

thm\_2Elebesgue\_2ERadon\_\_Nikodym2  
(TMQqSrSi1GVES2NViZEwyH3UQpkN9NhU2Zq)

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**Definition 1** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A.$ if  $(\exists x \in A.p (ap P x))$  **then** (the  $(\lambda x.x \in A \wedge p x)$  of type  $\iota \Rightarrow \iota$ ).

**Definition 2** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define  $c\_2Ebool\_2ET$  to be  $(ap (ap (c\_2Emin\_2E\_3D (2^2))) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x)$

**Definition 4** We define  $c\_2Ecombin\_2ES$  to be  $\lambda A.\lambda a : \iota.\lambda A.\lambda b : \iota.\lambda A.\lambda c : \iota.(\lambda V0f \in ((A\_27c^{A\_27b})^{A\_27a}))$

**Definition 5** We define  $c\_2Ecombin\_2EC$  to be  $\lambda A.\lambda a : \iota.\lambda A.\lambda b : \iota.\lambda A.\lambda c : \iota.(\lambda V0f \in ((A\_27c^{A\_27b})^{A\_27a}))$

**Definition 6** We define  $c\_2Ecombin\_2EK$  to be  $\lambda A.\lambda a : \iota.\lambda A.\lambda b : \iota.(\lambda V0x \in A\_27a.(\lambda V1y \in A\_27b.V0x))$

**Definition 7** We define  $c\_2Ecombin\_2EI$  to be  $\lambda A.\lambda a : \iota.(ap (ap (c\_2Ecombin\_2ES A\_27a (A\_27a^{A\_27a})) A\_27a))$

**Definition 8** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.\lambda a : \iota.(\lambda V0P \in (2^{A\_27a})).(ap (ap (c\_2Emin\_2E\_3D (2^{A\_27a})) P))$

**Definition 9** We define  $c\_2Ecombin\_2Eo$  to be  $\lambda A.\lambda a : \iota.\lambda A.\lambda b : \iota.\lambda A.\lambda c : \iota.(\lambda V0f \in (A\_27b^{A\_27c})).\lambda V1g \in (A\_27b^{A\_27c})$

Let  $ty\_2Eextreal\_2Eextreal : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Eextreal\_2Eextreal \tag{1}$$

Let  $c\_2Eextreal\_2ENegInf : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2ENegInf \in ty\_2Eextreal\_2Eextreal \tag{2}$$

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Enum\_2Enum \tag{3}$$

Let  $c\_2Enum\_2EZERO\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2EZERO\_REP \in omega \tag{4}$$

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{omega}) \tag{5}$$

**Definition 10** We define  $c\_Enum\_2E0$  to be  $(ap\ c\_Enum\_2EABS\_num\ c\_Enum\_2EZERO\_REP)$ .

Let  $ty\_2Erealax\_2Ereal : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Erealax\_2Ereal \quad (6)$$

Let  $c\_2Ereal\_2Ereal\_of\_num : \iota$  be given. Assume the following.

$$c\_2Ereal\_2Ereal\_of\_num \in (ty\_2Erealax\_2Ereal^{ty\_2Enum\_2Enum}) \quad (7)$$

Let  $c\_2Eextreal\_2ENormal : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2ENormal \in (ty\_2Eextreal\_2Eextreal^{ty\_2Erealax\_2Ereal}) \quad (8)$$

**Definition 11** We define  $c\_2Eextreal\_2Eextreal\_of\_num$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap\ c\_2Eextreal\_2Eextreal\_of\_num)$ .

Let  $c\_2Eextreal\_2Eextreal\_ainv : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2Eextreal\_ainv \in (ty\_2Eextreal\_2Eextreal^{ty\_2Eextreal\_2Eextreal}) \quad (9)$$

Let  $c\_2Eextreal\_2Eextreal\_le : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2Eextreal\_le \in ((2^{ty\_2Eextreal\_2Eextreal})^{ty\_2Eextreal\_2Eextreal}) \quad (10)$$

**Definition 12** We define  $c\_2Ebool\_2EF$  to be  $(ap\ (c\_2Ebool\_2E21\ 2)\ (\lambda V0t \in 2.V0t))$ .

**Definition 13** We define  $c\_2Emin\_2E3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o\ (p\ P \Rightarrow p\ Q)$  of type  $\iota$ .

**Definition 14** We define  $c\_2Ebool\_2E7E$  to be  $(\lambda V0t \in 2.(ap\ (ap\ c\_2Emin\_2E3D\_3D\_3E\ V0t)\ c\_2Ebool\_2E7E))$ .

**Definition 15** We define  $c\_2Eextreal\_2Eextreal\_lt$  to be  $\lambda V0x \in ty\_2Eextreal\_2Eextreal.\lambda V1y \in ty\_2Eextreal\_2Eextreal.$

**Definition 16** We define  $c\_2Ebool\_2E2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c\_2Ebool\_2E21\ 2)\ (\lambda V2t \in 2.V2t))))$ .

**Definition 17** We define  $c\_2Ebool\_2ECOND$  to be  $\lambda A\_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A\_27a.(\lambda V2t2 \in A\_27a.2)))$ .

**Definition 18** We define  $c\_2Emeasure\_2Efn\_minus$  to be  $\lambda A\_27a : \iota.\lambda V0f \in (ty\_2Eextreal\_2Eextreal^{A\_27a})$ .

**Definition 19** We define  $c\_2Emeasure\_2Efn\_plus$  to be  $\lambda A\_27a : \iota.\lambda V0f \in (ty\_2Eextreal\_2Eextreal^{A\_27a})$ .

Let  $ty\_2Ehreal\_2Ehreal : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Ehreal\_2Ehreal \quad (11)$$

Let  $ty\_2Epair\_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty\_2Epair\_2Eprod\ A0\ A1) \quad (12)$$

Let  $c\_2Erealax\_2Ereal\_REP\_CLASS : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Ereal\_REP\_CLASS \in ((2^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)})^{ty\_2Erealax\_2Ereal}) \quad (13)$$

**Definition 20** We define  $c\_2Erealax\_2Ereal\_REP$  to be  $\lambda V0a \in ty\_2Erealax\_2Ereal.(ap (c\_2Emin\_2E.40 (t$

Let  $c\_2Erealax\_2Etrealm\_neg : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Etrealm\_neg \in ((ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal) (ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)) \quad (14)$$

Let  $c\_2Erealax\_2Etrealm\_eq : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Etrealm\_eq \in ((2^{(ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)}) (ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)) \quad (15)$$

Let  $c\_2Erealax\_2Ereal\_ABS\_CLASS : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Ereal\_ABS\_CLASS \in (ty\_2Erealax\_2Ereal)^{(2^{(ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)})} \quad (16)$$

**Definition 21** We define  $c\_2Erealax\_2Ereal\_ABS$  to be  $\lambda V0r \in (ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)$

**Definition 22** We define  $c\_2Erealax\_2Ereal\_neg$  to be  $\lambda V0T1 \in ty\_2Erealax\_2Ereal.(ap c\_2Erealax\_2Ereal$

Let  $c\_2Erealax\_2Etrealm\_lt : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Etrealm\_lt \in ((2^{(ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)}) (ty\_2Epair\_2Eprod ty\_2Ehreal\_2Ehreal ty\_2Ehreal\_2Ehreal)) \quad (17)$$

**Definition 23** We define  $c\_2Erealax\_2Ereal\_lt$  to be  $\lambda V0T1 \in ty\_2Erealax\_2Ereal.\lambda V1T2 \in ty\_2Erealax\_2Ereal$

**Definition 24** We define  $c\_2Ereal\_2Ereal\_lte$  to be  $\lambda V0x \in ty\_2Erealax\_2Ereal.\lambda V1y \in ty\_2Erealax\_2Ereal$

**Definition 25** We define  $c\_2Ereal\_2Eabs$  to be  $\lambda V0x \in ty\_2Erealax\_2Ereal.(ap (ap (ap (c\_2Ebool\_2ECONJ$

Let  $c\_2Eextreal\_2EPosInf : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2EPosInf \in ty\_2Eextreal\_2Eextreal \quad (18)$$

Let  $c\_2Eextreal\_2Eextreal\_CASE : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Eextreal\_2Eextreal\_CASE A\_27a \in (((A\_27a^{(A\_27a^{ty\_2Erealax\_2Ereal})})^{A\_27a})^{A\_27a})^{ty\_2Eextreal\_2Eextreal}) \quad (19)$$

**Definition 26** We define  $c\_2Ebool\_2E.3F$  to be  $\lambda A\_27a : \iota. (\lambda V0P \in (2^{A\_27a}).(ap V0P (ap (c\_2Emin\_2E.40$

**Definition 27** We define  $c\_2Erelation\_2EWF$  to be  $\lambda A\_27a : \iota. \lambda V0R \in ((2^{A\_27a})^{A\_27a}).(ap (c\_2Ebool\_2E.21$

Let  $c\_2Ebool\_2EARB : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Ebool\_2EARB A\_27a \in A\_27a \quad (20)$$

**Definition 28** We define  $c\_2Erelation\_2ERESTRICT$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (A\_27b^{A\_27a}). \lambda V1f$

**Definition 29** We define  $c\_2Erelation\_2ETC$  to be  $\lambda A\_27a : \iota.\lambda V0R \in ((2^{A\_27a})^{A\_27a}).\lambda V1a \in A\_27a.\lambda V2b$

**Definition 30** We define  $c\_2Erelation\_2Eapprox$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0R \in ((2^{A\_27a})^{A\_27a}).\lambda V1M$

**Definition 31** We define  $c\_2Erelation\_2Ethe\_fun$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0R \in ((2^{A\_27a})^{A\_27a}).\lambda V1M$

**Definition 32** We define  $c\_2Erelation\_2EWFREC$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0R \in ((2^{A\_27a})^{A\_27a}).\lambda V1M$

**Definition 33** We define  $c\_2Eextreal\_2Eextreal\_abs$  to be  $(ap (ap (c\_2Erelation\_2EWFREC ty\_2Eextreal\_2E$

Let  $c\_2Emeasure\_2Em\_space : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty A\_27a \Rightarrow c\_2Emeasure\_2Em\_space A\_27a \in \\ ((2^{A\_27a})^{(ty\_2Epair\_2Eprod (2^{A\_27a}) (ty\_2Epair\_2Eprod (2^{A\_27a}) (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))})) \end{aligned} \quad (21)$$

**Definition 34** We define  $c\_2Ebool\_2EIN$  to be  $\lambda A\_27a : \iota.(\lambda V0x \in A\_27a.(\lambda V1f \in (2^{A\_27a}).(ap V1f V0x)))$

Let  $c\_2Epair\_2EABS\_prod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Epair\_2EABS\_prod \\ A\_27a A\_27b \in ((ty\_2Epair\_2Eprod A\_27a A\_27b)^{(2^{A\_27b})^{A\_27a}}) \end{aligned} \quad (22)$$

**Definition 35** We define  $c\_2Epair\_2E\_2C$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0x \in A\_27a.\lambda V1y \in A\_27b.(ap (c\_2$

Let  $c\_2Epred\_set\_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Epred\_set\_2EGSPEC \\ A\_27a A\_27b \in ((2^{A\_27a})^{(ty\_2Epair\_2Eprod A\_27a 2)^{A\_27b}}) \end{aligned} \quad (23)$$

**Definition 36** We define  $c\_2Epred\_set\_2EIMAGE$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0f \in (A\_27b^{A\_27a}).\lambda V1s \in$

**Definition 37** We define  $c\_2Epred\_set\_2EBIGUNION$  to be  $\lambda A\_27a : \iota.\lambda V0P \in (2^{(2^{A\_27a})}).(ap (c\_2Epred\_set$

**Definition 38** We define  $c\_2Epred\_set\_2EEMPTY$  to be  $\lambda A\_27a : \iota.(\lambda V0x \in A\_27a.c\_2Ebool\_2EF)$ .

**Definition 39** We define  $c\_2Epred\_set\_2EINTER$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).\lambda V1t \in (2^{A\_27a}).(ap (c\_2$

**Definition 40** We define  $c\_2Epred\_set\_2EDISJOINT$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).\lambda V1t \in (2^{A\_27a}).(ap$

**Definition 41** We define  $c\_2Ebool\_2E\_5C\_2F$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in$

**Definition 42** We define  $c\_2Epred\_set\_2EINSERT$  to be  $\lambda A\_27a : \iota.\lambda V0x \in A\_27a.\lambda V1s \in (2^{A\_27a}).(ap (c\_2$

**Definition 43** We define  $c\_2Epred\_set\_2EFINITE$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).(ap (c\_2Ebool\_2E\_21 2)$

Let  $c\_2Emeasure\_2Emeasurable\_sets : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Emeasurable\_sets \\ A\_27a \in & ((2^{(2^{A\_27a})})^{(ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealx\_2Ereal^{(2^{A\_27a})})))}) \end{aligned} \quad (24)$$

**Definition 44** We define  $c\_2Earithmetic\_2EZERO$  to be  $c\_2Enum\_2E0$ .

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \quad (25)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega}) \quad (26)$$

**Definition 45** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.(ap\ c\_2Enum\_2EABS\_num$

Let  $c\_2Earithmetic\_2E\_2B : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2E\_2B \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (27)$$

**Definition 46** We define  $c\_2Earithmetic\_2EBIT1$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Earithmetic$

**Definition 47** We define  $c\_2Earithmetic\_2ENUMERAL$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.V0x$ .

**Definition 48** We define  $c\_2Emeasure\_2Eindicator\_fn$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).(\lambda V1x \in A\_27a.(ap$

Let  $c\_2Eextreal\_2Eextreal\_mul : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2Eextreal\_mul \in ((ty\_2Eextreal\_2Eextreal^{ty\_2Eextreal\_2Eextreal})^{ty\_2Eextreal\_2Eextreal}) \quad (28)$$

Let  $c\_2Eextreal\_2Eextreal\_add : \iota$  be given. Assume the following.

$$c\_2Eextreal\_2Eextreal\_add \in ((ty\_2Eextreal\_2Eextreal^{ty\_2Eextreal\_2Eextreal})^{ty\_2Eextreal\_2Eextreal}) \quad (29)$$

Let  $c\_2Epred\_set\_2EITSET : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epred\_set\_2EITSET \\ A\_27a\ A\_27b \in & (((A\_27b^{A\_27b})^{(2^{A\_27a})})^{((A\_27b^{A\_27b})^{A\_27a})}) \end{aligned} \quad (30)$$

**Definition 49** We define  $c\_2Eextreal\_2EEXTREAL\_SUM\_IMAGE$  to be  $\lambda A\_27a : \iota.\lambda V0f \in (ty\_2Eextreal$

**Definition 50** We define  $c\_2Emeasure\_2Epos\_simple\_fn$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod\ (2^A$

Let  $c\_2Epair\_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epair\_2ESND \\ A\_27a\ A\_27b \in (A\_27b^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)}) \end{aligned} \quad (31)$$

Let  $c\_2Epair\_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epair\_2EFST \\ A\_27a\ A\_27b \in (A\_27a^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)}) \end{aligned} \quad (32)$$

**Definition 51** We define  $c\_2Epair\_2EUNCURRY$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda A\_27c : \iota. \lambda V0f \in ((A\_27c^{A\_27a})$

**Definition 52** We define  $c\_2Elebesgue\_2Epsfs$  to be  $\lambda A\_27a : \iota. \lambda V0m \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (ty\_2E$

Let  $c\_2Emeasure\_2Emeasure : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Emeasure\ A\_27a \in ( \\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})})^{(ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})})} \end{aligned} \quad (33)$$

Let  $c\_2Erealax\_2Etrealmul : \iota$  be given. Assume the following.

$$\begin{aligned} c\_2Erealax\_2Etrealmul \in (((ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal \\ ty\_2Ehreal\_2Ehreal)^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)}\ (ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal) \end{aligned} \quad (34)$$

**Definition 53** We define  $c\_2Erealax\_2Erealmul$  to be  $\lambda V0T1 \in ty\_2Erealax\_2Ereal. \lambda V1T2 \in ty\_2Erealax$

Let  $c\_2Erealax\_2Erealadd : \iota$  be given. Assume the following.

$$\begin{aligned} c\_2Erealax\_2Erealadd \in (((ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal \\ ty\_2Ehreal\_2Ehreal)^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)}\ (ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal) \end{aligned} \quad (35)$$

**Definition 54** We define  $c\_2Erealax\_2Erealadd$  to be  $\lambda V0T1 \in ty\_2Erealax\_2Ereal. \lambda V1T2 \in ty\_2Erealax$

**Definition 55** We define  $c\_2Ereal\_sigma\_2EREAL\_SUM\_IMAGE$  to be  $\lambda A\_27a : \iota. \lambda V0f \in (ty\_2Erealax\_2E$

**Definition 56** We define  $c\_2Elebesgue\_2Epos\_simple\_fn\_integral$  to be  $\lambda A\_27a : \iota. \lambda V0m \in (ty\_2Epair\_2E$

**Definition 57** We define  $c\_2Elebesgue\_2Epsfs$  to be  $\lambda A\_27a : \iota. \lambda V0m \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (ty\_2E$

**Definition 58** We define  $c\_2Ereal\_2Esup$  to be  $\lambda V0P \in (2^{ty\_2Erealax\_2Ereal}). (ap\ (c\_2Emin\_2E\_40\ ty\_2Ereal$

**Definition 59** We define  $c\_2Eextreal\_2Eextreal\_sup$  to be  $\lambda V0p \in (2^{ty\_2Eextreal\_2Eextreal}). (ap\ (ap\ (ap\ (c\_2E$

**Definition 60** We define  $c\_2Elebesgue\_2Epos\_fn\_integral$  to be  $\lambda A\_27a : \iota. \lambda V0m \in (ty\_2Epair\_2Eprod\ (2^{$

**Definition 61** We define  $c\_2Epred\_set\_2EUNIV$  to be  $\lambda A\_27a : \iota. (\lambda V0x \in A\_27a. c\_2Ebool\_2ET)$ .

Let  $c\_2Emeasure\_2Esubsets : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Esubsets\ A\_27a \in ( (2^{(2^{A\_27a})})^{(ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (2^{(2^{A\_27a})})}) ) \quad (36)$$

**Definition 62** We define  $c\_2Epred\_set\_2ESUBSET$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).\lambda V1t \in (2^{A\_27a}).(ap$

**Definition 63** We define  $c\_2Epred\_set\_2EINJ$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0f \in (A\_27b^{A\_27a}).\lambda V1s \in (2^{A\_27b})$

**Definition 64** We define  $c\_2Epred\_set\_2Ecountable$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).(ap\ (c\_2Ebool\_2E3F$

**Definition 65** We define  $c\_2Epred\_set\_2EUNION$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).\lambda V1t \in (2^{A\_27a}).(ap\ (c$

Let  $c\_2Emeasure\_2Espace : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Espace\ A\_27a \in ( (2^{A\_27a})^{(ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (2^{(2^{A\_27a})})}) ) \quad (37)$$

**Definition 66** We define  $c\_2Epred\_set\_2EDIFF$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).\lambda V1t \in (2^{A\_27a}).(ap\ (c\_2E$

**Definition 67** We define  $c\_2Emeasure\_2Esubset\_class$  to be  $\lambda A\_27a : \iota.\lambda V0sp \in (2^{A\_27a}).\lambda V1sts \in (2^{(2^{A\_27a})})$

**Definition 68** We define  $c\_2Emeasure\_2Ealgebra$  to be  $\lambda A\_27a : \iota.\lambda V0a \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (2^{(2^{A\_27a})}))$

**Definition 69** We define  $c\_2Emeasure\_2Esigma\_algebra$  to be  $\lambda A\_27a : \iota.\lambda V0a \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (2^{(2^{A\_27a})}))$

**Definition 70** We define  $c\_2Epred\_set\_2EBIGINTER$  to be  $\lambda A\_27a : \iota.\lambda V0P \in (2^{(2^{A\_27a})}).(ap\ (c\_2Epred\_set\_2E$

**Definition 71** We define  $c\_2Emeasure\_2Esigma$  to be  $\lambda A\_27a : \iota.\lambda V0sp \in (2^{A\_27a}).\lambda V1st \in (2^{(2^{A\_27a})}).(ap\ ($

**Definition 72** We define  $c\_2Emeasure\_2EBorel$  to be  $(ap\ (ap\ (c\_2Emeasure\_2Esigma\ ty\_2Eextreal\_2Eextreal$

**Definition 73** We define  $c\_2Epred\_set\_2EPREIMAGE$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0f \in (A\_27b^{A\_27a}).\lambda V$

**Definition 74** We define  $c\_2Epred\_set\_2EFUNSET$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0P \in (2^{A\_27a}).\lambda V1Q \in (2^{(2^{A\_27b})})$

**Definition 75** We define  $c\_2Emeasure\_2Emeasurable$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0a \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (2^{(2^{A\_27b})}))$

**Definition 76** We define  $c\_2ELebesgue\_2Eintegrable$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (2^{(2^{A\_27a})}))$

**Definition 77** We define  $c\_2ELebesgue\_2Emeasure\_absolutely\_continuous$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})})))$

Let  $c\_2Ereal\_2Esum : \iota$  be given. Assume the following.

$$c\_2Ereal\_2Esum \in ( (ty\_2Erealax\_2Ereal^{(ty\_2Erealax\_2Ereal^{ty\_2Eenum\_2Eenum})})^{(ty\_2Epair\_2Eprod\ ty\_2Eenum\_2Eenum)} ) \quad (38)$$

**Definition 78** We define  $c\_2Eprim\_rec\_2E3C$  to be  $\lambda V0m \in ty\_2Eenum\_2Eenum.\lambda V1n \in ty\_2Eenum\_2Eenum$

**Definition 79** We define  $c\_2Earithmic\_2E\_3E$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

**Definition 80** We define  $c\_2Earithmic\_2E\_3E\_3D$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

**Definition 81** We define  $c\_2Ereal\_2Ereal\_sub$  to be  $\lambda V0x \in ty\_2Erealax\_2Ereal.\lambda V1y \in ty\_2Erealax\_2Ereal$

Let  $ty\_2Emetric\_2Emetric : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty\_2Emetric\_2Emetric A0) \quad (39)$$

Let  $c\_2Emetric\_2Emetric : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Emetric\_2Emetric A\_27a \in ((ty\_2Emetric\_2Emetric A\_27a)^{(ty\_2Erealax\_2Ereal^{(ty\_2Epair\_2Eprod A\_27a A\_27a)})}) \quad (40)$$

**Definition 82** We define  $c\_2Emetric\_2Emr1$  to be  $(ap (c\_2Emetric\_2Emetric ty\_2Erealax\_2Ereal) (ap (c$

Let  $c\_2Emetric\_2Edist : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Emetric\_2Edist A\_27a \in ((ty\_2Erealax\_2Ereal^{(ty\_2Epair\_2Eprod A\_27a A\_27a)}) \quad (41)$$

Let  $ty\_2Etopology\_2Etopology : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty\_2Etopology\_2Etopology A0) \quad (42)$$

Let  $c\_2Etopology\_2Etopology : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Etopology\_2Etopology A\_27a \in ((ty\_2Etopology\_2Etopology A\_27a)^{(2^{(2^{A\_27a})})}) \quad (43)$$

**Definition 83** We define  $c\_2Emetric\_2Emtop$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Emetric\_2Emetric A\_27a).(ap$

Let  $c\_2Enets\_2Etends : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Enets\_2Etends A\_27a A\_27b \in (((2^{(ty\_2Epair\_2Eprod (ty\_2Etopology\_2Etopology A\_27a) ((2^{A\_27b})^{A\_27b}))})_{A\_27a})_{(A\_27a)^{A\_27b}}) \quad (44)$$

**Definition 84** We define  $c\_2Eseq\_2E\_2D\_2D\_3E$  to be  $\lambda V0x \in (ty\_2Erealax\_2Ereal^{ty\_2Enum\_2Enum}).\lambda V1x$

**Definition 85** We define  $c\_2Eseq\_2Esums$  to be  $\lambda V0f \in (ty\_2Erealax\_2Ereal^{ty\_2Enum\_2Enum}).\lambda V1s \in ty\_2Enum\_2Enum$

**Definition 86** We define  $c\_2Emeasure\_2Ecountably\_additive$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod$

**Definition 87** We define  $c\_2Emeasure\_2Epositive$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (ty\_2Enum\_2Enum$

**Definition 88** We define  $c\_2Emeasure\_2Emeasure\_space$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (ty\_2Enum\_2Enum$



Assume the following.

$$True \quad (45)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p \ V0t1) \Rightarrow (p \ V1t2)) \Rightarrow (((p \ V1t2) \Rightarrow (p \ V0t1)) \Rightarrow ((p \ V0t1) \Leftrightarrow (p \ V1t2)))))) \quad (46)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p \ V0t))) \quad (47)$$

Assume the following.

$$(\forall V0t \in 2.((p \ V0t) \vee (\neg(p \ V0t)))) \quad (48)$$

Assume the following.

$$\forall A\_27a.nonempty \ A\_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A\_27a.(p \ V0t)) \Leftrightarrow (p \ V0t))) \quad (49)$$

Assume the following.

$$(\forall V0t \in 2.(((True \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \wedge True) \Leftrightarrow (p \ V0t)) \wedge (((False \wedge (p \ V0t)) \Leftrightarrow False) \wedge (((p \ V0t) \wedge False) \Leftrightarrow False) \wedge (((p \ V0t) \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)))))) \quad (50)$$

Assume the following.

$$(\forall V0t \in 2.(((True \vee (p \ V0t)) \Leftrightarrow True) \wedge (((p \ V0t) \vee True) \Leftrightarrow True) \wedge (((False \vee (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \vee False) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \vee (p \ V0t)) \Leftrightarrow (p \ V0t)))))) \quad (51)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p \ V0t)) \Leftrightarrow True) \wedge (((p \ V0t) \Rightarrow (p \ V0t)) \Leftrightarrow True) \wedge (((p \ V0t) \Rightarrow False) \Leftrightarrow (\neg(p \ V0t)))))) \quad (52)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p \ V0t))) \Leftrightarrow (p \ V0t)) \wedge ((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (53)$$

Assume the following.

$$\forall A\_27a.nonempty \ A\_27a \Rightarrow (\forall V0x \in A\_27a.(V0x = V0x)) \quad (54)$$

Assume the following.

$$\forall A\_27a.nonempty \ A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow True)) \quad (55)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. (\forall V1y \in A\_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (56)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow (\forall V0f \in (A\_27b^{A\_27a}). (\forall V1g \in (A\_27b^{A\_27a}). ((V0f = V1g) \Leftrightarrow (\forall V2x \in A\_27a. ((ap\ V0f\ V2x) = (ap\ V1g\ V2x)))))) \quad (57)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg(p\ V0t)))))) \quad (58)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0t1 \in A\_27a. (\forall V1t2 \in A\_27a. (((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ c\_2Ebool\_2ET)\ V0t1)\ V1t2) = V0t1) \wedge ((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ c\_2Ebool\_2EF)\ V0t1)\ V1t2) = V1t2)))) \quad (59)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in (2^{A\_27a}). (\forall V1Q \in 2. (((\forall V2x \in A\_27a. (p\ (ap\ V0P\ V2x))) \wedge (p\ V1Q)) \Leftrightarrow (\forall V3x \in A\_27a. ((p\ (ap\ V0P\ V3x)) \wedge (p\ V1Q)))))) \quad (60)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in 2. (\forall V1Q \in (2^{A\_27a}). (((p\ V0P) \wedge (\forall V2x \in A\_27a. (p\ (ap\ V1Q\ V2x)))) \Leftrightarrow (\forall V3x \in A\_27a. ((p\ V0P) \wedge (p\ (ap\ V1Q\ V3x)))))) \quad (61)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0Q \in 2. (\forall V1P \in (2^{A\_27a}). (((\forall V2x \in A\_27a. ((p\ (ap\ V1P\ V2x)) \vee (p\ V0Q))) \Leftrightarrow ((\forall V3x \in A\_27a. (p\ (ap\ V1P\ V3x))) \vee (p\ V0Q)))))) \quad (62)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (\forall V2C \in 2. (((p\ V0A) \vee ((p\ V1B) \wedge (p\ V2C))) \Leftrightarrow (((p\ V0A) \vee (p\ V1B)) \wedge ((p\ V0A) \vee (p\ V2C)))))) \quad (63)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (\forall V2C \in 2. (((p\ V1B) \wedge ((p\ V2C) \vee (p\ V0A))) \Leftrightarrow (((p\ V1B) \vee (p\ V0A)) \wedge ((p\ V2C) \vee (p\ V0A)))))) \quad (64)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow (p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (65)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \forall V0b \in 2.(\forall V1f \in (A\_27b^{A\_27a}).(\forall V2g \in (A\_27b^{A\_27a}). \\ & (\forall V3x \in A\_27a.((ap\ (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ (A\_27b^{A\_27a})) \\ & V0b)\ V1f)\ V2g)\ V3x) = (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27b)\ V0b)\ (ap \\ & V1f\ V3x))\ (ap\ V2g\ V3x))))))))) \end{aligned} \quad (66)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \forall V0f \in (A\_27b^{A\_27a}).(\forall V1b \in 2.(\forall V2x \in A\_27a. \\ & (\forall V3y \in A\_27a.((ap\ V0f\ (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a) \\ & V1b)\ V2x)\ V3y) = (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27b)\ V1b)\ (ap\ V0f \\ & V2x))\ (ap\ V0f\ V3y))))))))) \end{aligned} \quad (67)$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in 2.(\forall V1x\_27 \in 2.(\forall V2y \in 2.(\forall V3y\_27 \in \\ & 2.(((p\ V0x) \Leftrightarrow (p\ V1x\_27)) \wedge ((p\ V1x\_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y\_27)))))) \Rightarrow \\ & (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x\_27) \Rightarrow (p\ V3y\_27)))))) \end{aligned} \quad (68)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in 2.(\forall V1Q \in 2. \\ & (\forall V2x \in A\_27a.(\forall V3x\_27 \in A\_27a.(\forall V4y \in A\_27a. \\ & (\forall V5y\_27 \in A\_27a.(((p\ V0P) \Leftrightarrow (p\ V1Q)) \wedge (((p\ V1Q) \Rightarrow (V2x = V3x\_27)) \wedge \\ & ((\neg(p\ V1Q)) \Rightarrow (V4y = V5y\_27)))))) \Rightarrow ((ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a) \\ & V0P)\ V2x)\ V4y) = (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ A\_27a)\ V1Q)\ V3x\_27) \\ & V5y\_27))))))))) \end{aligned} \quad (69)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.((ap\ (c\_2Ecombin\_2EI\ A\_27a)\ V0x) = V0x)) \quad (70)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \forall V0f \in (A\_27b^{A\_27a}).(((ap\ (ap\ (c\_2Ecombin\_2Eo\ A\_27a\ A\_27b \\ & A\_27b)\ (c\_2Ecombin\_2EI\ A\_27b))\ V0f) = V0f) \wedge ((ap\ (ap\ (c\_2Ecombin\_2Eo \\ & A\_27a\ A\_27b\ A\_27a)\ V0f)\ (c\_2Ecombin\_2EI\ A\_27a)) = V0f))) \end{aligned} \quad (71)$$

Assume the following.

$$(\forall V0x \in ty\_2Erealx\_2Ereal.((\neg((ap\ c\_2Eextreal\_2ENormal\ V0x) = c\_2Eextreal\_2ENegInf)) \wedge (\neg((ap\ c\_2Eextreal\_2ENormal\ V0x) = c\_2Eextreal\_2EPosInf)))) \quad (72)$$

Assume the following.

$$(\forall V0n \in ty\_2Enum\_2Enum.((\neg((ap\ c\_2Eextreal\_2Eextreal\_of\_num\ V0n) = c\_2Eextreal\_2ENegInf)) \wedge (\neg((ap\ c\_2Eextreal\_2Eextreal\_of\_num\ V0n) = c\_2Eextreal\_2EPosInf)))) \quad (73)$$

Assume the following.

$$(\forall V0x \in ty\_2Eextreal\_2Eextreal.((ap\ (ap\ c\_2Eextreal\_2Eextreal\_mul\ V0x) (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0)) = (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))) \quad (74)$$

Assume the following.

$$(\forall V0x \in ty\_2Eextreal\_2Eextreal.((ap\ (ap\ c\_2Eextreal\_2Eextreal\_mul\ (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))\ V0x) = (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))) \quad (75)$$

Assume the following.

$$(\forall V0x \in ty\_2Eextreal\_2Eextreal.((ap\ (ap\ c\_2Eextreal\_2Eextreal\_mul\ V0x) (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ (ap\ c\_2Earithmic\_2ENUMERAL\ (ap\ c\_2Earithmic\_2EBIT1\ c\_2Earithmic\_2EZERO)))) = V0x)) \quad (76)$$

Assume the following.

$$(\forall V0x \in ty\_2Eextreal\_2Eextreal.(p\ (ap\ (ap\ c\_2Eextreal\_2Eextreal\_le\ V0x)\ V0x))) \quad (77)$$

Assume the following.

$$(\forall V0x \in ty\_2Eextreal\_2Eextreal.(((ap\ c\_2Eextreal\_2Eextreal\_abs\ V0x) = V0x) \Leftrightarrow (p\ (ap\ (ap\ c\_2Eextreal\_2Eextreal\_le\ (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))\ V0x)))) \quad (78)$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A_{.27a}}) (ty\_2Epair\_2Eprod (2^{(2^{A_{.27a}})}) (ty\_2Erealax\_2Ereal^{(2^{A_{.27a}})}))). \\
& (\forall V1f \in (ty\_2Eextreal\_2Eextreal^{A_{.27a}}).(((p (ap (c\_2Emeasure\_2Emeasure\_space \\
& A_{.27a}) V0m)) \wedge (\forall V2x \in A_{.27a}.(p (ap (ap c\_2Eextreal\_2Eextreal\_le \\
& (ap c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0)) (ap V1f V2x)))))) \Rightarrow \\
& ((ap (ap (c\_2Elebesgue\_2Epos\_fn\_integral\ A_{.27a}) V0m) V1f) = \\
& (ap (ap (c\_2Elebesgue\_2Epos\_fn\_integral\ A_{.27a}) V0m) (\lambda V3x \in \\
& A_{.27a}.(ap (ap c\_2Eextreal\_2Eextreal\_mul (ap V1f V3x)) (ap (ap \\
& (c\_2Emeasure\_2Eindicator\_fn\ A_{.27a}) (ap (c\_2Emeasure\_2Em\_space \\
& A_{.27a}) V0m)) V3x)))))))))
\end{aligned} \tag{79}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A_{.27a}}) (ty\_2Epair\_2Eprod (2^{(2^{A_{.27a}})}) (ty\_2Erealax\_2Ereal^{(2^{A_{.27a}})}))). \\
& (\forall V1f \in (ty\_2Eextreal\_2Eextreal^{A_{.27a}}).(((p (ap (c\_2Emeasure\_2Emeasure\_space \\
& A_{.27a}) V0m)) \wedge (\forall V2x \in A_{.27a}.(p (ap (ap c\_2Eextreal\_2Eextreal\_le \\
& (ap c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0)) (ap V1f V2x)))))) \Rightarrow \\
& ((p (ap (ap (c\_2Elebesgue\_2Eintegrable\ A_{.27a}) V0m) V1f)) \Leftrightarrow ((p ( \\
& ap (ap (c\_2Ebool\_2EIN (ty\_2Eextreal\_2Eextreal^{A_{.27a}}) V1f) (ap \\
& (ap (c\_2Emeasure\_2Emeasurable\ A_{.27a}\ ty\_2Eextreal\_2Eextreal) \\
& (ap (ap (c\_2Epair\_2E\_2C (2^{A_{.27a}}) (2^{(2^{A_{.27a}})})) (ap (c\_2Emeasure\_2Em\_space \\
& A_{.27a}) V0m)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A_{.27a}) V0m))) \\
& c\_2Emeasure\_2EBorel))) \wedge (\neg((ap (ap (c\_2Elebesgue\_2Epos\_fn\_integral \\
& A_{.27a}) V0m) V1f) = c\_2Eextreal\_2EposInf)))))))))
\end{aligned} \tag{80}$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A_{.27a}}) (ty\_2Epair\_2Eprod (2^{(2^{A_{.27a}})}) (ty\_2Erealax\_2Ereal^{(2^{A_{.27a}})}))). \\
& (\forall V1f \in (ty\_2Eextreal\_2Eextreal^{A_{.27a}}).(\forall V2g \in ( \\
& ty\_2Eextreal\_2Eextreal^{A_{.27a}}).(((p (ap (c\_2Emeasure\_2Emeasure\_space \\
& A_{.27a}) V0m)) \wedge ((p (ap (ap (c\_2Elebesgue\_2Eintegrable\ A_{.27a}) V0m) \\
& V1f)) \wedge ((p (ap (ap (c\_2Ebool\_2EIN (ty\_2Eextreal\_2Eextreal^{A_{.27a}}) \\
& V2g) (ap (ap (c\_2Emeasure\_2Emeasurable\ A_{.27a}\ ty\_2Eextreal\_2Eextreal) \\
& (ap (ap (c\_2Epair\_2E\_2C (2^{A_{.27a}}) (2^{(2^{A_{.27a}})})) (ap (c\_2Emeasure\_2Em\_space \\
& A_{.27a}) V0m)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A_{.27a}) V0m))) \\
& c\_2Emeasure\_2EBorel))) \wedge (\forall V3x \in A_{.27a}.(p (ap (ap c\_2Eextreal\_2Eextreal\_le \\
& (ap c\_2Eextreal\_2Eextreal\_abs (ap V2g V3x)) (ap V1f V3x)))))) \Rightarrow \\
& (p (ap (ap (c\_2Elebesgue\_2Eintegrable\ A_{.27a}) V0m) V2g))))))
\end{aligned} \tag{81}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A-27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A-27a})})\ (ty\_2Erealx\_2Ereal^{(2^{A-27a})}))). \\
& (\forall V1f \in (ty\_2Eextreal\_2Eextreal^{A-27a}).(((p\ (ap\ (c\_2Emeasure\_2Emeasure\_space \\
& A.27a)\ V0m)) \wedge ((p\ (ap\ (ap\ (c\_2ELebesgue\_2Eintegrable\ A.27a)\ V0m) \\
& V1f)) \wedge (\forall V2x \in A.27a.(p\ (ap\ (ap\ c\_2Eextreal\_2Eextreal\_le \\
& (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))\ (ap\ V1f\ V2x)))))) \Rightarrow \\
& ((p\ (ap\ (ap\ (c\_2ELebesgue\_2Eintegrable\ A.27a)\ V0m)\ (\lambda V3x \in A.27a. \\
& (ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ ty\_2Eextreal\_2Eextreal)\ (ap\ (ap\ ( \\
& c\_2Emin\_2E\_3D\ ty\_2Eextreal\_2Eextreal)\ (ap\ V1f\ V3x))\ c\_2Eextreal\_2EPosInf))) \\
& (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))\ (ap\ V1f\ V3x)))) \wedge \\
& ((ap\ (ap\ (c\_2ELebesgue\_2Epos\_fn\_integral\ A.27a)\ V0m)\ V1f) = \\
& (ap\ (ap\ (c\_2ELebesgue\_2Epos\_fn\_integral\ A.27a)\ V0m)\ (\lambda V4x \in \\
& A.27a.(ap\ (ap\ (ap\ (c\_2Ebool\_2ECOND\ ty\_2Eextreal\_2Eextreal)\ ( \\
& ap\ (ap\ (c\_2Emin\_2E\_3D\ ty\_2Eextreal\_2Eextreal)\ (ap\ V1f\ V4x))\ c\_2Eextreal\_2EPosInf)) \\
& (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))\ (ap\ V1f\ V4x))))))))) \\
& \hspace{15em} (82)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A-27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A-27a})})\ (ty\_2Erealx\_2Ereal^{(2^{A-27a})}))). \\
& (\forall V1v \in (ty\_2Epair\_2Eprod\ (2^{A-27a})\ (ty\_2Epair\_2Eprod \\
& (2^{(2^{A-27a})})\ (ty\_2Erealx\_2Ereal^{(2^{A-27a})}))).(((p\ (ap\ (c\_2Emeasure\_2Emeasure\_space \\
& A.27a)\ V0m)) \wedge ((p\ (ap\ (c\_2Emeasure\_2Emeasure\_space\ A.27a)\ V1v)) \wedge \\
& (((ap\ (c\_2Emeasure\_2Em\_space\ A.27a)\ V1v) = (ap\ (c\_2Emeasure\_2Em\_space \\
& A.27a)\ V0m)) \wedge (((ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V1v) = \\
& (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m)) \wedge (p\ (ap\ (ap\ ( \\
& c\_2ELebesgue\_2Emeasure\_absolutely\_continuous\ A.27a)\ V1v) \\
& V0m)))))) \Rightarrow (\exists V2f \in (ty\_2Eextreal\_2Eextreal^{A-27a}).((p \\
& (ap\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Eextreal\_2Eextreal^{A-27a}))\ V2f)\ ( \\
& ap\ (ap\ (c\_2Emeasure\_2Emeasurable\ A.27a\ ty\_2Eextreal\_2Eextreal) \\
& (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A-27a})\ (2^{(2^{A-27a})}))\ (ap\ (c\_2Emeasure\_2Em\_space \\
& A.27a)\ V0m))\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m))) \\
& c\_2Emeasure\_2EBorel))) \wedge ((\forall V3x \in A.27a.(p\ (ap\ (ap\ c\_2Eextreal\_2Eextreal\_le \\
& (ap\ c\_2Eextreal\_2Eextreal\_of\_num\ c\_2Enum\_2E0))\ (ap\ V2f\ V3x)))) \wedge \\
& (\forall V4A \in (2^{A-27a}).((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (2^{A-27a})) \\
& V4A)\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m)))) \Rightarrow ((ap \\
& (ap\ (c\_2ELebesgue\_2Epos\_fn\_integral\ A.27a)\ V0m)\ (\lambda V5x \in \\
& A.27a.(ap\ (ap\ c\_2Eextreal\_2Eextreal\_mul\ (ap\ V2f\ V5x))\ (ap\ (ap \\
& (c\_2Emeasure\_2Eindicator\_fn\ A.27a)\ V4A)\ V5x)))) = (ap\ c\_2Eextreal\_2ENormal \\
& (ap\ (ap\ (c\_2Emeasure\_2Emeasure\ A.27a)\ V1v)\ V4A))))))))) \\
& \hspace{15em} (83)
\end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0x \in (2^{A.27a}). (\forall V1y \in \\ & (2^{(2^{A.27a})}). ((ap\ (c.2Emeasure.2Esubsets\ A.27a)\ (ap\ (ap\ (c.2Epair.2E\_2C \\ & (2^{A.27a})\ (2^{(2^{A.27a})})\ V0x)\ V1y)) = V1y)))) \end{aligned} \quad (84)$$

Assume the following.

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty.2Epair.2Eprod \\ & (2^{A.27a})\ (ty.2Epair.2Eprod\ (2^{(2^{A.27a})})\ (ty.2Erealax.2Ereal^{(2^{A.27a})}))). \\ & ((p\ (ap\ (c.2Emeasure.2Emeasure\_space\ A.27a)\ V0m)) \Rightarrow (p\ (ap\ (ap \\ & (c.2Ebool.2EIN\ (2^{A.27a})\ (ap\ (c.2Emeasure.2Em\_space\ A.27a) \\ & V0m))\ (ap\ (c.2Emeasure.2Emeasurable\_sets\ A.27a)\ V0m)))) \end{aligned} \quad (85)$$

Assume the following.

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0a \in (ty.2Epair.2Eprod \\ & (2^{A.27a})\ (2^{(2^{A.27a})})). (\forall V1f \in (ty.2Eextreal.2Eextreal^{A.27a}). \\ & (\forall V2s \in (2^{A.27a}). (((p\ (ap\ (c.2Emeasure.2Esigma\_algebra \\ & A.27a)\ V0a)) \wedge ((p\ (ap\ (ap\ (c.2Ebool.2EIN\ (ty.2Eextreal.2Eextreal^{A.27a}) \\ & V1f)\ (ap\ (ap\ (c.2Emeasure.2Emeasurable\ A.27a\ ty.2Eextreal.2Eextreal) \\ & V0a)\ c.2Emeasure.2EBorel))) \wedge (p\ (ap\ (ap\ (c.2Ebool.2EIN \\ & V2s)\ (ap\ (c.2Emeasure.2Esubsets\ A.27a)\ V0a)))))) \Rightarrow (p\ (ap\ (ap\ (c.2Ebool.2EIN \\ & (ty.2Eextreal.2Eextreal^{A.27a})\ (\lambda V3x \in A.27a. (ap\ (ap\ c.2Eextreal.2Eextreal\_mul \\ & (ap\ V1f\ V3x))\ (ap\ (ap\ (c.2Emeasure.2Eindicator\_fn\ A.27a)\ V2s) \\ & V3x))))\ (ap\ (ap\ (c.2Emeasure.2Emeasurable\ A.27a\ ty.2Eextreal.2Eextreal) \\ & V0a)\ c.2Emeasure.2EBorel)))))) \end{aligned} \quad (86)$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \quad (87)$$

Assume the following.

$$(\forall V0A \in 2. ((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \quad (88)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\ & (((p\ V0A) \Rightarrow False) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))) \end{aligned} \quad (89)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((\neg(p\ V0A)) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\ & ((p\ V0A) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))) \end{aligned} \quad (90)$$

Assume the following.

$$(\forall V0A \in 2. (((\neg(p\ V0A)) \Rightarrow False) \Rightarrow (((p\ V0A) \Rightarrow False) \Rightarrow False))) \quad (91)$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p \ V0p) \Leftrightarrow ( \\
& (p \ V1q) \Leftrightarrow (p \ V2r))) \Leftrightarrow (((p \ V0p) \vee ((p \ V1q) \vee (p \ V2r))) \wedge (((p \ V0p) \vee ((\neg( \\
& p \ V2r)) \vee (\neg(p \ V1q)))) \wedge (((p \ V1q) \vee ((\neg(p \ V2r)) \vee (\neg(p \ V0p)))) \wedge ((p \ V2r) \vee \\
& ((\neg(p \ V1q)) \vee (\neg(p \ V0p))))))))))
\end{aligned} \tag{92}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p \ V0p) \Leftrightarrow ( \\
& (p \ V1q) \wedge (p \ V2r))) \Leftrightarrow (((p \ V0p) \vee ((\neg(p \ V1q)) \vee (\neg(p \ V2r)))) \wedge (((p \ V1q) \vee \\
& (\neg(p \ V0p))) \wedge ((p \ V2r) \vee (\neg(p \ V0p))))))
\end{aligned} \tag{93}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p \ V0p) \Leftrightarrow ( \\
& (p \ V1q) \vee (p \ V2r))) \Leftrightarrow (((p \ V0p) \vee (\neg(p \ V1q))) \wedge (((p \ V0p) \vee (\neg(p \ V2r))) \wedge \\
& ((p \ V1q) \vee ((p \ V2r) \vee (\neg(p \ V0p))))))
\end{aligned} \tag{94}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p \ V0p) \Leftrightarrow ( \\
& (p \ V1q) \Rightarrow (p \ V2r))) \Leftrightarrow (((p \ V0p) \vee (p \ V1q)) \wedge (((p \ V0p) \vee (\neg(p \ V2r))) \wedge (( \\
& \neg(p \ V1q)) \vee ((p \ V2r) \vee (\neg(p \ V0p))))))
\end{aligned} \tag{95}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (((p \ V0p) \Leftrightarrow (\neg(p \ V1q))) \Leftrightarrow (((p \ V0p) \vee \\
& (p \ V1q)) \wedge ((\neg(p \ V1q)) \vee (\neg(p \ V0p))))))
\end{aligned} \tag{96}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (\forall V3s \in \\
& 2. (((p \ V0p) \Leftrightarrow (ap \ (ap \ (ap \ (c.2Ebool.2ECOND \ 2) \ V1q) \ V2r) \ V3s))) \Leftrightarrow \\
& (((p \ V0p) \vee ((p \ V1q) \vee (\neg(p \ V3s)))) \wedge (((p \ V0p) \vee ((\neg(p \ V2r)) \vee (\neg(p \ V1q)))) \wedge \\
& (((p \ V0p) \vee ((\neg(p \ V2r)) \vee (\neg(p \ V3s)))) \wedge (((\neg(p \ V1q)) \vee ((p \ V2r) \vee (\neg( \\
& p \ V0p)))) \wedge ((p \ V1q) \vee ((p \ V3s) \vee (\neg(p \ V0p))))))
\end{aligned} \tag{97}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p \ V0p) \Rightarrow (p \ V1q))) \Rightarrow (p \ V0p))) \tag{98}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p \ V0p) \Rightarrow (p \ V1q))) \Rightarrow (\neg(p \ V1q)))) \tag{99}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. ((\neg((p \ V0p) \vee (p \ V1q))) \Rightarrow (\neg(p \ V0p)))) \tag{100}$$



Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V1q)))))) \quad (101)$$

Assume the following.

$$(\forall V0p \in 2.((\neg(\neg(p V0p))) \Rightarrow (p V0p))) \quad (102)$$

**Theorem 1**

$$\begin{aligned} & \forall A.27a.nonempty \ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\ & (2^{A-27a}) (ty\_2Epair\_2Eprod (2^{2^{A-27a}}) (ty\_2Erealax\_2Ereal^{(2^{A-27a})}))). \\ & (\forall V1v \in (ty\_2Epair\_2Eprod (2^{A-27a}) (ty\_2Epair\_2Eprod \\ & (2^{(2^{A-27a})}) (ty\_2Erealax\_2Ereal^{(2^{A-27a})}))).(((p (ap (c\_2Emeasure\_2Emeasure\_space \\ & A.27a) V0m)) \wedge ((p (ap (c\_2Emeasure\_2Emeasure\_space A.27a) V1v)) \wedge \\ & (((ap (c\_2Emeasure\_2Em\_space A.27a) V1v) = (ap (c\_2Emeasure\_2Em\_space \\ & A.27a) V0m)) \wedge ((ap (c\_2Emeasure\_2Emeasurable\_sets A.27a) V1v) = \\ & (ap (c\_2Emeasure\_2Emeasurable\_sets A.27a) V0m)) \wedge (p (ap (ap ( \\ & c\_2Elebesgue\_2Emeasure\_absolutely\_continuous A.27a) V1v) \\ & V0m)))))) \Rightarrow (\exists V2f \in (ty\_2Eextreal\_2Eextreal^{A-27a}).((p \\ & (ap (ap (c\_2Ebool\_2EIN (ty\_2Eextreal\_2Eextreal^{A-27a}) V2f) ( \\ & ap (ap (c\_2Emeasure\_2Emeasurable A.27a ty\_2Eextreal\_2Eextreal) \\ & (ap (ap (c\_2Epair\_2E\_2C (2^{A-27a}) (2^{(2^{A-27a})})) (ap (c\_2Emeasure\_2Em\_space \\ & A.27a) V0m)) (ap (c\_2Emeasure\_2Emeasurable\_sets A.27a) V0m))) \\ & c\_2Emeasure\_2EBorel))) \wedge ((\forall V3x \in A.27a.(p (ap (ap c\_2Eextreal\_2Eextreal\_le \\ & (ap c\_2Eextreal\_2Eextreal\_of\_num c\_2Enum\_2E0)) (ap V2f V3x)))) \wedge \\ & ((\forall V4x \in A.27a.(\neg((ap V2f V4x) = c\_2Eextreal\_2EPosInf))) \wedge \\ & (\forall V5A \in (2^{A-27a}).((p (ap (ap (c\_2Ebool\_2EIN (2^{A-27a}) \\ & V5A) (ap (c\_2Emeasure\_2Emeasurable\_sets A.27a) V0m))) \Rightarrow ((ap \\ & (ap (c\_2Elebesgue\_2Epos\_fn\_integral A.27a) V0m) (\lambda V6x \in \\ & A.27a.(ap (ap c\_2Eextreal\_2Eextreal\_mul (ap V2f V6x)) (ap (ap \\ & (c\_2Emeasure\_2Eindicator\_fn A.27a) V5A) V6x)))) = (ap c\_2Eextreal\_2ENormal \\ & (ap (ap (c\_2Emeasure\_2Emeasure A.27a) V1v) V5A)))))))))) \end{aligned}$$