

thm_2Ehreal_2EHRAT__UP
(TMM7wSVhLQJbzduBUYdkXz9ueCoyYz96ReN)

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Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{1}$$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Epair_2Eprod\ A0\ A1) \tag{2}$$

Let $ty_2Ehrat_2Ehrat : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ehrat_2Ehrat \tag{3}$$

Let $c_2Ehrat_2Ehrat_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Ehrat_2Ehrat_REP_CLASS \in ((2^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)})_{ty_2Ehrat_2Ehrat}) \tag{4}$$

Definition 1 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A$.if $(\exists x \in A.p\ (ap\ P\ x))$ then (the $(\lambda x.x \in A \wedge p\ x)$ of type $\iota \Rightarrow \iota$).

Definition 2 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o\ (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define $c_2Ebool_2E_2ET$ to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 4 We define $c_2Ebool_2E_21$ to be $\lambda A.\lambda a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c_2Emin_2E_3D\ (2^{A-27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V2x \in 2.V2x))$

Definition 5 We define $c_2Ehrat_2Ehrat_REP$ to be $\lambda V0a \in ty_2Ehrat_2Ehrat.(ap\ (c_2Emin_2E_40\ (ty_2Ehrat_2Ehrat_REP_CLASS\ a)))$

Let $c_2Ehrat_2Etrac_add : \iota$ be given. Assume the following.

$$c_2Ehrat_2Etrac_add \in (((ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum)})_{c_2Ehrat_2Etrac_add}) \tag{5}$$

Let $c_2Eh_rat_2E_tr_at_eq : \iota$ be given. Assume the following.

$$c_2Eh_rat_2E_tr_at_eq \in ((2^{(ty_2E_pair_2E_prod\ ty_2E_num_2E_num\ ty_2E_num_2E_num)})^{(ty_2E_pair_2E_prod\ ty_2E_num_2E_num)}) \quad (6)$$

Let $c_2Eh_rat_2E_h_rat_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Eh_rat_2E_h_rat_ABS_CLASS \in (ty_2Eh_rat_2Eh_rat^{(2^{(ty_2E_pair_2E_prod\ ty_2E_num_2E_num\ ty_2E_num_2E_num)})}) \quad (7)$$

Definition 6 We define $c_2Eh_rat_2E_h_rat_ABS$ to be $\lambda V0r \in (ty_2E_pair_2E_prod\ ty_2E_num_2E_num\ ty_2E_num_2E_num)$

Definition 7 We define $c_2Eh_rat_2E_h_rat_add$ to be $\lambda V0T1 \in ty_2Eh_rat_2Eh_rat.\lambda V1T2 \in ty_2Eh_rat_2Eh_rat$

Definition 8 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ V0P\ (ap\ (c_2Emin_2E_40\ A_27a\ P))))$

Definition 9 We define $c_2Ehreal_2E_h_rat_lt$ to be $\lambda V0x \in ty_2Eh_rat_2Eh_rat.\lambda V1y \in ty_2Eh_rat_2Eh_rat$

Theorem 1

$$(\forall V0x \in ty_2Eh_rat_2Eh_rat.(\exists V1y \in ty_2Eh_rat_2Eh_rat. (p\ (ap\ (ap\ c_2Ehreal_2E_h_rat_lt\ V0x)\ V1y))))$$