Enum.((p (ap (ap c\_2Earithmetic\_2E\_3E \\
& \quad c\_2Enum\_2E0) V27n)) \Leftrightarrow False)) \wedge ((\forall V28n \in ty\_2Enum\_2Enum. \\
& \quad ((p (ap (ap c\_2Earithmetic\_2E\_3E (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V28n)) c\_2Enum\_2E0)) \Leftrightarrow (p (ap (ap c\_2Eprim\_rec\_2E\_3C c\_2Earithmetic\_2EZERO) \\
& \quad V28n)))))) \wedge ((\forall V29n \in ty\_2Enum\_2Enum.(\forall V30m \in ty\_2Enum\_2Enum. \\
& \quad ((p (ap (ap c\_2Earithmetic\_2E\_3E (ap c\_2Earithmetic\_2ENUMERAL \\
& \quad V29n)) (ap c\_2Earithmetic\_2ENUMERAL V30m))) \Leftrightarrow (p (ap (ap c\_2Eprim\_rec\_2E\_3C \\
& \quad V30m) V29n)))))) \wedge ((\forall V31n \in ty\_2Enum\_2Enum.((p (ap (ap c\_2Earithmetic\_2E\_3C\_3D \\
& \quad c\_2Enum\_2E0) V31n)) \Leftrightarrow True)) \wedge ((\forall V32n \in ty\_2Enum\_2Enum. \\
& \quad ((p (ap (ap c\_2Earithmetic\_2E\_3C\_3D (ap c\_2Earithmetic\_2ENUMERAL
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty\_2Enum\_2Enum. (\forall V1m \in ty\_2Enum\_2Enum. ( \\
& ((ap\ c\_2Enumeral\_2EiZ\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ c\_2Earithmetic\_2EZERO) \\
& V0n)) = V0n) \wedge (((ap\ c\_2Enumeral\_2EiZ\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& V0n)\ c\_2Earithmetic\_2EZERO)) = V0n) \wedge (((ap\ c\_2Enumeral\_2EiZ\ ( \\
& ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT1\ V0n))\ ( \\
& ap\ c\_2Earithmetic\_2EBIT1\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT2\ ( \\
& ap\ c\_2Enumeral\_2EiZ\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge \\
& (((ap\ c\_2Enumeral\_2EiZ\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT1 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT2\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT1 \\
& (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge ( \\
& ((ap\ c\_2Enumeral\_2EiZ\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT2 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT1\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT1 \\
& (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge ( \\
& ((ap\ c\_2Enumeral\_2EiZ\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT2 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT2\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT2 \\
& (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge ( \\
& ((ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ c\_2Earithmetic\_2EZERO) \\
& V0n)) = (ap\ c\_2Enum\_2ESUC\ V0n)) \wedge (((ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& V0n)\ c\_2Earithmetic\_2EZERO)) = (ap\ c\_2Enum\_2ESUC\ V0n)) \wedge (((ap \\
& c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT1 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT1\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT1 \\
& (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge ( \\
& ((ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT1 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT2\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT2 \\
& (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge ( \\
& ((ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT2 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT1\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT2 \\
& (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge ( \\
& ((ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT2 \\
& V0n))\ (ap\ c\_2Earithmetic\_2EBIT2\ V1m))) = (ap\ c\_2Earithmetic\_2EBIT1 \\
& (ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ V1m)))) \wedge \\
& (((ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ c\_2Earithmetic\_2EZERO) \\
& V0n)) = (ap\ c\_2Enumeral\_2EiiSUC\ V0n)) \wedge (((ap\ c\_2Enumeral\_2EiiSUC \\
& (ap\ (ap\ c\_2Earithmetic\_2E\_2B\ V0n)\ c\_2Earithmetic\_2EZERO)) = ( \\
& ap\ c\_2Enumeral\_2EiiSUC\ V0n)) \wedge (((ap\ c\_2Enumeral\_2EiiSUC\ (ap\ ( \\
& ap\ c\_2Earithmetic\_2E\_2B\ (ap\ c\_2Earithmetic\_2EBIT1\ V0n))\ (ap\ c\_2Earithmetic\_2EBIT1 \\
& V1m))) = (ap\ c\_2Earithmetic\_2EBIT2\ (ap\ c\_2Enum\_2ESUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& V0n)\ V1m)))) \wedge (((ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& (ap\ c\_2Earithmetic\_2EBIT1\ V0n))\ (ap\ c\_2Earithmetic\_2EBIT2\ V1m))) = \\
& (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& V0n)\ V1m)))) \wedge (((ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& (ap\ c\_2Earithmetic\_2EBIT2\ V0n))\ (ap\ c\_2Earithmetic\_2EBIT1\ V1m))) = \\
& (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& V0n)\ V1m)))) \wedge (((ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& (ap\ c\_2Earithmetic\_2EBIT2\ V0n))\ (ap\ c\_2Earithmetic\_2EBIT2\ V1m))) = \\
& (ap\ c\_2Earithmetic\_2EBIT2\ (ap\ c\_2Enumeral\_2EiiSUC\ (ap\ (ap\ c\_2Earithmetic\_2E\_2B \\
& V0n)\ V1m))))))))))))))))))))))))))))))
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty\_2Enum\_2Enum. (\forall V1m \in ty\_2Enum\_2Enum. ( \\
& \quad ((p (ap (ap c\_2Earithmic\_2E\_3C\_3D c\_2Earithmic\_2EZERO) V0n)) \Leftrightarrow \\
& \quad True) \wedge (((p (ap (ap c\_2Earithmic\_2E\_3C\_3D (ap c\_2Earithmic\_2EBIT1 \\
& \quad V0n)) c\_2Earithmic\_2EZERO)) \Leftrightarrow False) \wedge (((p (ap (ap c\_2Earithmic\_2E\_3C\_3D \\
& \quad (ap c\_2Earithmic\_2EBIT2 V0n)) c\_2Earithmic\_2EZERO)) \Leftrightarrow False) \wedge \\
& \quad (((p (ap (ap c\_2Earithmic\_2E\_3C\_3D (ap c\_2Earithmic\_2EBIT1 \\
& \quad V0n)) (ap c\_2Earithmic\_2EBIT1 V1m))) \Leftrightarrow (p (ap (ap c\_2Earithmic\_2E\_3C\_3D \\
& \quad V0n) V1m))) \wedge (((p (ap (ap c\_2Earithmic\_2E\_3C\_3D (ap c\_2Earithmic\_2EBIT1 \\
& \quad V0n)) (ap c\_2Earithmic\_2EBIT2 V1m))) \Leftrightarrow (p (ap (ap c\_2Earithmic\_2E\_3C\_3D \\
& \quad V0n) V1m))) \wedge (((p (ap (ap c\_2Earithmic\_2E\_3C\_3D (ap c\_2Earithmic\_2EBIT2 \\
& \quad V0n)) (ap c\_2Earithmic\_2EBIT1 V1m))) \Leftrightarrow (\neg (p (ap (ap c\_2Earithmic\_2E\_3C\_3D \\
& \quad V1m) V0n)))) \wedge ((p (ap (ap c\_2Earithmic\_2E\_3C\_3D (ap c\_2Earithmic\_2EBIT2 \\
& \quad V0n)) (ap c\_2Earithmic\_2EBIT2 V1m))) \Leftrightarrow (p (ap (ap c\_2Earithmic\_2E\_3C\_3D \\
& \quad V0n) V1m))))))))))
\end{aligned} \tag{66}$$

Assume the following.

$$\begin{aligned}
& (((ap c\_2Eprim\_rec\_2EPRE c\_2Earithmic\_2EZERO) = c\_2Earithmic\_2EZERO) \wedge \\
& (((ap c\_2Eprim\_rec\_2EPRE (ap c\_2Earithmic\_2EBIT1 c\_2Earithmic\_2EZERO)) = \\
& \quad c\_2Earithmic\_2EZERO) \wedge ((\forall V0n \in ty\_2Enum\_2Enum. ((ap \\
& \quad c\_2Eprim\_rec\_2EPRE (ap c\_2Earithmic\_2EBIT1 (ap c\_2Earithmic\_2EBIT1 \\
& \quad V0n))) = (ap c\_2Earithmic\_2EBIT2 (ap c\_2Eprim\_rec\_2EPRE (ap \\
& \quad c\_2Earithmic\_2EBIT1 V0n)))))) \wedge ((\forall V1n \in ty\_2Enum\_2Enum. \\
& ((ap c\_2Eprim\_rec\_2EPRE (ap c\_2Earithmic\_2EBIT1 (ap c\_2Earithmic\_2EBIT2 \\
& \quad V1n))) = (ap c\_2Earithmic\_2EBIT2 (ap c\_2Earithmic\_2EBIT1 \\
& \quad V1n)))) \wedge ((\forall V2n \in ty\_2Enum\_2Enum. ((ap c\_2Eprim\_rec\_2EPRE \\
& (ap c\_2Earithmic\_2EBIT2 V2n)) = (ap c\_2Earithmic\_2EBIT1 V2n)))))))))
\end{aligned} \tag{67}$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty A\_27a \Rightarrow (\forall V0m \in ty\_2Enum\_2Enum. ( \\
& \quad \forall V1n \in ty\_2Enum\_2Enum. (((ap (c\_2Ewords\_2En2w A\_27a) V0m) = \\
& \quad (ap (c\_2Ewords\_2En2w A\_27a) V1n)) \Leftrightarrow ((ap (ap c\_2Earithmic\_2EMOD \\
& \quad V0m) (ap (c\_2Ewords\_2Edimword A\_27a) (c\_2Ebool\_2Ethe\_value \\
& \quad A\_27a))) = (ap (ap c\_2Earithmic\_2EMOD V1n) (ap (c\_2Ewords\_2Edimword \\
& \quad A\_27a) (c\_2Ebool\_2Ethe\_value A\_27a))))))
\end{aligned} \tag{68}$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty A\_27a \Rightarrow ((ap (c\_2Ewords\_2Eword\_2comp \\
& \quad A\_27a) (ap (c\_2Ewords\_2En2w A\_27a) (ap c\_2Earithmic\_2ENUMERAL \\
& \quad (ap c\_2Earithmic\_2EBIT1 c\_2Earithmic\_2EZERO)))) = (c\_2Ewords\_2Eword\_T \\
& \quad A\_27a))
\end{aligned} \tag{69}$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0w \in (ty.2EfcP.2Ecart \\ 2\ A.27a).((ap\ (c.2Ewords.2Eword\_1comp\ A.27a)\ V0w) = (ap\ (ap\ ( \\ c.2Ewords.2Eword\_sub\ A.27a)\ (ap\ (c.2Ewords.2Eword\_2comp\ A.27a) \\ V0w))\ (ap\ (c.2Ewords.2En2w\ A.27a)\ (ap\ c.2Earithmetic.2ENUMERAL \\ (ap\ c.2Earithmetic.2EBIT1\ c.2Earithmetic.2EZERO)))))) \end{aligned} \quad (70)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0w \in (ty.2EfcP.2Ecart \\ 2\ A.27a).((ap\ (c.2Ewords.2Eword\_2comp\ A.27a)\ (ap\ (c.2Ewords.2Eword\_2comp \\ A.27a)\ V0w)) = V0w)) \end{aligned} \quad (71)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow ((ap\ (c.2Ewords.2Eword\_1comp \\ A.27a)\ (ap\ (c.2Ewords.2En2w\ A.27a)\ c.2Enum.2E0)) = (c.2Ewords.2Eword\_T \\ A.27a)) \end{aligned} \quad (72)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow ( \\ (\forall V0m \in ty.2Enum.2Enum.(\forall V1n \in ty.2Enum.2Enum.( \\ (ap\ (ap\ (c.2Ewords.2Eword\_add\ A.27a)\ (ap\ (c.2Ewords.2Eword\_2comp \\ A.27a)\ (ap\ (c.2Ewords.2En2w\ A.27a)\ V0m)))\ (ap\ (c.2Ewords.2Eword\_2comp \\ A.27a)\ (ap\ (c.2Ewords.2En2w\ A.27a)\ V1n))) = (ap\ (c.2Ewords.2Eword\_2comp \\ A.27a)\ (ap\ (c.2Ewords.2En2w\ A.27a)\ (ap\ (ap\ c.2Earithmetic.2E.2B \\ V0m)\ V1n)))))) \wedge (\forall V2m \in ty.2Enum.2Enum.(\forall V3n \in ty.2Enum.2Enum. \\ ((ap\ (ap\ (c.2Ewords.2Eword\_add\ A.27b)\ (ap\ (c.2Ewords.2En2w\ A.27b) \\ V2m))\ (ap\ (c.2Ewords.2Eword\_2comp\ A.27b)\ (ap\ (c.2Ewords.2En2w \\ A.27b)\ V3n))) = (ap\ (ap\ (ap\ (c.2Ebool.2ECOND\ (ty.2EfcP.2Ecart\ 2 \\ A.27b))\ (ap\ (ap\ c.2Earithmetic.2E.3C.3D\ V3n)\ V2m))\ (ap\ (c.2Ewords.2En2w \\ A.27b)\ (ap\ (ap\ c.2Earithmetic.2E.2D\ V2m)\ V3n)))\ (ap\ (c.2Ewords.2Eword\_2comp \\ A.27b)\ (ap\ (c.2Ewords.2En2w\ A.27b)\ (ap\ (ap\ c.2Earithmetic.2E.2D \\ V3n)\ V2m)))))))))) \end{aligned} \quad (73)$$

**Theorem 1**

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow ( \\ & ((ap\ (c\_2Ebinary\_ieee\_2Efloat\_negate\ A\_27t\ A\_27w)\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity \\ & \quad A\_27t\ A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t \\ & \quad A\_27w)))) = (ap\ (c\_2Ebinary\_ieee\_2Efloat\_minus\_infinity \\ & \quad A\_27t\ A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t \\ & \quad A\_27w)))) \wedge (((ap\ (c\_2Ebinary\_ieee\_2Efloat\_negate\ A\_27t\ A\_27w) \\ & \quad (ap\ (c\_2Ebinary\_ieee\_2Efloat\_minus\_infinity\ A\_27t\ A\_27w) \\ & \quad (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t\ A\_27w)))) = ( \\ & \quad ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity\ A\_27t\ A\_27w)\ ( \\ & \quad c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t\ A\_27w)))) \wedge (( \\ & \quad (ap\ (c\_2Ebinary\_ieee\_2Efloat\_abs\ A\_27t\ A\_27w)\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity \\ & \quad A\_27t\ A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t \\ & \quad A\_27w)))) = (ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity\ A\_27t \\ & \quad A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t\ A\_27w)))) \wedge \\ & ((ap\ (c\_2Ebinary\_ieee\_2Efloat\_abs\ A\_27t\ A\_27w)\ (ap\ (c\_2Ebinary\_ieee\_2Efloat\_minus\_infinity \\ & \quad A\_27t\ A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t \\ & \quad A\_27w)))) = (ap\ (c\_2Ebinary\_ieee\_2Efloat\_plus\_infinity\ A\_27t \\ & \quad A\_27w)\ (c\_2Ebool\_2Ethe\_value\ (ty\_2Epair\_2Eprod\ A\_27t\ A\_27w)))))) \end{aligned}$$