

thm\_2Ecombin\_2EMONOID\_\_CONJ\_\_T  
(TMZg8WxQyU3LUVpzm6zhoNjuBE2cBcxmEdo)

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**Definition 1** We define `c_2Emin_2E_3D` to be  $\lambda A. \lambda x \in A. \lambda y \in A. inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 2** We define `c_2Ebool_2ET` to be  $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

**Definition 3** We define `c_2Ebool_2E_21` to be  $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap (ap (c_2Emin_2E_3D (2^{A_27a}))$

**Definition 4** We define `c_2Ebool_2EF` to be  $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$ .

**Definition 5** We define `c_2Ecombin_2ELEFT_ID` to be  $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in ((A_27b^{A_27b})^{A_27a}). \lambda$

**Definition 6** We define `c_2Ecombin_2ERIGHT_ID` to be  $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in ((A_27a^{A_27b})^{A_27a}). \lambda$

**Definition 7** We define `c_2Ecombin_2EASSOC` to be  $\lambda A_27a : \iota. \lambda V0f \in ((A_27a^{A_27a})^{A_27a}). (ap (c_2Ebool$

**Definition 8** We define `c_2Emin_2E_3D_3D_3E` to be  $\lambda P \in 2. \lambda Q \in 2. inj\_o (p P \Rightarrow p Q)$  of type  $\iota$ .

**Definition 9** We define `c_2Ebool_2E_2F_5C` to be  $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2$

**Definition 10** We define `c_2Ecombin_2EMONOID` to be  $\lambda A_27a : \iota. \lambda V0f \in ((A_27a^{A_27a})^{A_27a}). \lambda V1e \in A$

Assume the following.

$$True \tag{1}$$

Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_27a. (p V0t)) \Leftrightarrow (p V0t))) \tag{2}$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p V0t1) \wedge ((p V1t2) \wedge (p V2t3)))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \wedge (p V2t3)))))) \tag{3}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0t \in 2.(((True \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \wedge True) \Leftrightarrow \\
 & (p \ V0t)) \wedge (((False \wedge (p \ V0t)) \Leftrightarrow False) \wedge (((p \ V0t) \wedge False) \Leftrightarrow False) \wedge \\
 & (((p \ V0t) \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)))))) \quad (4)
 \end{aligned}$$

Assume the following.

$$\forall A\_27a.nonempty \ A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow True)) \quad (5)$$

**Theorem 1**  $(p \ (ap \ (ap \ (c\_2Ecombin\_2EMONOID \ 2) \ c\_2Ebool\_2E\_2F\_5C) \ c\_2Ebool\_2ET))$ .