

Assume the following.

$$True \quad (13)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2))))) \quad (14)$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \quad (15)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_27a. (p V0t) \Leftrightarrow (p V0t))) \quad (16)$$

Assume the following.

$$(\forall V0t \in 2. (((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))) \quad (17)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (18)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (19)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (20)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (21)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0P \in (2^{A_27a}). (\forall V1Q \in \\ & 2. ((\forall V2x \in A_27a. ((p (ap V0P V2x)) \Rightarrow (p V1Q))) \Leftrightarrow ((\exists V3x \in A_27a. (p (ap V0P V3x)) \Rightarrow (p V1Q))))) \end{aligned} \quad (22)$$

Assume the following.

$$(\forall V0P \in 2. (\forall V1Q \in 2. (\forall V2R \in 2. (((((p V0P) \vee \\ (p V1Q)) \Rightarrow (p V2R)) \Leftrightarrow (((p V0P) \Rightarrow (p V2R)) \wedge ((p V1Q) \Rightarrow (p V2R))))))) \quad (23)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p V0t1) \Rightarrow \\ ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (24)$$

Assume the following.

$$(\forall V0x \in 2. (\forall V1x_27 \in 2. (\forall V2y \in 2. (\forall V3y_27 \in \\ 2. (((((p V0x) \Leftrightarrow (p V1x_27)) \wedge ((p V1x_27) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_27)))) \Rightarrow \\ (((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_27) \Rightarrow (p V3y_27))))))) \quad (25)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow \forall A_27b.\text{nonempty } A_27b \Rightarrow \forall A_27c. \\ & \quad \text{nonempty } A_27c \Rightarrow (\forall V0f \in (A_27b^{A_27a}). (\forall V1g \in (A_27a^{A_27c}). \\ & \quad (\forall V2x \in A_27c. ((ap (ap (ap (c_2Ecombin_2Eo A_27c A_27b A_27a) \\ & \quad V0f) V1g) V2x) = (ap V0f (ap V1g V2x))))))) \end{aligned} \quad (26)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow \forall A_27b.\text{nonempty } A_27b \Rightarrow (\\ & \quad (\forall V0f \in ((A_27a^{A_27b})^{ty_2Enum_2Enum}). ((ap (ap (c_2EindexedLists_2EMAPi \\ & \quad A_27a A_27b) V0f) (c_2Elist_2ENIL A_27b)) = (c_2Elist_2ENIL A_27a))) \wedge \\ & \quad (\forall V1f \in ((A_27a^{A_27b})^{ty_2Enum_2Enum}). (\forall V2h \in A_27b. \\ & \quad (\forall V3t \in (ty_2Elist_2Elist A_27b). ((ap (ap (c_2EindexedLists_2EMAPi \\ & \quad A_27a A_27b) V1f) (ap (ap (c_2Elist_2ECONS A_27b) V2h) V3t)) = (ap \\ & \quad (ap (c_2Elist_2ECONS A_27a) (ap (ap V1f c_2Enum_2E0) V2h)) (ap (\\ & \quad ap (c_2EindexedLists_2EMAPi A_27a A_27b) (ap (ap (c_2Ecombin_2Eo \\ & \quad ty_2Enum_2Enum (A_27a^{A_27b}) ty_2Enum_2Enum) V1f) c_2Enum_2ESUC) \\ & \quad V3t))))))) \end{aligned} \quad (27)$$

Assume the following.

$$\begin{aligned} & (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. (\\ & \quad (p (ap (ap c_2Eprim_rec_2E_3C V0n) (ap c_2Enum_2ESUC V1m))) \Leftrightarrow (\\ & \quad (V0n = c_2Enum_2E0) \vee (\exists V2n0 \in ty_2Enum_2Enum. ((V0n = (ap \\ & \quad c_2Enum_2ESUC V2n0)) \wedge (p (ap (ap c_2Eprim_rec_2E_3C V2n0) V1m))))))) \end{aligned} \quad (28)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0h \in A_27a. (\forall V1t \in \\ & \quad (ty_2Elist_2Elist A_27a). ((ap (c_2Elist_2EHD A_27a) (ap (ap (\\ & \quad c_2Elist_2ECONS A_27a) V0h) V1t)) = V0h))) \end{aligned} \quad (29)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty\ A_{27a} \Rightarrow & (((ap\ (c_2Elist_2ELENGTH\ A_{27a}) \\ (c_2Elist_2ENIL\ A_{27a})) = c_2Enum_2E0) \wedge (\forall V0h \in A_{27a}.(\\ \forall V1t \in (ty_2Elist_2Elist\ A_{27a}).((ap\ (c_2Elist_2ELENGTH \\ A_{27a})\ (ap\ (ap\ (c_2Elist_2ECONS\ A_{27a})\ V0h)\ V1t)) = (ap\ c_2Enum_2ESUC \\ (ap\ (c_2Elist_2ELENGTH\ A_{27a})\ V1t))))))) \end{aligned} \quad (30)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty\ A_{27a} \Rightarrow & (\forall V0P \in (2^{(ty_2Elist_2Elist\ A_{27a})}). \\ (((p\ (ap\ V0P\ (c_2Elist_2ENIL\ A_{27a}))) \wedge (\forall V1t \in (ty_2Elist_2Elist \\ A_{27a}).((p\ (ap\ V0P\ V1t)) \Rightarrow (\forall V2h \in A_{27a}.(p\ (ap\ V0P\ (ap\ (ap \\ (c_2Elist_2ECONS\ A_{27a})\ V2h)\ V1t))))))) \Rightarrow (\forall V3l \in (ty_2Elist_2Elist \\ A_{27a}).(p\ (ap\ V0P\ V3l)))))) \end{aligned} \quad (31)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty\ A_{27a} \Rightarrow & \forall A_{27b}.nonempty\ A_{27b} \Rightarrow (\\ \forall V0n \in ty_2Enum_2Enum.(\forall V1l \in A_{27b}.(\forall V2ls \in \\ (ty_2Elist_2Elist\ A_{27b}).(((ap\ (c_2Elist_2EEL\ A_{27a})\ c_2Enum_2E0) = \\ (c_2Elist_2EHD\ A_{27a})) \wedge ((ap\ (ap\ (c_2Elist_2EEL\ A_{27b})\ (ap\ c_2Enum_2ESUC \\ V0n))\ (ap\ (ap\ (c_2Elist_2ECONS\ A_{27b})\ V1l)\ V2ls)) = (ap\ (ap\ (c_2Elist_2EEL \\ A_{27b})\ V0n)\ V2ls))))))) \end{aligned} \quad (32)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.(\neg(p\ (ap\ (ap\ c_2Eprim_rec_2E_3C \\ V0n)\ c_2Enum_2E0)))) \quad (33)$$

Theorem 1

$$\begin{aligned} \forall A_{27a}.nonempty\ A_{27a} \Rightarrow & \forall A_{27b}.nonempty\ A_{27b} \Rightarrow (\\ \forall V0f \in ((A_{27b}^{A_{27a}})^{ty_2Enum_2Enum}).(\forall V1n \in ty_2Enum_2Enum. \\ (\forall V2l \in (ty_2Elist_2Elist\ A_{27a}).((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C \\ V1n)\ (ap\ (c_2Elist_2ELENGTH\ A_{27a})\ V2l))) \Rightarrow ((ap\ (ap\ (c_2Elist_2EEL \\ A_{27b})\ V1n)\ (ap\ (ap\ (c_2EindexedLists_2EMAPi\ A_{27b}\ A_{27a})\ V0f)\ \\ V2l)) = (ap\ (ap\ V0f\ V1n)\ (ap\ (ap\ (c_2Elist_2EEL\ A_{27a})\ V1n)\ V2l))))))) \end{aligned}$$