

thm_2Ebitstring_2Eops__to__v2w
(TMX5UcaYj6HiyxBSZvVqzmks1MBjY5nNL8X)

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Let $ty_2Esum_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Esum_2Esum\ A0\ A1) \quad (1)$$

Let $ty_2EfcP_2Efinite_image : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2EfcP_2Efinite_image\ A0) \quad (2)$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o\ (x = y)$ of type $\iota \Rightarrow \iota$.

Let $ty_2Ebool_2Eitself : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Ebool_2Eitself\ A0) \quad (3)$$

Let $c_2Ebool_2Ethe_value : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ebool_2Ethe_value\ A_27a \in (ty_2Ebool_2Eitself\ A_27a) \quad (4)$$

Let $ty_2Eenum_2Eenum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eenum_2Eenum \quad (5)$$

Let $c_2EfcP_2Edimindex : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2EfcP_2Edimindex\ A_27a \in (ty_2Eenum_2Eenum^{(ty_2Ebool_2Eitself\ A_27a)}) \quad (6)$$

Definition 2 We define c_2Ebool_2E2E to be $(ap\ (ap\ (c_2Emin_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 3 We define c_2Ebool_2E21 to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ (ap\ (c_2Emin_2E3D\ (2^{A_27a})))$

Definition 4 We define c_2Ebool_2EF to be $(ap\ (c_2Ebool_2E21\ 2)\ (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2E_7E))$

Definition 7 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2)))$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (7)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (8)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (9)$$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap c_2Enum_2EABS_num (ap V0m c_2Enum_2ESUC_REP))$

Definition 9 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\mathbf{if} (\exists x \in A.p (ap P x)) \mathbf{then} (the (\lambda x.x \in A \wedge p x))$ of type $\iota \Rightarrow \iota$.

Definition 10 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_40 A_27a) P)))$

Definition 11 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap V0m (ap V1n c_2Eprim_rec_2E_3C))$

Definition 12 We define $c_2Ebool_2E_3F_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap c_2Ebool_2E_2F_5C A_27a) P))$

Definition 13 We define $c_2Efcp_2Efinite_index$ to be $\lambda A_27a : \iota.(ap (c_2Emin_2E_40 (A_27a^{ty_2Enum_2Enum})) c_2Efinite_index)$

Let $ty_2Efcp_2Ecart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty_2Efcp_2Ecart A0 A1) \quad (10)$$

Let $c_2Efcp_2Edest_cart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Efcp_2Edest_cart A_27a A_27b \in ((A_27a^{(ty_2Efcp_2Efinite_image A_27b)})^{(ty_2Efcp_2Ecart A_27a A_27b)}) \quad (11)$$

Definition 14 We define $c_2Efcp_2Efcp_index$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in (ty_2Efcp_2Ecart A_27a A_27b).c_2Efcp_2Efcp_index A_27a A_27b V0x$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (12)$$

Definition 15 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 16 We define `c_2Earithmetic_2EZERO` to be `c_2Enum_2E0`.

Let `c_2Earithmetic_2E_2B` : ι be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (13)$$

Definition 17 We define `c_2Earithmetic_2EBIT2` to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2E_2B))$.

Definition 18 We define `c_2Earithmetic_2ENUMERAL` to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let `c_2Earithmetic_2EEXP` : ι be given. Assume the following.

$$c_2Earithmetic_2EEXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (14)$$

Definition 19 We define `c_2Ebool_2ECOND` to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.(ap (ap c_2Ebool_2ECOND))))$.

Definition 20 We define `c_2Ebit_2ESBIT` to be $\lambda V0b \in 2.\lambda V1n \in ty_2Enum_2Enum.(ap (ap (ap (c_2Ebit_2ESBIT))))$.

Let `c_2Esum_num_2ESUM` : ι be given. Assume the following.

$$c_2Esum_num_2ESUM \in ((ty_2Enum_2Enum^{(ty_2Enum_2Enum^{ty_2Enum_2Enum})})^{ty_2Enum_2Enum}) \quad (15)$$

Definition 21 We define `c_2Ewords_2Ew2n` to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2EfcP_2Ecart\ 2\ A_27a).(ap (ap c_2Ewords_2Ew2n))$.

Definition 22 We define `c_2Earithmetic_2EBIT1` to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2E_2B))$.

Let `c_2Earithmetic_2EDIV` : ι be given. Assume the following.

$$c_2Earithmetic_2EDIV \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (16)$$

Definition 23 We define `c_2Ebit_2EDIV_2EXP` to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (ap c_2Ebit_2EDIV_2EXP))$.

Let `c_2Earithmetic_2E_2D` : ι be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (17)$$

Let `c_2Earithmetic_2EMOD` : ι be given. Assume the following.

$$c_2Earithmetic_2EMOD \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (18)$$

Definition 24 We define `c_2Ebit_2EMOD_2EXP` to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (ap c_2Ebit_2EMOD_2EXP))$.

Definition 25 We define `c_2Ebit_2EBITS` to be $\lambda V0h \in ty_2Enum_2Enum.\lambda V1l \in ty_2Enum_2Enum.\lambda V2m \in ty_2Enum_2Enum.(ap (ap (ap c_2Ebit_2EBITS)))$.

Definition 26 We define `c_2Ebit_2EBIT` to be $\lambda V0b \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (ap c_2Ebit_2EBIT))$.

Definition 27 We define `c_2EfcP_2EFCP` to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0g \in (A_27a^{ty_2Enum_2Enum}).(ap (ap c_2EfcP_2EFCP)))$.

Definition 28 We define $c_2Ewords_2En2w$ to be $\lambda A_27a : \iota.\lambda V0n \in ty_2Enum_2Enum.(ap (c_2EfcP_2EFC$

Definition 29 We define $c_2Ewords_2Ew2w$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0w \in (ty_2EfcP_2Ecart\ 2\ A_27a$

Definition 30 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21\ 2) (\lambda V2t \in$

Definition 31 We define $c_2Earithmetic_2E_3C_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2$

Definition 32 We define $c_2Ewords_2Eword_lsl$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Definition 33 We define $c_2Ewords_2Eword_lor$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Definition 34 We define c_2Ebool_2ELET to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0f \in (A_27b^{A_27a}).(\lambda V1x \in A_27$

Definition 35 We define $c_2Ewords_2Eword_join$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a$

Definition 36 We define $c_2Ewords_2Eword_concat$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a$

Definition 37 We define $c_2Ewords_2Eword_xnor$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Definition 38 We define $c_2Ewords_2Eword_nand$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Definition 39 We define $c_2Ewords_2Eword_nor$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Definition 40 We define $c_2Ewords_2Eword_xor$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Definition 41 We define $c_2Ewords_2Eword_and$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a).\lambda V1$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Elist_2Elist\ A0) \quad (19)$$

Let $c_2Enumposrep_2En2l : \iota$ be given. Assume the following.

$$c_2Enumposrep_2En2l \in (((ty_2Elist_2Elist\ ty_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (20)$$

Definition 42 We define $c_2Enumposrep_2Enum_to_bin_list$ to be $(ap\ c_2Enumposrep_2En2l\ (ap\ c_2Earithmetic_2E_3C_3D$

Let $c_2Elist_2ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2ENIL\ A_27a \in (ty_2Elist_2Elist\ A_27a) \quad (21)$$

Let $c_2Ebitstring_2Eboolify : \iota$ be given. Assume the following.

$$c_2Ebitstring_2Eboolify \in (((ty_2Elist_2Elist\ 2)^{(ty_2Elist_2Elist\ ty_2Enum_2Enum)})^{(ty_2Elist_2Elist\ 2)}) \quad (22)$$

Definition 43 We define $c_2Ebitstring_2En2v$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Ebitstring_2Eboolify$

Let $c_2Elist_2ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2ECONS\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{A_27a}) \quad (23)$$

Let $c_2Elist_2ELENGTH : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2ELENGTH\ A_27a \in (ty_2Enum_2Enum^{(ty_2Elist_2Elist\ A_27a)}) \quad (24)$$

Let $c_2Elist_2ETAKE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2ETAKE\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{ty_2Enum_2Enum}) \quad (25)$$

Definition 44 We define $c_2Ebitstring_2Eshiftr$ to be $\lambda V0v \in (ty_2Elist_2Elist\ 2).\lambda V1m \in ty_2Enum_2Enum$

Let $c_2Elist_2EDROP : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2EDROP\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{ty_2Enum_2Enum}) \quad (26)$$

Definition 45 We define $c_2Ecombin_2EK$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0x \in A_27a.(\lambda V1y \in A_27b.V0x))$

Let $c_2Elist_2EGENLIST : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2EGENLIST\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{ty_2Enum_2Enum})^{(A_27a^{ty_2Enum_2Enum})}) \quad (27)$$

Let $c_2Elist_2EAPPEND : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2EAPPEND\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{(ty_2Elist_2Elist\ A_27a)}) \quad (28)$$

Definition 46 We define $c_2Elist_2EPAD_LEFT$ to be $\lambda A_27a : \iota.\lambda V0c \in A_27a.\lambda V1n \in ty_2Enum_2Enum$

Definition 47 We define $c_2Ebitstring_2Ezero_extend$ to be $\lambda V0n \in ty_2Enum_2Enum.\lambda V1v \in (ty_2Elist_2Elist\ 2)$

Definition 48 We define $c_2Ebitstring_2Efixwidth$ to be $\lambda V0n \in ty_2Enum_2Enum.\lambda V1v \in (ty_2Elist_2Elist\ 2)$

Definition 49 We define $c_2Ebitstring_2Efield$ to be $\lambda V0h \in ty_2Enum_2Enum.\lambda V1l \in ty_2Enum_2Enum$

Definition 50 We define $c_2Ebitstring_2Etestbit$ to be $\lambda V0b \in ty_2Enum_2Enum.\lambda V1v \in (ty_2Elist_2Elist\ 2)$

Definition 51 We define $c_2Ebitstring_2Ev2w$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2Elist_2Elist\ 2).(ap\ (c_2EfcP_2Elist\ 2)\ v)$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0n \in ty_2Enum_2Enum. (ap\ (c_2Ebitstring_2Ev2w\ A_27a)\ (ap\ c_2Ebitstring_2En2v\ V0n)) = (ap\ (c_2Ewords_2En2w\ A_27a)\ V0n))) \quad (29)$$

Assume the following.

$$True \quad (30)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_27a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \quad (31)$$

Assume the following.

$$(\forall V0t \in 2. (((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \quad (32)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (33)$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.\text{nonempty } A_27a \Rightarrow \forall A_27b.\text{nonempty } A_27b \Rightarrow \forall A_27c. \\
& \text{nonempty } A_27c \Rightarrow \forall A_27d.\text{nonempty } A_27d \Rightarrow \forall A_27e.\text{nonempty } \\
& A_27e \Rightarrow \forall A_27f.\text{nonempty } A_27f \Rightarrow \forall A_27g.\text{nonempty } A_27g \Rightarrow \\
& \forall A_27h.\text{nonempty } A_27h \Rightarrow \forall A_27i.\text{nonempty } A_27i \Rightarrow \forall A_27j. \\
& \text{nonempty } A_27j \Rightarrow \forall A_27k.\text{nonempty } A_27k \Rightarrow \forall A_27l.\text{nonempty } \\
& A_27l \Rightarrow \forall A_27m.\text{nonempty } A_27m \Rightarrow \forall A_27n.\text{nonempty } A_27n \Rightarrow \\
& \forall A_27o.\text{nonempty } A_27o \Rightarrow \forall A_27p.\text{nonempty } A_27p \Rightarrow \forall A_27q. \\
& \text{nonempty } A_27q \Rightarrow \forall A_27r.\text{nonempty } A_27r \Rightarrow \forall A_27s.\text{nonempty } \\
& A_27s \Rightarrow \forall A_27t.\text{nonempty } A_27t \Rightarrow ((\forall V0v \in (\text{ty_2Elist_2Elist} \\
& 2)).(\forall V1n \in \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_or} \\
& A_27c) (ap (c_2Ebitstring_2Ev2w A_27c) V0v)) (ap (c_2Ewords_2En2w} \\
& A_27c) V1n))) = (ap (ap (c_2Ewords_2Eword_or A_27c) (ap (c_2Ebitstring_2Ev2w} \\
& A_27c) V0v)) (ap (c_2Ebitstring_2Ev2w A_27c) (ap c_2Ebitstring_2En2v} \\
& V1n)))))) \wedge ((\forall V2v \in (\text{ty_2Elist_2Elist} 2)).(\forall V3n \in \\
& \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_or A_27d) (ap (c_2Ewords_2En2w} \\
& A_27d) V3n)) (ap (c_2Ebitstring_2Ev2w A_27d) V2v)) = (ap (ap (c_2Ewords_2Eword_or} \\
& A_27d) (ap (c_2Ebitstring_2Ev2w A_27d) (ap c_2Ebitstring_2En2v} \\
& V3n))) (ap (c_2Ebitstring_2Ev2w A_27d) V2v)))))) \wedge ((\forall V4v \in \\
& (\text{ty_2Elist_2Elist} 2)).(\forall V5n \in \text{ty_2Enum_2Enum}.\text{((ap (ap} \\
& (\text{c_2Ewords_2Eword_and A_27e) (ap (c_2Ebitstring_2Ev2w A_27e) \\
& V4v)) (ap (c_2Ewords_2En2w A_27e) V5n)) = (ap (ap (c_2Ewords_2Eword_and} \\
& A_27e) (ap (c_2Ebitstring_2Ev2w A_27e) V4v)) (ap (c_2Ebitstring_2Ev2w} \\
& A_27e) (ap c_2Ebitstring_2En2v V5n)))))) \wedge ((\forall V6v \in (\text{ty_2Elist_2Elist} \\
& 2)).(\forall V7n \in \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_and} \\
& A_27f) (ap (c_2Ewords_2En2w A_27f) V7n)) (ap (c_2Ebitstring_2Ev2w} \\
& A_27f) V6v)) = (ap (ap (c_2Ewords_2Eword_and A_27f) (ap (c_2Ebitstring_2Ev2w} \\
& A_27f) (ap c_2Ebitstring_2En2v V7n))) (ap (c_2Ebitstring_2Ev2w} \\
& A_27f) V6v)))))) \wedge ((\forall V8v \in (\text{ty_2Elist_2Elist} 2)).(\forall V9n \in \\
& \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_xor A_27g) (ap (c_2Ebitstring_2Ev2w} \\
& A_27g) V8v)) (ap (c_2Ewords_2En2w A_27g) V9n)) = (ap (ap (c_2Ewords_2Eword_xor} \\
& A_27g) (ap (c_2Ebitstring_2Ev2w A_27g) V8v)) (ap (c_2Ebitstring_2Ev2w} \\
& A_27g) (ap c_2Ebitstring_2En2v V9n)))))) \wedge ((\forall V10v \in (\text{ty_2Elist_2Elist} \\
& 2)).(\forall V11n \in \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_xor} \\
& A_27h) (ap (c_2Ewords_2En2w A_27h) V11n)) (ap (c_2Ebitstring_2Ev2w} \\
& A_27h) V10v)) = (ap (ap (c_2Ewords_2Eword_xor A_27h) (ap (c_2Ebitstring_2Ev2w} \\
& A_27h) (ap c_2Ebitstring_2En2v V11n))) (ap (c_2Ebitstring_2Ev2w} \\
& A_27h) V10v)))))) \wedge ((\forall V12v \in (\text{ty_2Elist_2Elist} 2)).(\forall V13n \in \\
& \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_nor A_27i) (ap (c_2Ebitstring_2Ev2w} \\
& A_27i) V12v)) (ap (c_2Ewords_2En2w A_27i) V13n)) = (ap (ap (c_2Ewords_2Eword_nor} \\
& A_27i) (ap (c_2Ebitstring_2Ev2w A_27i) V12v)) (ap (c_2Ebitstring_2Ev2w} \\
& A_27i) (ap c_2Ebitstring_2En2v V13n)))))) \wedge ((\forall V14v \in (\text{ty_2Elist_2Elist} \\
& 2)).(\forall V15n \in \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_nor} \\
& A_27j) (ap (c_2Ewords_2En2w A_27j) V15n)) (ap (c_2Ebitstring_2Ev2w} \\
& A_27j) V14v)) = (ap (ap (c_2Ewords_2Eword_nor A_27j) (ap (c_2Ebitstring_2Ev2w} \\
& A_27j) (ap c_2Ebitstring_2En2v V15n))) (ap (c_2Ebitstring_2Ev2w} \\
& A_27j) V14v)))))) \wedge ((\forall V16v \in (\text{ty_2Elist_2Elist} 2)).(\forall V17n \in \\
& \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_nand A_27k) (ap (} \\
& \text{c_2Ebitstring_2Ev2w A_27k) V16v)) (ap (c_2Ewords_2En2w A_27k) \\
& V17n)) = (ap (ap (c_2Ewords_2Eword_nand A_27k) (ap (c_2Ebitstring_2Ev2w} \\
& A_27k) V16v)) (ap (c_2Ebitstring_2Ev2w A_27k) (ap c_2Ebitstring_2En2v} \\
& V17n)))))) \wedge ((\forall V18v \in (\text{ty_2Elist_2Elist} 2)).(\forall V19n \in \\
& \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_nand A_27l) (ap (} \\
& \text{c_2Ewords_2En2w A_27l) V19n)) (ap (c_2Ebitstring_2Ev2w A_27l) \\
& V18v)) = (ap (ap (c_2Ewords_2Eword_nand A_27l) (ap (c_2Ebitstring_2Ev2w} \\
& A_27l) (ap c_2Ebitstring_2En2v V19n))) (ap (c_2Ebitstring_2Ev2w} \\
& A_27l) V18v)))))) \wedge ((\forall V20v \in (\text{ty_2Elist_2Elist} 2)).(\forall V21n \in \\
& \text{ty_2Enum_2Enum}.\text{((ap (ap (c_2Ewords_2Eword_xnor A_27m) (ap (} \\
& \text{c_2Ebitstring_2Ev2w A_27m) V20v)) (ap (c_2Ewords_2En2w A_27m) \\
& V21n)) = (ap (ap (c_2Ewords_2Eword_xnor A_27m) (ap (c_2Ebitstring_2Ev2w} \\
& A_27m) V20v)) (ap (c_2Ewords_2En2w A_27m) \\
\end{aligned}$$