

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (14)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg(p\ V0t)))))) \quad (15)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \quad (16)$$

Assume the following.

$$(\forall V0x \in 2. (\forall V1x_27 \in 2. (\forall V2y \in 2. (\forall V3y_27 \in 2. (((p\ V0x) \Leftrightarrow (p\ V1x_27)) \wedge ((p\ V1x_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y_27)))))) \Rightarrow (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x_27) \Rightarrow (p\ V3y_27)))))) \quad (17)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c.nonempty\ A_27c \Rightarrow (\forall V0f \in (A_27b^{A_27a}). (\forall V1g \in (A_27a^{A_27c}). (\forall V2x \in A_27c. ((ap\ (ap\ (ap\ (c_2Ecombin_2Eo\ A_27c\ A_27b\ A_27a)\ V0f)\ V1g)\ V2x) = (ap\ V0f\ (ap\ V1g\ V2x)))))) \quad (18)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow ((\forall V0l \in (ty_2Elist_2Elist\ A_27a). ((ap\ (ap\ (c_2Elist_2EAPPEND\ A_27a)\ (c_2Elist_2ENIL\ A_27a))\ V0l) = V0l)) \wedge (\forall V1l1 \in (ty_2Elist_2Elist\ A_27a). (\forall V2l2 \in (ty_2Elist_2Elist\ A_27a). (\forall V3h \in A_27a. ((ap\ (ap\ (c_2Elist_2EAPPEND\ A_27a)\ (ap\ (ap\ (c_2Elist_2ECONS\ A_27a)\ V3h)\ V1l1))\ V2l2) = (ap\ (ap\ (c_2Elist_2ECONS\ A_27a)\ V3h)\ (ap\ (ap\ (c_2Elist_2EAPPEND\ A_27a)\ V1l1)\ V2l2))))))))) \quad (19)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow ((\forall V0P \in (2^{A_27a}). ((p\ (ap\ (ap\ (c_2Elist_2EEVERY\ A_27a)\ V0P)\ (c_2Elist_2ENIL\ A_27a))) \Leftrightarrow True)) \wedge (\forall V1P \in (2^{A_27a}). (\forall V2h \in A_27a. (\forall V3t \in (ty_2Elist_2Elist\ A_27a). ((p\ (ap\ (ap\ (c_2Elist_2EEVERY\ A_27a)\ V1P)\ (ap\ (ap\ (c_2Elist_2ECONS\ A_27a)\ V2h)\ V3t))) \Leftrightarrow ((p\ (ap\ V1P\ V2h)) \wedge (p\ (ap\ (ap\ (c_2Elist_2EEVERY\ A_27a)\ V1P)\ V3t)))))))))) \quad (20)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.\text{nonempty } A_27a \Rightarrow ((\forall V0P \in (2^{A_27a}).((p (ap \\
& (ap (c_2Elist_2EEXISTS A_27a) V0P) (c_2Elist_2ENIL A_27a))) \Leftrightarrow \\
& \text{False})) \wedge (\forall V1P \in (2^{A_27a}).(\forall V2h \in A_27a.(\forall V3t \in \\
& (ty_2Elist_2Elist A_27a).((p (ap (ap (c_2Elist_2EEXISTS A_27a) \\
& V1P) (ap (ap (c_2Elist_2ECONS A_27a) V2h) V3t))) \Leftrightarrow ((p (ap V1P V2h)) \vee \\
& (p (ap (ap (c_2Elist_2EEXISTS A_27a) V1P) V3t))))))))))
\end{aligned} \tag{21}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0P \in (2^{(ty_2Elist_2Elist A_27a)}). \\
& (((p (ap V0P (c_2Elist_2ENIL A_27a))) \wedge (\forall V1t \in (ty_2Elist_2Elist \\
& A_27a).((p (ap V0P V1t)) \Rightarrow (\forall V2h \in A_27a.(p (ap V0P (ap (ap (\\
& c_2Elist_2ECONS A_27a) V2h) V1t))))))) \Rightarrow (\forall V3l \in (ty_2Elist_2Elist \\
& A_27a).(p (ap V0P V3l))))))
\end{aligned} \tag{22}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0l1 \in (ty_2Elist_2Elist \\
& A_27a).(\forall V1l2 \in (ty_2Elist_2Elist A_27a).(\forall V2l3 \in \\
& (ty_2Elist_2Elist A_27a).((ap (ap (c_2Elist_2EAPPEND A_27a) \\
& V0l1) (ap (ap (c_2Elist_2EAPPEND A_27a) V1l2) V2l3)) = (ap (ap (c_2Elist_2EAPPEND \\
& A_27a) (ap (ap (c_2Elist_2EAPPEND A_27a) V0l1) V1l2)) V2l3))))))
\end{aligned} \tag{23}$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0P \in (2^{A_27a}).(\forall V1l \in \\
& (ty_2Elist_2Elist A_27a).((p (ap (ap (c_2Elist_2EEXISTS A_27a) \\
& V0P) V1l)) \Rightarrow (\exists V2l1 \in (ty_2Elist_2Elist A_27a).(\exists V3x \in \\
& A_27a.(\exists V4l2 \in (ty_2Elist_2Elist A_27a).((V1l = (ap (ap \\
& (c_2Elist_2EAPPEND A_27a) V2l1) (ap (ap (c_2Elist_2ECONS A_27a) \\
& V3x) V4l2)))) \wedge ((p (ap (ap (c_2Elist_2EVERY A_27a) (ap (ap (c_2Ecombin_2Eo \\
& A_27a 2 2) c_2Ebool_2E7E) V0P)) V2l1)) \wedge (p (ap V0P V3x))))))))))
\end{aligned}$$