

thm_2Efrac_2EFRAC (TMG8EaTEfGcNBYf41yHkHGsqEFVpnDqMFH1)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{1}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{2}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \tag{3}$$

Definition 3 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Let $ty_2Einteger_2Eint : \iota$ be given. Assume the following.

$$nonempty\ ty_2Einteger_2Eint \tag{4}$$

Let $c_2Einteger_2Eint_of_num : \iota$ be given. Assume the following.

$$c_2Einteger_2Eint_of_num \in (ty_2Einteger_2Eint^{ty_2Enum_2Enum}) \tag{5}$$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Epair_2Eprod\ A0\ A1) \tag{6}$$

Let $c_2Einteger_2Eint_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Einteger_2Eint_REP_CLASS \in ((2^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)})\ ty_2Einteger_2Eint) \tag{7}$$

Definition 12 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in A_27a.\lambda V1y \in A_27b.(ap (c_2$

Assume the following.

$$True \tag{15}$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \tag{16}$$

Assume the following.

$$\begin{aligned} & ((\forall V0a \in ty_2Efrac_2Efrac.((ap\ c_2Efrac_2Eabs_frac\ (\\ & \quad ap\ c_2Efrac_2Erep_frac\ V0a)) = V0a)) \wedge (\forall V1r \in (ty_2Epair_2Eprod \\ & \quad ty_2Einteger_2Eint\ ty_2Einteger_2Eint).((p\ (ap\ (\lambda V2f \in (ty_2Epair_2Eprod \\ & \quad ty_2Einteger_2Eint\ ty_2Einteger_2Eint).(ap\ (ap\ c_2Einteger_2Eint_lt \\ & \quad (ap\ c_2Einteger_2Eint_of_num\ c_2Enum_2E0))\ (ap\ (c_2Epair_2ESND \\ & \quad ty_2Einteger_2Eint\ ty_2Einteger_2Eint)\ V2f)))\ V1r)) \Leftrightarrow ((ap\ c_2Efrac_2Erep_frac \\ & \quad (ap\ c_2Efrac_2Eabs_frac\ V1r)) = V1r)))) \end{aligned} \tag{17}$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad \forall V0x \in (ty_2Epair_2Eprod\ A_27a\ A_27b).((ap\ (ap\ (c_2Epair_2E_2C \\ & \quad A_27a\ A_27b)\ (ap\ (c_2Epair_2EFST\ A_27a\ A_27b)\ V0x))\ (ap\ (c_2Epair_2ESND \\ & \quad A_27a\ A_27b)\ V0x)) = V0x)) \end{aligned} \tag{18}$$

Theorem 1

$$\begin{aligned} & (\forall V0f \in ty_2Efrac_2Efrac.((ap\ c_2Efrac_2Eabs_frac\ (ap \\ & \quad (ap\ (c_2Epair_2E_2C\ ty_2Einteger_2Eint\ ty_2Einteger_2Eint) \\ & \quad (ap\ c_2Efrac_2Efrac_nmr\ V0f))\ (ap\ c_2Efrac_2Efrac_dnm\ V0f))) = \\ & \quad V0f)) \end{aligned}$$