

thm_2Ebitstring_2Elength_bitify (TMercVTLK- DARt3gWwZSQhRTDMoJmeaab6zT)

October 26, 2020

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{1}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{2}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \tag{3}$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \tag{4}$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \tag{5}$$

Definition 4 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 5 We define c_2Ebool_2E21 to be $\lambda A.\lambda a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c_2Emin_2E3D\ (2^{A-27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V1x \in 2.V1x))$

Definition 6 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num\ (ap\ (ap\ (c_2Emin_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Let $c_2Earithmetic_2E2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \tag{6}$$

Definition 7 We define $c_2Earithmic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmic_2E$

Definition 8 We define $c_2Earithmic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 9 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 10 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 11 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t)))$

Definition 12 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x))$ then (the $(\lambda x.x \in A \wedge P x)$ of type $\iota \Rightarrow \iota$).

Definition 13 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.(ap (ap c_2Ebool_2E_21 2) (\lambda V3t3 \in 2.V3t3))))$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty_2Elist_2Elist A0) \quad (7)$$

Let $c_2Ebitstring_2Ebitify : \iota$ be given. Assume the following.

$$c_2Ebitstring_2Ebitify \in (((ty_2Elist_2Elist ty_2Enum_2Enum)^{(ty_2Elist_2Elist 2)})^{(ty_2Elist_2Elist ty_2Enum_2Enum)}) \quad (8)$$

Let $c_2Elist_2EAPPEND : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Elist_2EAPPEND A_27a \in (((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)})^{(ty_2Elist_2Elist A_27a)}) \quad (9)$$

Let $c_2Elist_2EMAP : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Elist_2EMAP A_27a A_27b \in (((ty_2Elist_2Elist A_27b)^{(ty_2Elist_2Elist A_27a)})^{(A_27b^{A_27a})}) \quad (10)$$

Let $c_2Elist_2EREVERSE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Elist_2EREVERSE A_27a \in ((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)}) \quad (11)$$

Let $c_2Elist_2ELENGTH : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Elist_2ELENGTH A_27a \in (ty_2Enum_2Enum)^{(ty_2Elist_2Elist A_27a)} \quad (12)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(ap (ap c_2Earithmic_2E_2B V0m) V1n) = (ap (ap c_2Earithmic_2E_2B V1n) V0m)))) \quad (13)$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad \forall V2p \in ty_2Enum_2Enum. (((ap (ap c_2Earithmetic_2E_2B V0m) \\
& \quad V2p) = (ap (ap c_2Earithmetic_2E_2B V1n) V2p)) \Leftrightarrow (V0m = V1n)))))) \\
& \tag{14}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0v \in (ty_2Elist_2Elist 2). (\forall V1a \in (ty_2Elist_2Elist \\
& \quad ty_2Enum_2Enum). ((ap (ap c_2Ebitstring_2Ebitify V1a) V0v) = (\\
& \quad ap (ap (c_2Elist_2EAPPEND ty_2Enum_2Enum) (ap (c_2Elist_2EREVERSE \\
& \quad ty_2Enum_2Enum) (ap (ap (c_2Elist_2EMAP 2 ty_2Enum_2Enum) (\lambda V2b \in \\
& \quad 2. (ap (ap (ap (c_2Ebool_2ECOND ty_2Enum_2Enum) V2b) (ap c_2Earithmetic_2ENUMERAL \\
& \quad (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))) c_2Enum_2E0))) \\
& \quad V0v))) V1a)))))) \\
& \tag{15}
\end{aligned}$$

Assume the following.

$$True \tag{16}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \tag{17}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0l1 \in (ty_2Elist_2Elist \\
& \quad A_27a). (\forall V1l2 \in (ty_2Elist_2Elist A_27a). ((ap (c_2Elist_2ELENGTH \\
& \quad A_27a) (ap (ap (c_2Elist_2EAPPEND A_27a) V0l1) V1l2)) = (ap (ap c_2Earithmetic_2E_2B \\
& \quad (ap (c_2Elist_2ELENGTH A_27a) V0l1)) (ap (c_2Elist_2ELENGTH A_27a) \\
& \quad V1l2)))))) \\
& \tag{18}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow (\\
& \quad \forall V0l \in (ty_2Elist_2Elist A_27a). (\forall V1f \in (A_27b^{A_27a}). \\
& \quad ((ap (c_2Elist_2ELENGTH A_27b) (ap (ap (c_2Elist_2EMAP A_27a A_27b) \\
& \quad V1f) V0l)) = (ap (c_2Elist_2ELENGTH A_27a) V0l)))))) \\
& \tag{19}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0l \in (ty_2Elist_2Elist \\
& \quad A_27a). ((ap (c_2Elist_2ELENGTH A_27a) (ap (c_2Elist_2EREVERSE \\
& \quad A_27a) V0l)) = (ap (c_2Elist_2ELENGTH A_27a) V0l)))) \\
& \tag{20}
\end{aligned}$$

Theorem 1

$$\begin{aligned} & (\forall V0v \in (ty_2Elist_2Elist\ 2).(\forall V1l \in (ty_2Elist_2Elist \\ & ty_2Enum_2Enum).((ap (c_2Elist_2ELENGTH\ ty_2Enum_2Enum) (ap \\ & (ap\ c_2Ebitstring_2Ebitify\ V1l)\ V0v)) = (ap (ap\ c_2Earithmetic_2E_2B \\ & (ap (c_2Elist_2ELENGTH\ ty_2Enum_2Enum)\ V1l)) (ap (c_2Elist_2ELENGTH \\ & 2)\ V0v)))))) \end{aligned}$$