

# thm\_2Efinite\_map\_2EDRESTRICT\_FUNION\_SUBSET (TMKPYzw4fjytBuNYzjhVjLpuu3vcxErav8E)

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**Definition 1** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A.$ if  $(\exists x \in A.p (ap P x))$  **then** (the  $(\lambda x.x \in A \wedge p x)$  of type  $\iota \Rightarrow \iota$ ).

**Definition 2** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define  $c\_2Ebool\_2E\_3F$  to be  $\lambda A.\lambda P \in (2^{A-27a}).(ap V0P (ap (c\_2Emin\_2E\_40 A P)))$

**Definition 4** We define  $c\_2Ebool\_2E\_2T$  to be  $(ap (ap (c\_2Emin\_2E\_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

**Definition 5** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.\lambda P \in (2^{A-27a}).(ap (ap (c\_2Emin\_2E\_3D (2^{A-27a}) P)))$

**Definition 6** We define  $c\_2Ebool\_2E\_2F$  to be  $(ap (c\_2Ebool\_2E\_21 2) (\lambda V0t \in 2.V0t))$ .

**Definition 7** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p P \Rightarrow p Q)$  of type  $\iota$ .

**Definition 8** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2.(ap (ap c\_2Emin\_2E\_3D\_3D\_3E V0t) c\_2Ebool\_2E\_2F))$

Let  $ty\_2Eone\_2Eone : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Eone\_2Eone \tag{1}$$

**Definition 9** We define  $c\_2Eone\_2Eone$  to be  $(ap (c\_2Emin\_2E\_40 ty\_2Eone\_2Eone) (\lambda V0x \in ty\_2Eone\_2Eone.V0x))$

**Definition 10** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in 2.V2t)))$

Let  $ty\_2Esum\_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty\_2Esum\_2Esum\ A0\ A1) \tag{2}$$

Let  $c\_2Esum\_2EABS\_sum : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Esum\_2EABS\_sum\ A\_27a\ A\_27b \in ((ty\_2Esum\_2Esum\ A\_27a\ A\_27b)^{((2^{A-27b})^{A-27a})^2}) \tag{3}$$

**Definition 11** We define  $c\_2Esum\_2EINR$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0e \in A\_27b. (ap (c\_2Esum\_2EABS$

Let  $ty\_2Efinite\_map\_2Efmap : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty\_2Efinite\_map\_2Efmap A0 A1) \quad (4)$$

Let  $c\_2Efinite\_map\_2Efmap\_ABS : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Efinite\_map\_2Efmap\_ABS A\_27a A\_27b \in ((ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)^{(ty\_2Esum\_2Esum A\_27b ty\_2Eone\_2Eone)^{A\_27a}}) \quad (5)$$

**Definition 12** We define  $c\_2Efinite\_map\_2EFEMPTY$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. (ap (c\_2Efinite\_map\_2E$

Let  $c\_2Efinite\_map\_2EDRESTRICT : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Efinite\_map\_2EDRESTRICT A\_27a A\_27b \in (((ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)^{(2^{A\_27a}}))^{(ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)}) \quad (6)$$

**Definition 13** We define  $c\_2Ebool\_2ECOND$  to be  $\lambda A\_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A\_27a. (\lambda V2t2 \in A\_27a. ($

Let  $c\_2Efinite\_map\_2Efmap\_REP : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Efinite\_map\_2Efmap\_REP A\_27a A\_27b \in (((ty\_2Esum\_2Esum A\_27b ty\_2Eone\_2Eone)^{A\_27a})^{(ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)}) \quad (7)$$

Let  $c\_2Esum\_2EOUTL : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Esum\_2EOUTL A\_27a A\_27b \in (A\_27a^{(ty\_2Esum\_2Esum A\_27a A\_27b)}) \quad (8)$$

**Definition 14** We define  $c\_2Efinite\_map\_2EFAPPLY$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (ty\_2Efinite\_map$

Let  $c\_2Esum\_2EISL : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Esum\_2EISL A\_27a A\_27b \in (2^{(ty\_2Esum\_2Esum A\_27a A\_27b)}) \quad (9)$$

**Definition 15** We define  $c\_2Efinite\_map\_2EFDOM$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (ty\_2Efinite\_map$

Let  $c\_2Efinite\_map\_2EFUNION : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Efinite\_map\_2EFUNION A\_27a A\_27b \in (((ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)^{(ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)})^{(ty\_2Efinite\_map\_2Efmap A\_27a A\_27b)}) \quad (10)$$

**Definition 16** We define  $c\_2Ebool\_2EIN$  to be  $\lambda A\_27a : \iota. (\lambda V0x \in A\_27a. (\lambda V1f \in (2^{A\_27a}). (ap\ V1f\ V0x)))$

**Definition 17** We define  $c\_2Efinite\_map\_2ESUBMAP$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (ty\_2Efinite\_map\ A\_27a\ A\_27b). (\lambda V1g \in (2^{A\_27b}). (ap\ V1g\ (V0f\ V1g)))$

**Definition 18** We define  $c\_2Epred\_set\_2ESUBSET$  to be  $\lambda A\_27a : \iota. \lambda V0s \in (2^{A\_27a}). \lambda V1t \in (2^{A\_27a}). (ap\ (c\_2Ebool\_2E21\ 2)\ (\lambda V2t \in (2^{A\_27a}). (V0s\ V2t)))$

**Definition 19** We define  $c\_2Ebool\_2E\_5C\_2F$  to be  $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap\ (c\_2Ebool\_2E\_21\ 2)\ (\lambda V2t \in 2. (V0t1\ V2t))))$

Let  $ty\_2Epair\_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty\_2Epair\_2Eprod\ A0\ A1) \quad (11)$$

Let  $c\_2Epair\_2EABS\_prod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epair\_2EABS\_prod\ A\_27a\ A\_27b \in ((ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)^{(2^{A\_27b})^{A\_27a}}) \quad (12)$$

**Definition 20** We define  $c\_2Epair\_2E\_2C$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0x \in A\_27a. \lambda V1y \in A\_27b. (ap\ (c\_2Ebool\_2E\_5C\_2F)\ (V0x\ V1y))$

Let  $c\_2Epred\_set\_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epred\_set\_2EGSPEC\ A\_27a\ A\_27b \in ((2^{A\_27a})^{(ty\_2Epair\_2Eprod\ A\_27a\ 2)^{A\_27b}}) \quad (13)$$

**Definition 21** We define  $c\_2Epred\_set\_2EUNION$  to be  $\lambda A\_27a : \iota. \lambda V0s \in (2^{A\_27a}). \lambda V1t \in (2^{A\_27a}). (ap\ (c\_2Ebool\_2E\_5C\_2F)\ (V0s\ V1t))$

**Definition 22** We define  $c\_2Epred\_set\_2EINTER$  to be  $\lambda A\_27a : \iota. \lambda V0s \in (2^{A\_27a}). \lambda V1t \in (2^{A\_27a}). (ap\ (c\_2Ebool\_2E\_5C\_2F)\ (V0s\ V1t))$

Assume the following.

$$True \quad (14)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \vee (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \vee True) \Leftrightarrow True) \wedge \\ & (((False \vee (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \vee False) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \vee \\ & (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (16)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (17)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. (\forall V1y \in A\_27a. ((V0x = V1y) \Rightarrow (V1y = V0x)))) \quad (18)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. (\forall V1y \in A\_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (19)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg( \\ & p\ V0t)))))) \end{aligned} \quad (20)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow \\ & ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \end{aligned} \quad (21)$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in 2. (\forall V1x\_27 \in 2. (\forall V2y \in 2. (\forall V3y\_27 \in \\ & 2. (((p\ V0x) \Leftrightarrow (p\ V1x\_27)) \wedge ((p\ V1x\_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y\_27)))) \Rightarrow \\ & (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x\_27) \Rightarrow (p\ V3y\_27)))))) \end{aligned} \quad (22)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in 2. (\forall V1Q \in 2. \\ & (\forall V2x \in A\_27a. (\forall V3x\_27 \in A\_27a. (\forall V4y \in A\_27a. \\ & (\forall V5y\_27 \in A\_27a. (((p\ V0P) \Leftrightarrow (p\ V1Q)) \wedge ((p\ V1Q) \Rightarrow (V2x = V3x\_27)) \wedge \\ & ((\neg(p\ V1Q)) \Rightarrow (V4y = V5y\_27)))) \Rightarrow ((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a) \\ & V0P)\ V2x)\ V4y) = (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ V1Q)\ V3x\_27 \\ & V5y\_27)))))) \end{aligned} \quad (23)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow ((\forall V0t1 \in A\_27a. (\forall V1t2 \in \\ & A\_27a. ((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ c\_2Ebool\_2ET)\ V0t1) \\ & V1t2) = V0t1))) \wedge (\forall V2t1 \in A\_27a. (\forall V3t2 \in A\_27a. ((ap \\ & (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ c\_2Ebool\_2EF)\ V2t1)\ V3t2) = V3t2)))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow ( \\
& \quad \forall V0f \in (ty\_2Efinite\_map\_2E fmap\ A_{.27a}\ A_{.27b}).(\forall V1r \in \\
& \quad (2^{A_{.27a}}).(((ap\ (c\_2Efinite\_map\_2EFDOM\ A_{.27a}\ A_{.27b})\ (ap\ (ap \\
& \quad (c\_2Efinite\_map\_2EDRESTRICT\ A_{.27a}\ A_{.27b})\ V0f)\ V1r))) = (ap\ (ap \\
& \quad (c\_2Epred\_set\_2EINTER\ A_{.27a})\ (ap\ (c\_2Efinite\_map\_2EFDOM\ A_{.27a} \\
& \quad A_{.27b})\ V0f))\ V1r)) \wedge (\forall V2x \in A_{.27a}.((ap\ (ap\ (c\_2Efinite\_map\_2EFAPPLY \\
& \quad A_{.27a}\ A_{.27b})\ (ap\ (ap\ (c\_2Efinite\_map\_2EDRESTRICT\ A_{.27a}\ A_{.27b}) \\
& \quad V0f)\ V1r))\ V2x) = (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A_{.27b})\ (ap\ (ap\ (c\_2Ebool\_2EIN \\
& \quad A_{.27a})\ V2x)\ (ap\ (ap\ (c\_2Epred\_set\_2EINTER\ A_{.27a})\ (ap\ (c\_2Efinite\_map\_2EFDOM \\
& \quad A_{.27a}\ A_{.27b})\ V0f))\ V1r)))\ (ap\ (ap\ (c\_2Efinite\_map\_2EFAPPLY\ A_{.27a} \\
& \quad A_{.27b})\ V0f)\ V2x))\ (ap\ (ap\ (c\_2Efinite\_map\_2EFAPPLY\ A_{.27a}\ A_{.27b}) \\
& \quad (c\_2Efinite\_map\_2EFEMPTY\ A_{.27a}\ A_{.27b}))\ V2x)))))) \\
& \hspace{15em} (25)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow ( \\
& \quad \forall V0f \in (ty\_2Efinite\_map\_2E fmap\ A_{.27a}\ A_{.27b}).(\forall V1g \in \\
& \quad (ty\_2Efinite\_map\_2E fmap\ A_{.27a}\ A_{.27b}).(((ap\ (c\_2Efinite\_map\_2EFDOM \\
& \quad A_{.27a}\ A_{.27b})\ (ap\ (ap\ (c\_2Efinite\_map\_2EFUNION\ A_{.27a}\ A_{.27b})\ V0f) \\
& \quad V1g))) = (ap\ (ap\ (c\_2Epred\_set\_2EUNION\ A_{.27a})\ (ap\ (c\_2Efinite\_map\_2EFDOM \\
& \quad A_{.27a}\ A_{.27b})\ V0f))\ (ap\ (c\_2Efinite\_map\_2EFDOM\ A_{.27a}\ A_{.27b})\ V1g))) \wedge \\
& \quad (\forall V2x \in A_{.27a}.((ap\ (ap\ (c\_2Efinite\_map\_2EFAPPLY\ A_{.27a} \\
& \quad A_{.27b})\ (ap\ (ap\ (c\_2Efinite\_map\_2EFUNION\ A_{.27a}\ A_{.27b})\ V0f)\ V1g)) \\
& \quad V2x) = (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A_{.27b})\ (ap\ (ap\ (c\_2Ebool\_2EIN \\
& \quad A_{.27a})\ V2x)\ (ap\ (c\_2Efinite\_map\_2EFDOM\ A_{.27a}\ A_{.27b})\ V0f)))\ (ap \\
& \quad (ap\ (c\_2Efinite\_map\_2EFAPPLY\ A_{.27a}\ A_{.27b})\ V0f)\ V2x))\ (ap\ (ap\ ( \\
& \quad c\_2Efinite\_map\_2EFAPPLY\ A_{.27a}\ A_{.27b})\ V1g)\ V2x)))))) \\
& \hspace{15em} (26)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow ( \\
& \quad \forall V0f \in (ty\_2Efinite\_map\_2E fmap\ A_{.27a}\ A_{.27b}).(\forall V1g \in \\
& \quad (ty\_2Efinite\_map\_2E fmap\ A_{.27a}\ A_{.27b}).((p\ (ap\ (ap\ (c\_2Efinite\_map\_2ESUBMAP \\
& \quad A_{.27a}\ A_{.27b})\ V0f)\ V1g)) \Leftrightarrow ((ap\ (ap\ (c\_2Efinite\_map\_2EFUNION\ A_{.27a} \\
& \quad A_{.27b})\ V0f)\ V1g) = V1g)))) \\
& \hspace{15em} (27)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0s \in (2^{A_{.27a}}).(\forall V1t \in \\
& \quad (2^{A_{.27a}}).(\forall V2x \in A_{.27a}.((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A_{.27a}) \\
& \quad V2x)\ (ap\ (ap\ (c\_2Epred\_set\_2EUNION\ A_{.27a})\ V0s)\ V1t))) \Leftrightarrow ((p\ (ap \\
& \quad (ap\ (c\_2Ebool\_2EIN\ A_{.27a})\ V2x)\ V0s)) \vee (p\ (ap\ (ap\ (c\_2Ebool\_2EIN \\
& \quad A_{.27a})\ V2x)\ V1t)))))) \\
& \hspace{15em} (28)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0s \in (2^{A-27a}). (\forall V1t \in \\
& (2^{A-27a}). (\forall V2x \in A.27a. ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A.27a) \\
& V2x)\ (ap\ (ap\ (c\_2Epred\_set\_2EINTER\ A.27a)\ V0s)\ V1t)))) \Leftrightarrow ((p\ (ap\ (29) \\
& (ap\ (c\_2Ebool\_2EIN\ A.27a)\ V2x)\ V0s)) \wedge (p\ (ap\ (ap\ (c\_2Ebool\_2EIN \\
& A.27a)\ V2x)\ V1t))))))
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow ( \\
& \forall V0s2 \in (2^{A-27a}). (\forall V1s1 \in (2^{A-27a}). (\forall V2f \in \\
& (ty\_2Efinite\_map\_2Efmap\ A.27a\ A.27b). (\forall V3g \in (ty\_2Efinite\_map\_2Efmap \\
& A.27a\ A.27b). ((p\ (ap\ (ap\ (c\_2Epred\_set\_2ESUBSET\ A.27a)\ V0s2) \\
& V1s1)) \Rightarrow (\exists V4h \in (ty\_2Efinite\_map\_2Efmap\ A.27a\ A.27b). \\
& ((ap\ (ap\ (c\_2Efinite\_map\_2EFUNION\ A.27a\ A.27b)\ (ap\ (ap\ (c\_2Efinite\_map\_2EDRESTRICT \\
& A.27a\ A.27b)\ V2f)\ V1s1))\ V3g) = (ap\ (ap\ (c\_2Efinite\_map\_2EFUNION \\
& A.27a\ A.27b)\ (ap\ (ap\ (c\_2Efinite\_map\_2EDRESTRICT\ A.27a\ A.27b) \\
& V2f)\ V0s2))\ V4h))))))
\end{aligned}$$