





**Definition 22** We define  $c\_2Esum\_2EINR$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0e \in A\_27b.(ap (c\_2Esum\_2EABS$

**Definition 23** We define  $c\_2Esum\_2EINL$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0e \in A\_27a.(ap (c\_2Esum\_2EABS$

Let  $c\_2Esum\_2E\_2B\_2B : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow \forall A\_27c. \\ & nonempty\ A\_27c \Rightarrow \forall A\_27d.nonempty\ A\_27d \Rightarrow c\_2Esum\_2E\_2B\_2B \\ & A\_27a\ A\_27b\ A\_27c\ A\_27d \in (((ty\_2Esum\_2Esum\ A\_27c\ A\_27d)^{(ty\_2Esum\_2Esum\ A\_27a\ A\_27b)})(A\_27d^{A\_27b})) \end{aligned} \quad (11)$$

Assume the following.

$$True \quad (12)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p\ V0t1) \Rightarrow (p\ V1t2)) \Rightarrow ((p \\ & V1t2) \Rightarrow (p\ V0t1)) \Rightarrow ((p\ V0t1) \Leftrightarrow (p\ V1t2)))))) \end{aligned} \quad (13)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p\ V0t))) \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in \\ & A\_27a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (16)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow \\ & True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (( \\ & (p\ V0t) \Rightarrow False) \Leftrightarrow \neg(p\ V0t)))))) \end{aligned} \quad (17)$$

Assume the following.

$$\begin{aligned} & ((\forall V0t \in 2.((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t)) \wedge (((\neg True) \Leftrightarrow False) \wedge \\ & ((\neg False) \Leftrightarrow True))) \end{aligned} \quad (18)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow \\ & True)) \end{aligned} \quad (19)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.(\forall V1y \in \\ & A\_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \end{aligned} \quad (20)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow (p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (21)$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1x_{.27} \in 2.(\forall V2y \in 2.(\forall V3y_{.27} \in 2.(((p V0x) \Leftrightarrow (p V1x_{.27})) \wedge ((p V1x_{.27}) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_{.27})))))) \Rightarrow ((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_{.27}) \Rightarrow (p V3y_{.27})))))) \quad (22)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow (\forall V0x \in A_{.27a}.((ap (c_{.2}Ecombin_{.2}EI A_{.27a}) V0x) = V0x)) \quad (23)$$

Assume the following.

$$(\forall V0n \in ty_{.2}Enum_{.2}Enum.(\neg((ap c_{.2}Enum_{.2}ESUC V0n) = c_{.2}Enum_{.2}E0))) \quad (24)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow ((\neg(p (ap (c_{.2}Epred_{.set}_{.2}EFINITE A_{.27a}) (c_{.2}Epred_{.set}_{.2}EUNIV A_{.27a})))) \Leftrightarrow (\exists V0f \in (A_{.27a}^{A_{.27a}}).((\forall V1x \in A_{.27a}.(\forall V2y \in A_{.27a}.(((ap V0f V1x) = (ap V0f V2y)) \Rightarrow (V1x = V2y)))) \wedge (\exists V3y \in A_{.27a}.(\forall V4x \in A_{.27a}.(\neg((ap V0f V4x) = V3y)))))))))) \quad (25)$$

Assume the following.

$$(\forall V0m \in ty_{.2}Enum_{.2}Enum.(\forall V1n \in ty_{.2}Enum_{.2}Enum.((ap c_{.2}Enum_{.2}ESUC V0m) = (ap c_{.2}Enum_{.2}ESUC V1n)) \Leftrightarrow (V0m = V1n))) \quad (26)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow \forall A_{.27b}.nonempty A_{.27b} \Rightarrow ((\forall V0y \in A_{.27a}.(\forall V1x \in A_{.27a}.(((ap (c_{.2}Esum_{.2}EINL A_{.27a} A_{.27b}) V0y) \Leftrightarrow (V1x = V0y)))) \wedge (\forall V2y \in A_{.27b}.(\forall V3x \in A_{.27b}.(((ap (c_{.2}Esum_{.2}EINR A_{.27a} A_{.27b}) V2y) \Leftrightarrow (V3x = V2y)))))) \quad (27)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow \forall A_{.27b}.nonempty A_{.27b} \Rightarrow ((\forall V0P \in (2^{(ty_{.2}Esum_{.2}Esum A_{.27a} A_{.27b})}).((\forall V1s \in (ty_{.2}Esum_{.2}Esum A_{.27a} A_{.27b}).(p (ap V0P V1s)) \Leftrightarrow ((\forall V2x \in A_{.27a}.(p (ap V0P (ap (c_{.2}Esum_{.2}EINL A_{.27a} A_{.27b}) V2x)))) \wedge (\forall V3y \in A_{.27b}.(p (ap V0P (ap (c_{.2}Esum_{.2}EINR A_{.27a} A_{.27b}) V3y)))))))))) \quad (28)$$

Assume the following.

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow ( \\ & \forall V0x \in A.27a. (\forall V1y \in A.27b. (\neg((ap\ (c.2Esum\_2EINL \\ & A.27a\ A.27b)\ V0x) = (ap\ (c.2Esum\_2EINR\ A.27a\ A.27b)\ V1y)))))) \end{aligned} \quad (29)$$

Assume the following.

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow \forall A.27c. \\ & nonempty\ A.27c \Rightarrow \forall A.27d.nonempty\ A.27d \Rightarrow ((\forall V0f \in ( \\ & A.27c^{A.27a}). (\forall V1g \in (A.27d^{A.27b}). (\forall V2a \in A.27a. \\ & ((ap\ (ap\ (ap\ (c.2Esum\_2E\_2B\_2B\ A.27a\ A.27b\ A.27c\ A.27d)\ V0f)\ V1g) \\ & (ap\ (c.2Esum\_2EINL\ A.27a\ A.27b)\ V2a)) = (ap\ (c.2Esum\_2EINL\ A.27c \\ & A.27d)\ (ap\ V0f\ V2a)))))) \wedge (\forall V3f \in (A.27c^{A.27a}). (\forall V4g \in \\ & (A.27d^{A.27b}). (\forall V5b \in A.27b. ((ap\ (ap\ (ap\ (c.2Esum\_2E\_2B\_2B \\ & A.27a\ A.27b\ A.27c\ A.27d)\ V3f)\ V4g)\ (ap\ (c.2Esum\_2EINR\ A.27a\ A.27b) \\ & V5b)) = (ap\ (c.2Esum\_2EINR\ A.27c\ A.27d)\ (ap\ V4g\ V5b)))))) \end{aligned} \quad (30)$$

**Theorem 1**

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow (\neg(p\ (ap\ (c.2Epred\_set\_2EFINITE \\ & (ty\_2Esum\_2Esum\ ty\_2Enum\_2Enum\ A.27a))\ (c.2Epred\_set\_2EUNIV \\ & (ty\_2Esum\_2Esum\ ty\_2Enum\_2Enum\ A.27a)))))) \end{aligned}$$