

thm_2Eblast_2Eword__lsl__bv__expand (TMY- DoGXnagRBp15upZ9ZpMtVXAqfcAvyhhP)

October 26, 2020

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{1}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{2}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \tag{3}$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \tag{4}$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \tag{5}$$

Definition 4 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 5 We define c_2Ebool_2E21 to be $\lambda A.\lambda a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c_2Emin_2E3D\ (2^{A-27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V2x \in 2.V2x))$

Definition 6 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num\ (c_2Enum_2ESUC_REP\ m))$

Let $c_2Earithmetic_2E2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \tag{6}$$

Definition 7 We define $c_2Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EBIT2) n)$.

Definition 8 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $c_2Elogroot_2ELOG : \iota$ be given. Assume the following.

$$c_2Elogroot_2ELOG \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (7)$$

Definition 9 We define c_2Ebit_2ELOG2 to be $(ap c_2Elogroot_2ELOG (ap c_2Earithmetic_2ENUMERAL))$.

Definition 10 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\text{if } (\exists x \in A.p (ap P x)) \text{ then } (the (\lambda x.x \in A) \text{ of type } \iota \Rightarrow \iota)$.

Definition 11 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21) 2) (\lambda V0t \in 2.V0t)$.

Definition 12 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 13 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21) 2) (\lambda V2t \in 2.V0t)))$.

Definition 14 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.(ap (c_2Ebool_2E_21) 2) (\lambda V2t \in 2.V0t))))$.

Definition 15 We define $c_2Ecombin_2ES$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.(\lambda V0f \in ((A_27c^{A_27b})^{A_27a}))$.

Definition 16 We define $c_2Ecombin_2EC$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.(\lambda V0f \in ((A_27c^{A_27b})^{A_27a}))$.

Definition 17 We define $c_2Ecombin_2EK$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0x \in A_27a.(\lambda V1y \in A_27b.V0x))$.

Definition 18 We define $c_2Ecombin_2EI$ to be $\lambda A_27a : \iota.(ap (ap (c_2Ecombin_2ES) A_27a) (A_27a^{A_27a}))$.

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty_2Elist_2Elist A0) \quad (8)$$

Let $c_2Elist_2EFOLDL : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Elist_2EFOLDL \\ & A_27a A_27b \in (((A_27b^{(ty_2Elist_2Elist A_27a)})^{A_27b})^{(A_27b^{A_27a})^{A_27b}}) \end{aligned} \quad (9)$$

Definition 19 We define $c_2Emarker_2EAbbrev$ to be $\lambda V0x \in 2.V0x$.

Let $c_2Earithmetic_2EEVEN : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EEVEN \in (2^{ty_2Enum_2Enum}) \quad (10)$$

Let $c_2Earithmetic_2EODD : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EODD \in (2^{ty_2Enum_2Enum}) \quad (11)$$

Definition 20 We define $c_Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_Emin_2E_3D_3D_3E V0t) c_Ebool_2E_7E))$

Definition 21 We define $c_Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_Emin_2E_40$

Definition 22 We define $c_Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 23 We define $c_Earithmetic_2E_3E$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 24 We define $c_Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_Ebool_2E_21 2) (\lambda V2t \in$

Definition 25 We define $c_Earithmetic_2E_3E_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 26 We define $c_Eprim_rec_2EPRE$ to be $\lambda V0m \in ty_2Enum_2Enum.(ap (ap (ap (c_Ebool_2E_2E$

Let $c_Earithmetic_2EEXP : \iota$ be given. Assume the following.

$$c_Earithmetic_2EEXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (12)$$

Let $c_Earithmetic_2E_2A : \iota$ be given. Assume the following.

$$c_Earithmetic_2E_2A \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (13)$$

Definition 27 We define $c_Enumeral_2EiiSUC$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap c_Enum_2ESUC (ap$

Definition 28 We define $c_Enumeral_2EiZ$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $c_Elist_2EMAP : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_Elist_2EMAP \\ & A_27a A_27b \in (((ty_Elist_2Elist A_27b)^{(ty_Elist_2Elist A_27a)})^{(A_27b^{A_27a})}) \end{aligned} \quad (14)$$

Let $c_Elist_2ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_Elist_2ECONS A_27a \in (((ty_Elist_2Elist A_27a)^{(ty_Elist_2Elist A_27a)})^{A_27a}) \quad (15)$$

Let $c_Elist_2ELIST_TO_SET : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_Elist_2ELIST_TO_SET A_27a \in ((2^{A_27a})^{(ty_Elist_2Elist A_27a)}) \quad (16)$$

Definition 29 We define c_Ebool_2EIN to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.(\lambda V1f \in (2^{A_27a}).(ap V1f V0x))$

Let $c_Elist_2ESNOC : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_Elist_2ESNOC A_27a \in (((ty_Elist_2Elist A_27a)^{(ty_Elist_2Elist A_27a)})^{A_27a}) \quad (17)$$

Let $c_2Elist_2ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2ENIL\ A_27a \in (ty_2Elist_2Elist\ A_27a) \quad (18)$$

Let $c_2Erich_list_2ECOUNT_LIST : \iota$ be given. Assume the following.

$$c_2Erich_list_2ECOUNT_LIST \in ((ty_2Elist_2Elist\ ty_2Enum_2Enum)^{ty_2Enum_2Enum}) \quad (19)$$

Definition 30 We define $c_2Ecombin_2Eo$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in (A_27b^{A_27c}).\lambda V1$

Let $ty_2Efcf_2Efinite_image : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Efcf_2Efinite_image\ A0) \quad (20)$$

Let $ty_2Ebool_2Eitself : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Ebool_2Eitself\ A0) \quad (21)$$

Let $c_2Ebool_2Ethe_value : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ebool_2Ethe_value\ A_27a \in (ty_2Ebool_2Eitself\ A_27a) \quad (22)$$

Let $c_2Efcf_2Edimindex : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Efcf_2Edimindex\ A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself\ A_27a)}) \quad (23)$$

Definition 31 We define $c_2Ebool_2E_3F_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ (ap\ c_2Ebool_2E_2F_25C$

Definition 32 We define $c_2Efcf_2Efinite_index$ to be $\lambda A_27a : \iota.(ap\ (c_2Emin_2E_40\ (A_27a^{ty_2Enum_2Enum}$

Let $ty_2Efcf_2Ecart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Efcf_2Ecart\ A0\ A1) \quad (24)$$

Let $c_2Efcf_2Edest_cart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Efcf_2Edest_cart\ A_27a\ A_27b \in ((A_27a^{(ty_2Efcf_2Efinite_image\ A_27b)})^{(ty_2Efcf_2Ecart\ A_27a\ A_27b)}) \quad (25)$$

Definition 33 We define $c_2Efcf_2Efcf_index$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in (ty_2Efcf_2Ecart\ A_27a$

Definition 34 We define c_2Efcf_2EFCP to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0g \in (A_27a^{ty_2Enum_2Enum}).(ap$

Definition 35 We define c_2Ebit_2ESBIT to be $\lambda V0b \in 2.\lambda V1n \in ty_2Enum_2Enum.(ap\ (ap\ (ap\ (c_2Ebo$

Let $c_Esum_num_ESUM : \iota$ be given. Assume the following.

$$c_Esum_num_ESUM \in ((ty_Enum_Enum^{(ty_Enum_Enum^{ty_Enum_Enum})})^{ty_Enum_Enum}) \quad (26)$$

Definition 36 We define c_Ewords_Ew2n to be $\lambda A_27a : \iota. \lambda V0w \in (ty_EfcP_Ecart\ 2\ A_27a). (ap\ (ap\ c_Esum_num_ESUM\ w))$

Let $c_Earithmetic_E_2D : \iota$ be given. Assume the following.

$$c_Earithmetic_E_2D \in ((ty_Enum_Enum^{ty_Enum_Enum})^{ty_Enum_Enum}) \quad (27)$$

Definition 37 We define $c_Earithmetic_E_3C_3D$ to be $\lambda V0m \in ty_Enum_Enum. \lambda V1n \in ty_Enum_Enum. c_Earithmetic_E_2D\ m\ n$

Definition 38 We define $c_Ewords_Eword_lsl$ to be $\lambda A_27a : \iota. \lambda V0w \in (ty_EfcP_Ecart\ 2\ A_27a). \lambda V1l \in ty_Enum_Enum. c_Ewords_Ew2n\ w\ l$

Definition 39 We define $c_Ewords_Eword_lsl_bv$ to be $\lambda A_27a : \iota. \lambda V0w \in (ty_EfcP_Ecart\ 2\ A_27a). \lambda V1l \in ty_Enum_Enum. c_Ewords_Eword_lsl\ w\ l$

Let $c_Earithmetic_EMOD : \iota$ be given. Assume the following.

$$c_Earithmetic_EMOD \in ((ty_Enum_Enum^{ty_Enum_Enum})^{ty_Enum_Enum}) \quad (28)$$

Let $c_Ewords_Edimword : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_Ewords_Edimword\ A_27a \in (ty_Enum_Enum^{(ty_Ebool_Eitself\ A_27a)}) \quad (29)$$

Let $c_Earithmetic_EDIV : \iota$ be given. Assume the following.

$$c_Earithmetic_EDIV \in ((ty_Enum_Enum^{ty_Enum_Enum})^{ty_Enum_Enum}) \quad (30)$$

Definition 40 We define $c_Ebit_EDIV_EXP$ to be $\lambda V0x \in ty_Enum_Enum. \lambda V1n \in ty_Enum_Enum. c_Earithmetic_EDIV\ x\ n$

Definition 41 We define $c_Ebit_EMOD_EXP$ to be $\lambda V0x \in ty_Enum_Enum. \lambda V1n \in ty_Enum_Enum. c_Earithmetic_EMOD\ x\ n$

Definition 42 We define c_Ebit_EBITS to be $\lambda V0h \in ty_Enum_Enum. \lambda V1l \in ty_Enum_Enum. \lambda V2n \in ty_Enum_Enum. c_Ebit_EMOD_EXP\ h\ l\ n$

Definition 43 We define $c_Earithmetic_EBIT1$ to be $\lambda V0n \in ty_Enum_Enum. (ap\ (ap\ c_Earithmetic_EBIT1)\ n)$

Definition 44 We define c_Ebit_EBIT to be $\lambda V0b \in ty_Enum_Enum. \lambda V1n \in ty_Enum_Enum. (ap\ (ap\ c_Ebit_EBIT1)\ b)\ n$

Definition 45 We define c_Ewords_En2w to be $\lambda A_27a : \iota. \lambda V0n \in ty_Enum_Enum. (ap\ (c_EfcP_EFC)\ n)\ A_27a$

Definition 46 We define c_Ewords_Ew2w to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0w \in (ty_EfcP_Ecart\ 2\ A_27a). c_Ewords_Ew2n\ w\ A_27b$

Definition 47 We define $c_Earithmetic_EMIN$ to be $\lambda V0m \in ty_Enum_Enum. \lambda V1n \in ty_Enum_Enum. c_Earithmetic_E_2D\ m\ n$

Definition 48 We define $c_Ewords_Eword_bits$ to be $\lambda A_27a : \iota. \lambda V0h \in ty_Enum_Enum. \lambda V1l \in ty_Enum_Enum. c_Ewords_Eword_lsl_bv\ h\ l$

Definition 49 We define $c_Ewords_Eword_extract$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0h \in ty_Enum_Enum. c_Ewords_Eword_bits\ h\ A_27b$

Definition 50 We define $c_2Ewords_2Eword_add$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1$

Definition 51 We define $c_2Ewords_2Eword_ror$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1$

Definition 52 We define $c_2Ewords_2Eword_rol$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1$

Definition 53 We define $c_2Ewords_2Eword_lsr$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1$

Definition 54 We define $c_2Ewords_2Eword_msb$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1$

Definition 55 We define $c_2Ewords_2Eword_asr$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B V0m) c_2Enum_2E0) = V0m)) \quad (31)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B c_2Enum_2E0) V0m) = V0m) \wedge (((ap (ap c_2Earithmetic_2E_2B V0m) c_2Enum_2E0) = V0m) \wedge (((ap (ap c_2Earithmetic_2E_2B (ap c_2Enum_2ESUC V0m)) V1n) = (ap c_2Enum_2ESUC (ap (ap c_2Earithmetic_2E_2B V0m) V1n))) \wedge ((ap (ap c_2Earithmetic_2E_2B V0m) (ap c_2Enum_2ESUC V1n)) = (ap c_2Enum_2ESUC (ap (ap c_2Earithmetic_2E_2B V0m) V1n)))))))))) \quad (32)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B V0m) V1n) = (ap (ap c_2Earithmetic_2E_2B V1n) V0m)))) \quad (33)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B V0m) V1n) = (ap (ap c_2Earithmetic_2E_2B V1n) V0m)))) \quad (34)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\forall V2p \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B V0m) (ap (ap c_2Earithmetic_2E_2B V1n) V2p)) = (ap (ap c_2Earithmetic_2E_2B (ap (ap c_2Earithmetic_2E_2B V0m) V1n)) V2p)))))) \quad (35)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n)) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Enum_2ESUC V0m)) V1n)))))) \quad (36)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.(p (ap (ap c_2Earithmetic_2E_3C_3D c_2Enum_2E0) V0n))) \quad (37)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\neg(p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D V1n) V0m)))))) \quad (38)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3C_3D V0n) c_2Enum_2E0)) \Leftrightarrow (V0n = c_2Enum_2E0))) \quad (39)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(((ap (ap c_2Earithmetic_2E_2D c_2Enum_2E0) V0m) = c_2Enum_2E0) \wedge ((ap (ap c_2Earithmetic_2E_2D V0m) c_2Enum_2E0) = V0m)))) \quad (40)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(((ap c_2Enum_2ESUC V0m) = (ap (ap c_2Earithmetic_2E_2B V0m) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))))) \quad (41)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(((ap (ap c_2Earithmetic_2E_2A c_2Enum_2E0) V0m) = c_2Enum_2E0) \wedge (((ap (ap c_2Earithmetic_2E_2A V0m) c_2Enum_2E0) = c_2Enum_2E0) \wedge (((ap (ap c_2Earithmetic_2E_2A (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))) V0m) = V0m) \wedge (((ap (ap c_2Earithmetic_2E_2A V0m) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))) = V0m) \wedge ((ap (ap c_2Earithmetic_2E_2A (ap c_2Enum_2ESUC V0m)) V1n) = (ap c_2Earithmetic_2E_2B (ap (ap c_2Earithmetic_2E_2A V0m) V1n)) V1n) \wedge ((ap (ap c_2Earithmetic_2E_2A V0m) (ap c_2Enum_2ESUC V1n)) = (ap (ap c_2Earithmetic_2E_2B V0m) (ap (ap c_2Earithmetic_2E_2A V0m) V1n)))))))))) \quad (42)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\forall V2p \in ty_2Enum_2Enum.(((ap (ap c_2Earithmetic_2E_2B V0m) V2p) = (ap (ap c_2Earithmetic_2E_2B V1n) V2p)) \Leftrightarrow (V0m = V1n)))))) \quad (43)$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad \forall V2p \in ty_2Enum_2Enum. (((p (ap (ap (ap c_2Earithmetic_2E_3C_3D \\
& \quad V0m) V1n)) \wedge (p (ap (ap c_2Earithmetic_2E_3C_3D V1n) V2p))) \Rightarrow (p (\\
& \quad \quad ap (ap c_2Earithmetic_2E_3C_3D V0m) V2p))))))
\end{aligned} \tag{44}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad \forall V2p \in ty_2Enum_2Enum. (((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& \quad V0m) V1n)) \wedge (p (ap (ap c_2Eprim_rec_2E_3C V1n) V2p))) \Rightarrow (p (ap (ap \\
& \quad \quad c_2Eprim_rec_2E_3C V0m) V2p))))))
\end{aligned} \tag{45}$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (p (ap (ap c_2Earithmetic_2E_3C_3D V0m) V0m))) \tag{46}$$

Assume the following.

$$(\forall V0c \in ty_2Enum_2Enum. ((ap (ap c_2Earithmetic_2E_2D V0c) V0c) = c_2Enum_2E0)) \tag{47}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad (V0m = V1n) \Leftrightarrow ((p (ap (ap c_2Earithmetic_2E_3C_3D V0m) V1n)) \wedge (p (\\
& \quad \quad ap (ap c_2Earithmetic_2E_3C_3D V1n) V0m))))))
\end{aligned} \tag{48}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad \forall V2p \in ty_2Enum_2Enum. ((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& \quad (ap (ap c_2Earithmetic_2E_2B V0m) V1n)) (ap (ap c_2Earithmetic_2E_2B \\
& \quad \quad V0m) V2p))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D V1n) V2p))))))
\end{aligned} \tag{49}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad (\neg (p (ap (ap c_2Earithmetic_2E_3C_3D V0m) V1n))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& \quad \quad (ap c_2Enum_2ESUC V1n)) V0m))))))
\end{aligned} \tag{50}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& \quad (\neg (V0m = V1n)) \Leftrightarrow ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Enum_2ESUC \\
& \quad \quad V0m)) V1n)) \vee (p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Enum_2ESUC \\
& \quad \quad \quad V1n)) V0m))))))
\end{aligned} \tag{51}$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.((ap\ c_2Enum_2ESUC\ V0n) = (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2ENUMERAL\ (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO)))\ V0n))) \quad (52)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\forall V2p \in ty_2Enum_2Enum.((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V0m)\ (ap\ (ap\ c_2Earithmetic_2E_2D\ V1n)\ V2p))) \Leftrightarrow ((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0m)\ V2p))\ V1n)) \vee (p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V0m)\ c_2Enum_2E0))))))) \quad (53)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\forall V2p \in ty_2Enum_2Enum.((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ (ap\ (ap\ c_2Earithmetic_2E_2D\ V0m)\ V1n))\ V2p))) \Leftrightarrow (p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V0m)\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V1n)\ V2p)))))) \quad (54)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\forall V2p \in ty_2Enum_2Enum.((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V0m)\ (ap\ (ap\ c_2Earithmetic_2E_2D\ V1n)\ V2p))) \Leftrightarrow (p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0m)\ V2p))\ V1n)))))) \quad (55)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\forall V2p \in ty_2Enum_2Enum.((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ (ap\ (ap\ c_2Earithmetic_2E_2D\ V0m)\ V1n))\ V2p))) \Leftrightarrow ((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V0m)\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V1n)\ V2p))) \wedge (p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ c_2Enum_2E0)\ V2p)))))) \quad (56)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.(\forall V1k \in ty_2Enum_2Enum.((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V1k)\ V0n)) \Rightarrow ((ap\ (ap\ c_2Earithmetic_2EMOD\ V1k)\ V0n) = V1k)))) \quad (57)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ c_2Enum_2E0)\ V1n)) \Rightarrow (p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ (ap\ (ap\ c_2Earithmetic_2EMOD\ V0m)\ V1n))\ V1n)))) \quad (58)$$

Assume the following.

$$\begin{aligned}
& (\forall V0x \in ty_2Enum_2Enum. (\forall V1y \in ty_2Enum_2Enum. (\\
& (p (ap (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) V1y)) \Rightarrow (((ap (ap c_2Earithmetic_2EMOD \\
& V0x) V1y) = V0x) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C V0x) V1y)))))) \\
& \hspace{15em} (59)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0f \in ((A_27a^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}). \\
& (\forall V1g \in (A_27a^{ty_2Enum_2Enum}). ((\forall V2n \in ty_2Enum_2Enum. \\
& ((ap V1g (ap c_2Enum_2ESUC V2n)) = (ap (ap V0f V2n) (ap c_2Enum_2ESUC \\
& V2n)))) \Leftrightarrow ((\forall V3n \in ty_2Enum_2Enum. ((ap V1g (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT1 V3n))) = (ap (ap V0f (ap (ap c_2Earithmetic_2E_2D \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 V3n))) \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 V3n)))))) \wedge \\
& (\forall V4n \in ty_2Enum_2Enum. ((ap V1g (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT2 V4n))) = (ap (ap V0f (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT1 V4n))) (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT2 V4n))))))))) \\
& \hspace{15em} (60)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0P \in (2^{ty_2Enum_2Enum}). (\forall V1a \in ty_2Enum_2Enum. \\
& (\forall V2b \in ty_2Enum_2Enum. ((p (ap V0P (ap (ap c_2Earithmetic_2E_2D \\
& V1a) V2b))) \Leftrightarrow (\forall V3d \in ty_2Enum_2Enum. (((V2b = (ap (ap c_2Earithmetic_2E_2B \\
& V1a) V3d)) \Rightarrow (p (ap V0P c_2Enum_2E0))) \wedge ((V1a = (ap (ap c_2Earithmetic_2E_2B \\
& V2b) V3d)) \Rightarrow (p (ap V0P V3d)))))))))) \\
& \hspace{15em} (61)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. (\\
& \forall V2p \in ty_2Enum_2Enum. (((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& (ap (ap c_2Earithmetic_2EMIN V1m) V0n)) V2p)) \Leftrightarrow ((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V1m) V2p)) \vee (p (ap (ap c_2Earithmetic_2E_3C_3D V0n) V2p)))) \wedge ((\\
& p (ap (ap c_2Earithmetic_2E_3C_3D V2p) (ap (ap c_2Earithmetic_2EMIN \\
& V1m) V0n))) \Leftrightarrow ((p (ap (ap c_2Earithmetic_2E_3C_3D V2p) V1m)) \wedge (p \\
& (ap (ap c_2Earithmetic_2E_3C_3D V2p) V0n)))))) \\
& \hspace{15em} (62)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. ((ap (ap c_2Earithmetic_2EMIN V0n) \\
& V0n) = V0n)) \\
& \hspace{15em} (63)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0h \in ty_2Enum_2Enum. (\forall V1l \in ty_2Enum_2Enum. (\\
& \quad \forall V2n \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C V2n) \\
& \quad (ap (ap c_2Earithmetic_2EEXP (ap c_2Earithmetic_2ENUMERAL (ap \\
& \quad \quad c_2Earithmetic_2EBIT2 c_2Earithmetic_2EZERO))) V1l))) \Rightarrow ((ap \\
& \quad \quad (ap (ap c_2Ebit_2EBITS V0h) V1l) V2n) = c_2Enum_2E0))))))
\end{aligned} \tag{64}$$

Assume the following.

$$True \tag{65}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p \\
& \quad V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2))))))
\end{aligned} \tag{66}$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \tag{67}$$

Assume the following.

$$(\forall V0t \in 2. ((p V0t) \vee \neg(p V0t))) \tag{68}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in \\
& \quad A_27a. (p V0t)) \Leftrightarrow (p V0t)))
\end{aligned} \tag{69}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p V0t1) \wedge \\
& \quad ((p V1t2) \wedge (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \wedge (p V2t3))))))
\end{aligned} \tag{70}$$

Assume the following.

$$(\forall V0t \in 2. (\neg(p V0t) \Rightarrow ((p V0t) \Rightarrow False))) \tag{71}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2. (((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow \\
& \quad (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge \\
& \quad (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t))))))
\end{aligned} \tag{72}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2. (((True \vee (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \vee True) \Leftrightarrow True) \wedge \\
& \quad (((False \vee (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee False) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee \\
& \quad (p V0t)) \Leftrightarrow (p V0t))))))
\end{aligned} \tag{73}$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge ((p V0t) \Rightarrow False) \Leftrightarrow (\neg (p V0t)))))) \quad (74)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (75)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(V0x = V0x)) \quad (76)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (77)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (78)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow (\forall V0f \in (A_27b^{A_27a}).(\forall V1g \in (A_27b^{A_27a}).((V0f = V1g) \Leftrightarrow (\forall V2x \in A_27a.((ap V0f V2x) = (ap V1g V2x)))))) \quad (79)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (80)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0t1 \in A_27a.(\forall V1t2 \in A_27a.(((ap (ap (ap (c_2Ebool_2ECOND A_27a) c_2Ebool_2ET) V0t1) V1t2) = V0t1) \wedge ((ap (ap (ap (c_2Ebool_2ECOND A_27a) c_2Ebool_2EF) V0t1) V1t2) = V1t2)))) \quad (81)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0P \in (2^{A_27a}).((\neg(\forall V1x \in A_27a.(p (ap V0P V1x)))) \Leftrightarrow (\exists V2x \in A_27a.(\neg(p (ap V0P V2x)))))) \quad (82)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.((\neg((p V0A) \Rightarrow (p V1B))) \Leftrightarrow ((p V0A) \wedge (\neg(p V1B)))))) \quad (83)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p V0A) \vee (p V1B) \vee (p V2C))) \Leftrightarrow (((p V0A) \vee (p V1B)) \vee (p V2C)))))) \quad (84)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p V0A) \wedge (p V1B))) \Leftrightarrow ((\neg(p V0A) \vee \neg(p V1B)))) \wedge ((\neg((p V0A) \vee (p V1B))) \Leftrightarrow ((\neg(p V0A) \wedge \neg(p V1B))))))) \quad (85)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p V0A) \vee (p V1B) \wedge (p V2C)) \Leftrightarrow (((p V0A) \vee (p V1B)) \wedge ((p V0A) \vee (p V2C)))))) \quad (86)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p V1B) \wedge (p V2C) \vee (p V0A)) \Leftrightarrow (((p V1B) \vee (p V0A)) \wedge ((p V2C) \vee (p V0A)))))) \quad (87)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((p V0A) \Rightarrow (p V1B)) \Leftrightarrow ((\neg(p V0A) \vee (p V1B)))))) \quad (88)$$

Assume the following.

$$(\forall V0P \in 2.(\forall V1Q \in 2.(\forall V2R \in 2.(((p V0P) \vee (p V1Q)) \Rightarrow (p V2R)) \Leftrightarrow (((p V0P) \Rightarrow (p V2R)) \wedge ((p V1Q) \Rightarrow (p V2R)))))) \quad (89)$$

Assume the following.

$$(\forall V0t \in 2.(((p V0t) \Rightarrow \text{False}) \Leftrightarrow ((p V0t) \Leftrightarrow \text{False}))) \quad (90)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (91)$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1x_{27} \in 2.(\forall V2y \in 2.(\forall V3y_{27} \in 2.(((p V0x) \Leftrightarrow (p V1x_{27})) \wedge ((p V1x_{27}) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_{27})))) \Rightarrow (((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_{27}) \Rightarrow (p V3y_{27})))))) \quad (92)$$

Assume the following.

$$\forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0f \in (2^{A_{27a}}). (\forall V1v \in A_{27a}. ((\forall V2x \in A_{27a}. ((V2x = V1v) \Rightarrow (p (ap V0f V2x)))) \Leftrightarrow (p (ap V0f V1v)))))) \quad (93)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c. \\
& nonempty\ A_27c \Rightarrow (\forall V0f \in (A_27b^{A_27a}). (\forall V1g \in (A_27a^{A_27c}). \\
& (\forall V2x \in A_27c. ((ap\ (ap\ (ap\ (c_2Ecombin_2Eo\ A_27c\ A_27b\ A_27a) \\
& V0f)\ V1g)\ V2x) = (ap\ V0f\ (ap\ V1g\ V2x))))))
\end{aligned} \tag{94}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0x \in A_27a. (\forall V1y \in A_27b. ((ap\ (ap\ (c_2Ecombin_2EK \\
& A_27a\ A_27b)\ V0x)\ V1y) = V0x)))
\end{aligned} \tag{95}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((ap\ (c_2Ecombin_2EI \\
& A_27a)\ V0x) = V0x))
\end{aligned} \tag{96}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0f \in (A_27b^{A_27a}). (((ap\ (ap\ (c_2Ecombin_2Eo\ A_27a\ A_27b \\
& A_27b)\ (c_2Ecombin_2EI\ A_27b))\ V0f) = V0f) \wedge ((ap\ (ap\ (c_2Ecombin_2Eo \\
& A_27a\ A_27b\ A_27a)\ V0f)\ (c_2Ecombin_2EI\ A_27a)) = V0f)))
\end{aligned} \tag{97}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0x \in (ty_2EfcP_2Ecart\ A_27a\ A_27b). (\forall V1y \in (ty_2EfcP_2Ecart \\
& A_27a\ A_27b). ((V0x = V1y) \Leftrightarrow (\forall V2i \in ty_2Enum_2Enum. ((p\ (ap \\
& (ap\ c_2Eprim_rec_2E_3C\ V2i)\ (ap\ (c_2EfcP_2Edimindex\ A_27b)\ (\\
& c_2Ebool_2Ethe_value\ A_27b)))) \Rightarrow ((ap\ (ap\ (c_2EfcP_2EfcP_index \\
& A_27a\ A_27b)\ V0x)\ V2i) = (ap\ (ap\ (c_2EfcP_2EfcP_index\ A_27a\ A_27b) \\
& V1y)\ V2i))))))
\end{aligned} \tag{98}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0g \in (A_27a^{ty_2Enum_2Enum}). (\forall V1i \in ty_2Enum_2Enum. \\
& ((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V1i)\ (ap\ (c_2EfcP_2Edimindex\ A_27b) \\
& (c_2Ebool_2Ethe_value\ A_27b)))) \Rightarrow ((ap\ (ap\ (c_2EfcP_2EfcP_index \\
& A_27a\ A_27b)\ (ap\ (c_2EfcP_2EFCP\ A_27a\ A_27b)\ V0g))\ V1i) = (ap\ V0g \\
& V1i))))))
\end{aligned} \tag{99}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& (\forall V0f \in (A_27b^{A_27a}).((ap\ (ap\ (c_2Elist_2EMAP\ A_27a\ A_27b) \\
& V0f)\ (c_2Elist_2ENIL\ A_27a)) = (c_2Elist_2ENIL\ A_27b))) \wedge (\forall V1f \in \\
& (A_27b^{A_27a}).(\forall V2h \in A_27a.(\forall V3t \in (ty_2Elist_2Elist \\
& A_27a).((ap\ (ap\ (c_2Elist_2EMAP\ A_27a\ A_27b)\ V1f)\ (ap\ (ap\ (c_2Elist_2ECONS \\
& A_27a)\ V2h)\ V3t)) = (ap\ (ap\ (c_2Elist_2ECONS\ A_27b)\ (ap\ V1f\ V2h)) \\
& (ap\ (ap\ (c_2Elist_2EMAP\ A_27a\ A_27b)\ V1f)\ V3t)))))) \\
& \hspace{10em} (100)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& (\forall V0f \in ((A_27b^{A_27a})^{A_27b}).(\forall V1e \in A_27b.((ap\ (\\
& ap\ (ap\ (c_2Elist_2EFOLDL\ A_27a\ A_27b)\ V0f)\ V1e)\ (c_2Elist_2ENIL \\
& A_27a)) = V1e))) \wedge (\forall V2f \in ((A_27b^{A_27a})^{A_27b}).(\forall V3e \in \\
& A_27b.(\forall V4x \in A_27a.(\forall V5l \in (ty_2Elist_2Elist\ A_27a). \\
& ((ap\ (ap\ (ap\ (c_2Elist_2EFOLDL\ A_27a\ A_27b)\ V2f)\ V3e)\ (ap\ (ap\ (c_2Elist_2ECONS \\
& A_27a)\ V4x)\ V5l)) = (ap\ (ap\ (ap\ (c_2Elist_2EFOLDL\ A_27a\ A_27b)\ V2f) \\
& (ap\ (ap\ V2f\ V3e)\ V4x))\ V5l)))))) \\
& \hspace{10em} (101)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in (2^{(ty_2Elist_2Elist\ A_27a)}). \\
& (((p\ (ap\ V0P\ (c_2Elist_2ENIL\ A_27a))) \wedge (\forall V1t \in (ty_2Elist_2Elist \\
& A_27a).((p\ (ap\ V0P\ V1t)) \Rightarrow (\forall V2h \in A_27a.(p\ (ap\ V0P\ (ap\ (ap\ (\\
& c_2Elist_2ECONS\ A_27a)\ V2h)\ V1t)))))) \Rightarrow (\forall V3l \in (ty_2Elist_2Elist \\
& A_27a).(p\ (ap\ V0P\ V3l)))))) \\
& \hspace{10em} (102)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0l \in (ty_2Elist_2Elist\ A_27a).(\forall V1l_27 \in (ty_2Elist_2Elist \\
& A_27a).(\forall V2b \in A_27b.(\forall V3b_27 \in A_27b.(\forall V4f \in \\
& ((A_27b^{A_27a})^{A_27b}).(\forall V5f_27 \in ((A_27b^{A_27a})^{A_27b}). \\
& (((V0l = V1l_27) \wedge ((V2b = V3b_27) \wedge (\forall V6x \in A_27a.(\forall V7a \in \\
& A_27b.((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V6x)\ (ap\ (c_2Elist_2ELIST_TO_SET \\
& A_27a)\ V1l_27)))) \Rightarrow ((ap\ (ap\ V4f\ V7a)\ V6x) = (ap\ (ap\ V5f_27\ V7a)\ V6x)))))) \Rightarrow \\
& ((ap\ (ap\ (ap\ (c_2Elist_2EFOLDL\ A_27a\ A_27b)\ V4f)\ V2b)\ V0l) = (ap\ (\\
& ap\ (ap\ (c_2Elist_2EFOLDL\ A_27a\ A_27b)\ V5f_27)\ V3b_27)\ V1l_27)))))) \\
& \hspace{10em} (103)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow (\\
& \quad \forall V_0f \in ((A_{.27b}^{A_{.27a}})^{A_{.27b}}).(\forall V_1e \in A_{.27b}.(\forall V_2x \in \\
& \quad A_{.27a}.(\forall V_3l \in (ty_2Elist_2Elist\ A_{.27a}).((ap\ (ap\ (ap\ (c_2Elist_2EFOLDL \\
& \quad A_{.27a}\ A_{.27b})\ V_0f)\ V_1e)\ (ap\ (ap\ (c_2Elist_2ESNOC\ A_{.27a})\ V_2x)\ V_3l)) = \\
& \quad (ap\ (ap\ V_0f\ (ap\ (ap\ (ap\ (c_2Elist_2EFOLDL\ A_{.27a}\ A_{.27b})\ V_0f)\ V_1e)\ V_3l)) \\
& \quad \quad \quad V_2x)))))) \\
\end{aligned}
\tag{104}$$

Assume the following.

$$\begin{aligned}
& (\forall V_0a \in ty_2Enum_2Enum.(\forall V_1n \in ty_2Enum_2Enum.(\\
& \quad ((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ (ap\ c_2Earithmetic_2ENUMERAL \\
& \quad \quad (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO)))\ V_0a)) \wedge (\\
& \quad p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ c_2Enum_2E0)\ V_1n))) \Rightarrow ((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D \\
& \quad \quad (ap\ (ap\ c_2Earithmetic_2EEXP\ V_0a)\ (ap\ (ap\ c_2Elogroot_2ELOG\ V_0a) \\
& \quad \quad V_1n)))\ V_1n)) \wedge (p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V_1n)\ (ap\ (ap\ c_2Earithmetic_2EEXP \\
& \quad \quad V_0a)\ (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Elogroot_2ELOG\ V_0a)\ V_1n)))))))))) \\
\end{aligned}
\tag{105}$$

Assume the following.

$$\begin{aligned}
& (\forall V_0P \in (2^{ty_2Enum_2Enum}).(((p\ (ap\ V_0P\ c_2Enum_2E0)) \wedge \\
& (\forall V_1n \in ty_2Enum_2Enum.((p\ (ap\ V_0P\ V_1n)) \Rightarrow (p\ (ap\ V_0P\ (ap\ c_2Enum_2ESUC \\
& \quad V_1n)))))) \Rightarrow (\forall V_2n \in ty_2Enum_2Enum.(p\ (ap\ V_0P\ V_2n)))))) \\
\end{aligned}
\tag{106}$$

Assume the following.

$$\begin{aligned}
& ((\forall V0n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B \\
& \quad c_2Enum_2E0) V0n) = V0n)) \wedge ((\forall V1n \in ty_2Enum_2Enum.((ap \\
& \quad (ap c_2Earithmetic_2E_2B V1n) c_2Enum_2E0) = V1n)) \wedge ((\forall V2n \in \\
& \quad ty_2Enum_2Enum.(\forall V3m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B \\
& \quad (ap c_2Earithmetic_2ENUMERAL V2n)) (ap c_2Earithmetic_2ENUMERAL \\
& \quad V3m)) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Enumeral_2EiZ (ap \\
& \quad (ap c_2Earithmetic_2E_2B V2n) V3m)))))) \wedge ((\forall V4n \in ty_2Enum_2Enum. \\
& \quad ((ap (ap c_2Earithmetic_2E_2A c_2Enum_2E0) V4n) = c_2Enum_2E0)) \wedge \\
& \quad ((\forall V5n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A \\
& \quad V5n) c_2Enum_2E0) = c_2Enum_2E0)) \wedge ((\forall V6n \in ty_2Enum_2Enum. \\
& \quad (\forall V7m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A (\\
& \quad ap c_2Earithmetic_2ENUMERAL V6n)) (ap c_2Earithmetic_2ENUMERAL \\
& \quad V7m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2E_2A \\
& \quad V6n) V7m)))))) \wedge ((\forall V8n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D \\
& \quad c_2Enum_2E0) V8n) = c_2Enum_2E0)) \wedge ((\forall V9n \in ty_2Enum_2Enum. \\
& \quad ((ap (ap c_2Earithmetic_2E_2D V9n) c_2Enum_2E0) = V9n)) \wedge ((\forall V10n \in \\
& \quad ty_2Enum_2Enum.(\forall V11m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D \\
& \quad (ap c_2Earithmetic_2ENUMERAL V10n)) (ap c_2Earithmetic_2ENUMERAL \\
& \quad V11m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2E_2D \\
& \quad V10n) V11m)))))) \wedge ((\forall V12n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEXP \\
& \quad c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad V12n))) = c_2Enum_2E0)) \wedge ((\forall V13n \in ty_2Enum_2Enum.((ap \\
& \quad (ap c_2Earithmetic_2EEXP c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL \\
& \quad (ap c_2Earithmetic_2EBIT2 V13n))) = c_2Enum_2E0)) \wedge ((\forall V14n \in \\
& \quad ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEXP V14n) c_2Enum_2E0) = \\
& \quad (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))))) \wedge \\
& \quad ((\forall V15n \in ty_2Enum_2Enum.(\forall V16m \in ty_2Enum_2Enum. \\
& \quad ((ap (ap c_2Earithmetic_2EEXP (ap c_2Earithmetic_2ENUMERAL V15n)) \\
& \quad (ap c_2Earithmetic_2ENUMERAL V16m)) = (ap c_2Earithmetic_2ENUMERAL \\
& \quad (ap (ap c_2Earithmetic_2EEXP V15n) V16m)))))) \wedge ((ap c_2Enum_2ESUC \\
& \quad c_2Enum_2E0) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad c_2Earithmetic_2EZERO))) \wedge ((\forall V17n \in ty_2Enum_2Enum.(\\
& \quad (ap c_2Enum_2ESUC (ap c_2Earithmetic_2ENUMERAL V17n)) = (ap c_2Earithmetic_2ENUMERAL \\
& \quad (ap c_2Enum_2ESUC V17n)))))) \wedge ((ap c_2Eprim_rec_2EPRE c_2Enum_2E0) = \\
& \quad c_2Enum_2E0) \wedge ((\forall V18n \in ty_2Enum_2Enum.((ap c_2Eprim_rec_2EPRE \\
& \quad (ap c_2Earithmetic_2ENUMERAL V18n)) = (ap c_2Earithmetic_2ENUMERAL \\
& \quad (ap c_2Eprim_rec_2EPRE V18n)))))) \wedge ((\forall V19n \in ty_2Enum_2Enum. \\
& \quad (((ap c_2Earithmetic_2ENUMERAL V19n) = c_2Enum_2E0) \Leftrightarrow (V19n = c_2Earithmetic_2EZERO))) \wedge \\
& \quad ((\forall V20n \in ty_2Enum_2Enum.((c_2Enum_2E0 = (ap c_2Earithmetic_2ENUMERAL \\
& \quad V20n)) \Leftrightarrow (V20n = c_2Earithmetic_2EZERO))) \wedge ((\forall V21n \in ty_2Enum_2Enum. \\
& \quad (\forall V22m \in ty_2Enum_2Enum.(((ap c_2Earithmetic_2ENUMERAL \\
& \quad V21n) = (ap c_2Earithmetic_2ENUMERAL V22m)) \Leftrightarrow (V21n = V22m)))))) \wedge \\
& \quad ((\forall V23n \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C \\
& \quad V23n) c_2Enum_2E0)) \Leftrightarrow False)) \wedge ((\forall V24n \in ty_2Enum_2Enum. \\
& \quad ((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL \\
& \quad V24n))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) \\
& \quad V24n)))))) \wedge ((\forall V25n \in ty_2Enum_2Enum.(\forall V26m \in ty_2Enum_2Enum. \\
& \quad ((p (ap (ap c_2Eprim_rec_2E_3C (ap c_2Earithmetic_2ENUMERAL \\
& \quad V25n)) (ap c_2Earithmetic_2ENUMERAL V26m))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C \\
& \quad V25n) V26m)))))) \wedge ((\forall V27n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3E \\
& \quad c_2Enum_2E0) V27n)) \Leftrightarrow False)) \wedge ((\forall V28n \in ty_2Enum_2Enum. \\
& \quad ((p (ap (ap c_2Earithmetic_2E_3E (ap c_2Earithmetic_2ENUMERAL \\
& \quad V28n)) c_2Enum_2E0)) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) \\
& \quad V28n)))))) \wedge ((\forall V29n \in ty_2Enum_2Enum.(\forall V30m \in ty_2Enum_2Enum. \\
& \quad ((p (ap (ap c_2Earithmetic_2E_3E (ap c_2Earithmetic_2ENUMERAL \\
& \quad V29n)) (ap c_2Earithmetic_2ENUMERAL V30m))) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C \\
& \quad V30m) V29n)))))) \wedge ((\forall V31n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& \quad c_2Enum_2E0) V31n)) \Leftrightarrow True)) \wedge ((\forall V32n \in ty_2Enum_2Enum. \\
& \quad ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2ENUMERAL
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. (\\
& ((ap\ c_2Enumeral_2EiZ\ (ap\ (ap\ c_2Earithmetic_2E_2B\ c_2Earithmetic_2EZERO) \\
& V0n)) = V0n) \wedge (((ap\ c_2Enumeral_2EiZ\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& V0n)\ c_2Earithmetic_2EZERO)) = V0n) \wedge (((ap\ c_2Enumeral_2EiZ\ (\\
& ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT1\ V0n))\ (\\
& ap\ c_2Earithmetic_2EBIT1\ V1m))) = (ap\ c_2Earithmetic_2EBIT2\ (\\
& ap\ c_2Enumeral_2EiZ\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge \\
& (((ap\ c_2Enumeral_2EiZ\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT1 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT2\ V1m))) = (ap\ c_2Earithmetic_2EBIT1 \\
& (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge (\\
& ((ap\ c_2Enumeral_2EiZ\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT2 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT1\ V1m))) = (ap\ c_2Earithmetic_2EBIT1 \\
& (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge (\\
& ((ap\ c_2Enumeral_2EiZ\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT2 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT2\ V1m))) = (ap\ c_2Earithmetic_2EBIT2 \\
& (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge (\\
& ((ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ c_2Earithmetic_2EZERO) \\
& V0n)) = (ap\ c_2Enum_2ESUC\ V0n)) \wedge (((ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& V0n)\ c_2Earithmetic_2EZERO)) = (ap\ c_2Enum_2ESUC\ V0n)) \wedge (((ap \\
& c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT1 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT1\ V1m))) = (ap\ c_2Earithmetic_2EBIT1 \\
& (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge (\\
& ((ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT1 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT2\ V1m))) = (ap\ c_2Earithmetic_2EBIT2 \\
& (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge (\\
& ((ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT2 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT1\ V1m))) = (ap\ c_2Earithmetic_2EBIT2 \\
& (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge (\\
& ((ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT2 \\
& V0n))\ (ap\ c_2Earithmetic_2EBIT2\ V1m))) = (ap\ c_2Earithmetic_2EBIT1 \\
& (ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ V1m)))) \wedge \\
& (((ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B\ c_2Earithmetic_2EZERO) \\
& V0n)) = (ap\ c_2Enumeral_2EiiSUC\ V0n)) \wedge (((ap\ c_2Enumeral_2EiiSUC \\
& (ap\ (ap\ c_2Earithmetic_2E_2B\ V0n)\ c_2Earithmetic_2EZERO)) = (\\
& ap\ c_2Enumeral_2EiiSUC\ V0n)) \wedge (((ap\ c_2Enumeral_2EiiSUC\ (ap\ (\\
& ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Earithmetic_2EBIT1\ V0n))\ (ap\ c_2Earithmetic_2EBIT1 \\
& V1m))) = (ap\ c_2Earithmetic_2EBIT2\ (ap\ c_2Enum_2ESUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& V0n)\ V1m)))) \wedge (((ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& (ap\ c_2Earithmetic_2EBIT1\ V0n))\ (ap\ c_2Earithmetic_2EBIT2\ V1m))) = \\
& (ap\ c_2Earithmetic_2EBIT1\ (ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& V0n)\ V1m)))) \wedge (((ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& (ap\ c_2Earithmetic_2EBIT2\ V0n))\ (ap\ c_2Earithmetic_2EBIT1\ V1m))) = \\
& (ap\ c_2Earithmetic_2EBIT1\ (ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& V0n)\ V1m)))) \wedge (((ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& (ap\ c_2Earithmetic_2EBIT2\ V0n))\ (ap\ c_2Earithmetic_2EBIT2\ V1m))) = \\
& (ap\ c_2Earithmetic_2EBIT2\ (ap\ c_2Enumeral_2EiiSUC\ (ap\ (ap\ c_2Earithmetic_2E_2B \\
& V0n)\ V1m))
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. (\\
& ((p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) (ap c_2Earithmetic_2EBIT1 \\
& V0n))) \Leftrightarrow True) \wedge (((p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) \\
& (ap c_2Earithmetic_2EBIT2 V0n))) \Leftrightarrow True) \wedge (((p (ap (ap c_2Eprim_rec_2E_3C \\
& V0n) c_2Earithmetic_2EZERO)) \Leftrightarrow False) \wedge (((p (ap (ap c_2Eprim_rec_2E_3C \\
& (ap c_2Earithmetic_2EBIT1 V0n)) (ap c_2Earithmetic_2EBIT1 V1m))) \Leftrightarrow \\
& (p (ap (ap c_2Eprim_rec_2E_3C V0n) V1m))) \wedge (((p (ap (ap c_2Eprim_rec_2E_3C \\
& (ap c_2Earithmetic_2EBIT2 V0n)) (ap c_2Earithmetic_2EBIT2 V1m))) \Leftrightarrow \\
& (p (ap (ap c_2Eprim_rec_2E_3C V0n) V1m))) \wedge (((p (ap (ap c_2Eprim_rec_2E_3C \\
& (ap c_2Earithmetic_2EBIT1 V0n)) (ap c_2Earithmetic_2EBIT2 V1m))) \Leftrightarrow \\
& (\neg(p (ap (ap c_2Eprim_rec_2E_3C V1m) V0n)))) \wedge ((p (ap (ap c_2Eprim_rec_2E_3C \\
& (ap c_2Earithmetic_2EBIT2 V0n)) (ap c_2Earithmetic_2EBIT1 V1m))) \Leftrightarrow \\
& (p (ap (ap c_2Eprim_rec_2E_3C V0n) V1m))))))))))
\end{aligned} \tag{109}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. (\\
& ((p (ap (ap c_2Earithmetic_2E_3C_3D c_2Earithmetic_2EZERO) V0n)) \Leftrightarrow \\
& True) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT1 \\
& V0n)) c_2Earithmetic_2EZERO)) \Leftrightarrow False) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D \\
& (ap c_2Earithmetic_2EBIT2 V0n)) c_2Earithmetic_2EZERO)) \Leftrightarrow False) \wedge \\
& (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT1 \\
& V0n)) (ap c_2Earithmetic_2EBIT1 V1m))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V0n) V1m))) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT1 \\
& V0n)) (ap c_2Earithmetic_2EBIT2 V1m))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V0n) V1m))) \wedge (((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT2 \\
& V0n)) (ap c_2Earithmetic_2EBIT1 V1m))) \Leftrightarrow (\neg(p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V1m) V0n)))) \wedge ((p (ap (ap c_2Earithmetic_2E_3C_3D (ap c_2Earithmetic_2EBIT2 \\
& V0n)) (ap c_2Earithmetic_2EBIT2 V1m))) \Leftrightarrow (p (ap (ap c_2Earithmetic_2E_3C_3D \\
& V0n) V1m))))))))))
\end{aligned} \tag{110}$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum. (\neg(p (ap (ap c_2Eprim_rec_2E_3C V0n) V0n)))) \tag{111}$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum. (\neg(p (ap (ap c_2Eprim_rec_2E_3C V0n) c_2Enum_2E0)))) \tag{112}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& (p (ap (ap c_2Eprim_rec_2E_3C V0m) (ap c_2Enum_2ESUC V1n))) \Leftrightarrow (\\
& (V0m = V1n) \vee (p (ap (ap c_2Eprim_rec_2E_3C V0m) V1n))))))
\end{aligned} \tag{113}$$

Assume the following.

$$\begin{aligned}
& (((ap\ c_2Erich_list_2ECOUNT_LIST\ c_2Enum_2E0) = (c_2Elist_2ENIL \\
& ty_2Enum_2Enum)) \wedge (\forall V0n \in ty_2Enum_2Enum. ((ap\ c_2Erich_list_2ECOUNT_LIST \\
& (ap\ c_2Enum_2ESUC\ V0n)) = (ap\ (ap\ (c_2Elist_2ECONS\ ty_2Enum_2Enum) \\
& c_2Enum_2E0) (ap\ (ap\ (c_2Elist_2EMAP\ ty_2Enum_2Enum\ ty_2Enum_2Enum) \\
& c_2Enum_2ESUC) (ap\ c_2Erich_list_2ECOUNT_LIST\ V0n))))))
\end{aligned} \tag{114}$$

Assume the following.

$$\begin{aligned}
& (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\
& (p\ (ap\ (ap\ (c_2Ebool_2EIN\ ty_2Enum_2Enum)\ V0m)\ (ap\ (c_2Elist_2ELIST_TO_SET \\
& ty_2Enum_2Enum)\ (ap\ c_2Erich_list_2ECOUNT_LIST\ V1n)))) \Leftrightarrow (\\
& p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V0m)\ V1n))))
\end{aligned} \tag{115}$$

Assume the following.

$$\begin{aligned}
& (((ap\ c_2Erich_list_2ECOUNT_LIST\ c_2Enum_2E0) = (c_2Elist_2ENIL \\
& ty_2Enum_2Enum)) \wedge (\forall V0n \in ty_2Enum_2Enum. ((ap\ c_2Erich_list_2ECOUNT_LIST \\
& (ap\ c_2Enum_2ESUC\ V0n)) = (ap\ (ap\ (c_2Elist_2ESNOC\ ty_2Enum_2Enum) \\
& V0n)\ (ap\ c_2Erich_list_2ECOUNT_LIST\ V0n))))))
\end{aligned} \tag{116}$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \tag{117}$$

Assume the following.

$$(\forall V0A \in 2. ((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \tag{118}$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\
& (((p\ V0A) \Rightarrow False) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False))))))
\end{aligned} \tag{119}$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((\neg(p\ V0A)) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\
& ((p\ V0A) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False))))))
\end{aligned} \tag{120}$$

Assume the following.

$$(\forall V0A \in 2. (((\neg(p\ V0A)) \Rightarrow False) \Rightarrow ((p\ V0A) \Rightarrow False) \Rightarrow False)) \tag{121}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p\ V0p) \Leftrightarrow (\\
& (p\ V1q) \Leftrightarrow (p\ V2r))) \Leftrightarrow (((p\ V0p) \vee ((p\ V1q) \vee (p\ V2r))) \wedge (((p\ V0p) \vee ((\neg \\
& p\ V2r)) \vee (\neg(p\ V1q)))) \wedge (((p\ V1q) \vee ((\neg(p\ V2r)) \vee (\neg(p\ V0p)))) \wedge ((p\ V2r) \vee \\
& ((\neg(p\ V1q)) \vee (\neg(p\ V0p))))))))))
\end{aligned} \tag{122}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (\\
& (p V1q) \wedge (p V2r))) \Leftrightarrow (((p V0p) \vee (\neg(p V1q)) \vee (\neg(p V2r)))) \wedge (((p V1q) \vee \\
& (\neg(p V0p))) \wedge ((p V2r) \vee (\neg(p V0p))))))))))
\end{aligned} \tag{123}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (\\
& (p V1q) \vee (p V2r))) \Leftrightarrow (((p V0p) \vee (\neg(p V1q))) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge \\
& ((p V1q) \vee ((p V2r) \vee (\neg(p V0p))))))))))
\end{aligned} \tag{124}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (\\
& (p V1q) \Rightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge (\\
& (\neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p))))))))))
\end{aligned} \tag{125}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (((p V0p) \Leftrightarrow (\neg(p V1q))) \Leftrightarrow (((p V0p) \vee \\
& (p V1q)) \wedge ((\neg(p V1q)) \vee (\neg(p V0p))))))
\end{aligned} \tag{126}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (p V0p))) \tag{127}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (\neg(p V1q)))) \tag{128}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V0p)))) \tag{129}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V1q)))) \tag{130}$$

Assume the following.

$$(\forall V0p \in 2. ((\neg(\neg(p V0p))) \Rightarrow (p V0p))) \tag{131}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty A.27a \Rightarrow (p (ap (ap (ap c.2Eprim_rec.2E.3C c.2Enum.2E0) \\
& (ap (c.2Ewords.2Edimword A.27a) (c.2Ebool.2Ethe_value A.27a))))
\end{aligned} \tag{132}$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (p\ (ap\ (ap\ c.2Eprim_rec.2E_3C\ c.2Enum.2E0) \\ & (ap\ (c.2Efc2Edimindex\ A.27a)\ (c.2Ebool.2Ethe_value\ A.27a)))) \end{aligned} \quad (133)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (p\ (ap\ (ap\ c.2Eprim_rec.2E_3C\ (\\ & ap\ (c.2Efc2Edimindex\ A.27a)\ (c.2Ebool.2Ethe_value\ A.27a))) \\ & (ap\ (c.2Ewords.2Edimword\ A.27a)\ (c.2Ebool.2Ethe_value\ A.27a)))) \end{aligned} \quad (134)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0n \in ty.2Enum.2Enum. (\\ & (ap\ (c.2Ewords.2Ew2n\ A.27a)\ (ap\ (c.2Ewords.2En2w\ A.27a)\ V0n))) = \\ & (ap\ (ap\ c.2Earithmetic.2EMOD\ V0n)\ (ap\ (c.2Ewords.2Edimword\ A.27a) \\ & (c.2Ebool.2Ethe_value\ A.27a)))) \end{aligned} \quad (135)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0m \in ty.2Enum.2Enum. (\\ & \forall V1n \in ty.2Enum.2Enum. ((ap\ (c.2Ewords.2En2w\ A.27a)\ V0m) = \\ & (ap\ (c.2Ewords.2En2w\ A.27a)\ V1n)) \Leftrightarrow ((ap\ (ap\ c.2Earithmetic.2EMOD \\ & V0m)\ (ap\ (c.2Ewords.2Edimword\ A.27a)\ (c.2Ebool.2Ethe_value \\ & A.27a))) = (ap\ (ap\ c.2Earithmetic.2EMOD\ V1n)\ (ap\ (c.2Ewords.2Edimword \\ & A.27a)\ (c.2Ebool.2Ethe_value\ A.27a)))))) \end{aligned} \quad (136)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0w \in (ty.2Efc2Ecart \\ & 2\ A.27a). (\exists V1n \in ty.2Enum.2Enum. ((V0w = (ap\ (c.2Ewords.2En2w \\ & A.27a)\ V1n)) \wedge (p\ (ap\ (ap\ c.2Eprim_rec.2E_3C\ V1n)\ (ap\ (c.2Ewords.2Edimword \\ & A.27a)\ (c.2Ebool.2Ethe_value\ A.27a)))))) \end{aligned} \quad (137)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0i \in ty.2Enum.2Enum. (\\ & (p\ (ap\ (ap\ c.2Eprim_rec.2E_3C\ V0i)\ (ap\ (c.2Efc2Edimindex\ A.27a) \\ & (c.2Ebool.2Ethe_value\ A.27a)))) \Rightarrow (\neg (p\ (ap\ (ap\ (c.2Efc2Efc_index \\ & 2\ A.27a)\ (ap\ (c.2Ewords.2En2w\ A.27a)\ c.2Enum.2E0))\ V0i)))) \end{aligned} \quad (138)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0w \in (ty.2Efc2Ecart \\ & 2\ A.27a). ((ap\ (c.2Ewords.2Ew2w\ A.27a\ A.27a)\ V0w) = V0w)) \end{aligned} \quad (139)$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0h \in ty_2Enum_2Enum. (\\
& \quad \forall V1l \in ty_2Enum_2Enum. (\forall V2n \in ty_2Enum_2Enum. ((\\
& \quad \quad ap\ (ap\ (ap\ (c_2Ewords_2Eword_bits\ A_{.27a}\ V0h)\ V1l)\ (ap\ (c_2Ewords_2En2w \\
& \quad \quad \quad A_{.27a}\ V2n))) = (ap\ (c_2Ewords_2En2w\ A_{.27a})\ (ap\ (ap\ (ap\ c_2Ebit_2EBITS \\
& \quad \quad \quad \quad (ap\ (ap\ c_2Earithmetic_2EMIN\ V0h)\ (ap\ (ap\ c_2Earithmetic_2E_2D \\
& \quad \quad \quad \quad \quad (ap\ (c_2EfcP_2Edimindex\ A_{.27a})\ (c_2Ebool_2Ethe_value\ A_{.27a})))) \\
& \quad \quad \quad (ap\ c_2Earithmetic_2ENUMERAL\ (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO)))))) \\
& \quad \quad \quad V1l)\ V2n))))))
\end{aligned} \tag{140}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow (\\
& \quad \forall V0w \in (ty_2EfcP_2Ecart\ 2\ A_{.27a}). ((ap\ (c_2Ewords_2Ew2w \\
& \quad \quad A_{.27a}\ A_{.27b})\ V0w) = (ap\ (ap\ (ap\ (c_2Ewords_2Eword_extract\ A_{.27a} \\
& \quad \quad \quad A_{.27b})\ (ap\ (ap\ c_2Earithmetic_2E_2D\ (ap\ (c_2EfcP_2Edimindex\ A_{.27a}) \\
& \quad \quad \quad \quad (c_2Ebool_2Ethe_value\ A_{.27a}))))\ (ap\ c_2Earithmetic_2ENUMERAL \\
& \quad \quad \quad (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO))))\ c_2Enum_2E0 \\
& \quad \quad \quad V0w)))
\end{aligned} \tag{141}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0h \in ty_2Enum_2Enum. (\\
& \quad \forall V1l \in ty_2Enum_2Enum. (\forall V2w \in (ty_2EfcP_2Ecart\ 2 \\
& \quad \quad A_{.27a}). ((ap\ (ap\ (ap\ (c_2Ewords_2Eword_bits\ A_{.27a})\ V0h)\ V1l)\ V2w) = \\
& \quad \quad \quad (ap\ (ap\ (ap\ (c_2Ewords_2Eword_extract\ A_{.27a}\ A_{.27a})\ V0h)\ V1l)\ V2w))))))
\end{aligned} \tag{142}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow (\\
& \quad \forall V0h \in ty_2Enum_2Enum. (\forall V1l \in ty_2Enum_2Enum. (\forall V2w \in \\
& \quad \quad (ty_2EfcP_2Ecart\ 2\ A_{.27a}). ((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V0h) \\
& \quad \quad \quad V1l)) \Rightarrow ((ap\ (ap\ (ap\ (c_2Ewords_2Eword_extract\ A_{.27a}\ A_{.27b})\ V0h) \\
& \quad \quad \quad \quad V1l)\ V2w) = (ap\ (c_2Ewords_2En2w\ A_{.27b})\ c_2Enum_2E0))))))
\end{aligned} \tag{143}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0w \in (ty_2EfcP_2Ecart \\
& \quad 2\ A_{.27a}). (\forall V1h \in ty_2Enum_2Enum. ((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D \\
& \quad \quad (ap\ (ap\ c_2Earithmetic_2E_2D\ (ap\ (c_2EfcP_2Edimindex\ A_{.27a})\ (\\
& \quad \quad \quad c_2Ebool_2Ethe_value\ A_{.27a}))))\ (ap\ c_2Earithmetic_2ENUMERAL \\
& \quad \quad \quad (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO))))\ V1h)) \Rightarrow \\
& \quad \quad \quad ((ap\ (ap\ (ap\ (c_2Ewords_2Eword_bits\ A_{.27a})\ V1h)\ c_2Enum_2E0) \\
& \quad \quad \quad \quad V0w) = V0w))))
\end{aligned} \tag{144}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0h \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. (\forall V2m_27 \in \\
& \quad ty_2Enum_2Enum. (\forall V3l \in ty_2Enum_2Enum. (\forall V4s \in ty_2Enum_2Enum. \\
& \quad (\forall V5w \in (ty_2Efc_2Ecart\ 2\ A_27a). ((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D \\
& \quad V3l)\ V1m)) \wedge ((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V2m_27)\ V0h)) \wedge \\
& \quad ((V2m_27 = (ap\ (ap\ c_2Earithmetic_2E_2B\ V1m)\ (ap\ c_2Earithmetic_2ENUMERAL \\
& \quad (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO)))) \wedge (V4s = \\
& \quad (ap\ (ap\ c_2Earithmetic_2E_2D\ V2m_27)\ V3l)))))) \Rightarrow ((ap\ (ap\ (c_2Ewords_2Eword_add \\
& \quad A_27b)\ (ap\ (ap\ (c_2Ewords_2Eword_lsl\ A_27b)\ (ap\ (ap\ (ap\ (c_2Ewords_2Eword_extract \\
& \quad A_27a\ A_27b)\ V0h)\ V2m_27)\ V5w))\ V4s))\ (ap\ (ap\ (ap\ (c_2Ewords_2Eword_extract \\
& \quad A_27a\ A_27b)\ V1m)\ V3l)\ V5w)) = (ap\ (ap\ (ap\ (c_2Ewords_2Eword_extract \\
& \quad A_27a\ A_27b)\ (ap\ (ap\ c_2Earithmetic_2EMIN\ V0h)\ (ap\ (ap\ c_2Earithmetic_2EMIN \\
& \quad (ap\ (ap\ c_2Earithmetic_2E_2D\ (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap \\
& \quad (c_2Efc_2Edimindex\ A_27b)\ (c_2Ebool_2Ethe_value\ A_27b)))) \\
& \quad V3l))\ (ap\ c_2Earithmetic_2ENUMERAL\ (ap\ c_2Earithmetic_2EBIT1 \\
& \quad c_2Earithmetic_2EZERO))))\ (ap\ (ap\ c_2Earithmetic_2E_2D\ (ap\ (\\
& \quad c_2Efc_2Edimindex\ A_27a)\ (c_2Ebool_2Ethe_value\ A_27a)))\ (\\
& \quad ap\ c_2Earithmetic_2ENUMERAL\ (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO)))))) \\
& \quad V3l)\ V5w))))))))) \\
& \hspace{15em} (145)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow ((\forall V0w \in (ty_2Efc_2Ecart \\
& \quad 2\ A_27a). ((ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ V0w)\ (ap\ (c_2Ewords_2En2w \\
& \quad A_27a)\ c_2Enum_2E0)) = V0w)) \wedge (\forall V1w \in (ty_2Efc_2Ecart\ 2 \\
& \quad A_27a). ((ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ (ap\ (c_2Ewords_2En2w \\
& \quad A_27a)\ c_2Enum_2E0))\ V1w) = V1w))) \\
& \hspace{15em} (146)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0v \in (ty_2Efc_2Ecart \\
& \quad 2\ A_27a). (\forall V1w \in (ty_2Efc_2Ecart\ 2\ A_27a). ((ap\ (ap\ (c_2Ewords_2Eword_add \\
& \quad A_27a)\ V0v)\ V1w) = (ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ V1w)\ V0v)))) \\
& \hspace{15em} (147)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow ((\forall V0n \in ty_2Enum_2Enum. \\
& ((ap\ (ap\ (c_2Ewords_2Eword_lsl\ A.27a)\ (ap\ (c_2Ewords_2En2w\ A.27a)\ \\
& c_2Enum_2E0))\ V0n) = (ap\ (c_2Ewords_2En2w\ A.27a)\ c_2Enum_2E0))) \wedge \\
& ((\forall V1n \in ty_2Enum_2Enum. ((ap\ (ap\ (c_2Ewords_2Eword_asr\ \\
& A.27a)\ (ap\ (c_2Ewords_2En2w\ A.27a)\ c_2Enum_2E0))\ V1n) = (ap\ (c_2Ewords_2En2w\ \\
& A.27a)\ c_2Enum_2E0))) \wedge ((\forall V2n \in ty_2Enum_2Enum. ((ap\ (ap\ \\
& (c_2Ewords_2Eword_lsr\ A.27a)\ (ap\ (c_2Ewords_2En2w\ A.27a)\ c_2Enum_2E0))\ \\
& V2n) = (ap\ (c_2Ewords_2En2w\ A.27a)\ c_2Enum_2E0))) \wedge ((\forall V3n \in \\
& ty_2Enum_2Enum. ((ap\ (ap\ (c_2Ewords_2Eword_rol\ A.27a)\ (ap\ (c_2Ewords_2En2w\ \\
& A.27a)\ c_2Enum_2E0))\ V3n) = (ap\ (c_2Ewords_2En2w\ A.27a)\ c_2Enum_2E0))) \wedge \\
& ((\forall V4n \in ty_2Enum_2Enum. ((ap\ (ap\ (c_2Ewords_2Eword_ror\ \\
& A.27a)\ (ap\ (c_2Ewords_2En2w\ A.27a)\ c_2Enum_2E0))\ V4n) = (ap\ (c_2Ewords_2En2w\ \\
& A.27a)\ c_2Enum_2E0))))))
\end{aligned}$$

(148)

Theorem 1

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0w \in (ty_2Efc_2Ecart \\
& 2 A_{27a}). (\forall V1m \in (ty_2Efc_2Ecart 2 A_{27a}). ((ap (ap (c_2Ewords_2Eword_lsl_bv \\
& A_{27a}) V0w) V1m) = (ap (ap (ap (c_2Ebool_2ECOND (ty_2Efc_2Ecart \\
& 2 A_{27a}) (ap (ap (c_2Emin_2E_3D ty_2Enum_2Enum) (ap (c_2Efc_2Edimindex \\
& A_{27a}) (c_2Ebool_2Ethe_value A_{27a}))) (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) (ap (c_2Efc_2EFCP \\
& 2 A_{27a}) (ap (c_2Ecombin_2EK 2 ty_2Enum_2Enum) (ap (ap c_2Ebool_2E_2F_5C \\
& (ap c_2Ebool_2E_7E (ap (ap (c_2Efc_2Efc_index 2 A_{27a}) V1m) \\
& c_2Enum_2E0))) (ap (ap (c_2Efc_2Efc_index 2 A_{27a}) V0w) c_2Enum_2E0)))))) \\
& (ap (c_2Efc_2EFCP 2 A_{27a}) (\lambda V2k \in ty_2Enum_2Enum. (ap (ap \\
& c_2Ebool_2E_2F_5C (ap (ap (ap (c_2Elist_2EFOLDL ty_2Enum_2Enum \\
& 2) (\lambda V3a \in 2. (\lambda V4j \in ty_2Enum_2Enum. (ap (ap c_2Ebool_2E_5C_2F \\
& V3a) (ap (ap c_2Ebool_2E_2F_5C (ap (ap (c_2Emin_2E_3D (ty_2Efc_2Ecart \\
& 2 A_{27a}) (ap (ap (ap (c_2Ewords_2Eword_bits A_{27a}) (ap c_2Ebit_2ELOG2 \\
& (ap (ap c_2Earithmetic_2E_2D (ap (c_2Efc_2Edimindex A_{27a}) (\\
& c_2Ebool_2Ethe_value A_{27a}))) (ap c_2Earithmetic_2ENUMERAL \\
& (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))))) c_2Enum_2E0) \\
& V1m)) (ap (c_2Ewords_2En2w A_{27a}) V4j))) (ap (ap c_2Ebool_2E_2F_5C \\
& (ap (ap c_2Earithmetic_2E_3C_3D V4j) V2k)) (ap (ap (c_2Efc_2Efc_index \\
& 2 A_{27a}) V0w) (ap (ap c_2Earithmetic_2E_2D V2k) V4j)))))) c_2Ebool_2EF \\
& (ap c_2Erich_list_2ECOUNT_LIST (ap (c_2Efc_2Edimindex A_{27a}) \\
& (c_2Ebool_2Ethe_value A_{27a})))) (ap (ap (c_2Emin_2E_3D (ty_2Efc_2Ecart \\
& 2 A_{27a}) (ap (ap (ap (c_2Ewords_2Eword_bits A_{27a}) (ap (ap c_2Earithmetic_2E_2D \\
& (ap (c_2Efc_2Edimindex A_{27a}) (c_2Ebool_2Ethe_value A_{27a}))) \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) \\
& (ap (ap c_2Earithmetic_2E_2B (ap c_2Ebit_2ELOG2 (ap (ap c_2Earithmetic_2E_2D \\
& (ap (c_2Efc_2Edimindex A_{27a}) (c_2Ebool_2Ethe_value A_{27a}))) \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))))) \\
& (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) \\
& V1m)) (ap (c_2Ewords_2En2w A_{27a}) c_2Enum_2E0))))))
\end{aligned}$$