

thm_2Elebesgue_2Eintegrable__add__pos (TMcwf6dAsr1hC8Nt9M8GcsZqEgYi6py8h2C)

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Definition 1 We define `c_2Emin_2E_40` to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p \text{ (ap } P \ x)) \text{ then (the } (\lambda x. x \in A \wedge p \text{ of type } \iota \Rightarrow \iota).$

Definition 2 We define `c_2Emin_2E_3D` to be $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj_o } (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define `c_2Ebool_2E_3F` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } V0P \text{ (ap } (c_2Emin_2E_40 \ A$

Definition 4 We define `c_2Ebool_2E_T` to be $(\text{ap } (\text{ap } (c_2Emin_2E_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x$

Let `ty_2Eextreal_2Eextreal` : ι be given. Assume the following.

$$\text{nonempty } ty_2Eextreal_2Eextreal \tag{1}$$

Let `ty_2Erealax_2Ereal` : ι be given. Assume the following.

$$\text{nonempty } ty_2Erealax_2Ereal \tag{2}$$

Let `c_2Eextreal_2EENormal` : ι be given. Assume the following.

$$c_2Eextreal_2EENormal \in (ty_2Eextreal_2Eextreal^{ty_2Erealax_2Ereal}) \tag{3}$$

Let `c_2Eextreal_2ENegInf` : ι be given. Assume the following.

$$c_2Eextreal_2ENegInf \in ty_2Eextreal_2Eextreal \tag{4}$$

Let `c_2Eextreal_2Eextreal_le` : ι be given. Assume the following.

$$c_2Eextreal_2Eextreal_le \in ((2^{ty_2Eextreal_2Eextreal})^{ty_2Eextreal_2Eextreal}) \tag{5}$$

Definition 5 We define `c_2Ebool_2E_21` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (c_2Emin_2E_3D \ (2^{A-27$

Definition 6 We define `c_2Ebool_2E_F` to be $(\text{ap } (c_2Ebool_2E_21 \ 2) \ (\lambda V0t \in 2.V0t))$.

Definition 7 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2. \lambda Q \in 2. \text{inj_o } (p \ P \Rightarrow \ p \ Q)$ of type ι .

Definition 8 We define c_Ebool_E7E to be $(\lambda V0t \in 2.(ap (ap c_Emin_E3D_3D_3E V0t) c_Ebool_E7E$

Definition 9 We define $c_Eextreal_Eextreal_It$ to be $\lambda V0x \in ty_Eextreal_Eextreal.\lambda V1y \in ty_Eextreal$

Let $c_EEnum_EZERO_REP : \iota$ be given. Assume the following.

$$c_EEnum_EZERO_REP \in \omega \tag{6}$$

Let $ty_EEnum_EEnum : \iota$ be given. Assume the following.

$$nonempty\ ty_EEnum_EEnum \tag{7}$$

Let $c_EEnum_EABS_num : \iota$ be given. Assume the following.

$$c_EEnum_EABS_num \in (ty_EEnum_EEnum^{\omega\omega}) \tag{8}$$

Definition 10 We define c_EEnum_E0 to be $(ap c_EEnum_EABS_num c_EEnum_EZERO_REP)$.

Let $c_Ereal_Ereal_of_num : \iota$ be given. Assume the following.

$$c_Ereal_Ereal_of_num \in (ty_Erealax_Ereal^{ty_EEnum_EEnum}) \tag{9}$$

Definition 11 We define $c_Eextreal_Eextreal_of_num$ to be $\lambda V0n \in ty_EEnum_EEnum.(ap c_Eextreal$

Let $c_Eextreal_Eextreal_ainv : \iota$ be given. Assume the following.

$$c_Eextreal_Eextreal_ainv \in (ty_Eextreal_Eextreal^{ty_Eextreal_Eextreal}) \tag{10}$$

Definition 12 We define $c_Ebool_E2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_Ebool_E21\ 2) (\lambda V2t \in$

Definition 13 We define c_Ebool_ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.($

Definition 14 We define $c_Emeasure_Efn_minus$ to be $\lambda A_27a : \iota.\lambda V0f \in (ty_Eextreal_Eextreal^{A_27a})$

Definition 15 We define $c_Emeasure_Efn_plus$ to be $\lambda A_27a : \iota.\lambda V0f \in (ty_Eextreal_Eextreal^{A_27a})$.

Let $c_Eextreal_EPosInf : \iota$ be given. Assume the following.

$$c_Eextreal_EPosInf \in ty_Eextreal_Eextreal \tag{11}$$

Let $ty_Epair_Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_Epair_Eprod\ A0\ A1) \tag{12}$$

Let $c_Emeasure_Em_space : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Emeasure_Em_space\ A_27a \in ((2^{A_27a})(ty_Epair_Eprod\ (2^{A_27a})\ (ty_Epair_Eprod\ (2^{(2^{A_27a})})\ (ty_Erealax_Ereal^{(2^{A_27a})})))) \tag{13}$$

Definition 16 We define c_Ebool_2EIN to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. (\lambda V1f \in (2^{A_27a}). (ap\ V1f\ V0x)))$

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a. nonempty\ A_27a \Rightarrow \forall A_27b. nonempty\ A_27b \Rightarrow c_2Epair_2EABS_prod \\ A_27a\ A_27b \in ((ty_2Epair_2Eprod\ A_27a\ A_27b)^{(2^{A_27b}})^{A_27a}) \end{aligned} \quad (14)$$

Definition 17 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0x \in A_27a. \lambda V1y \in A_27b. (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27b))\ V0x\ V1y$

Let $c_2Epred_set_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a. nonempty\ A_27a \Rightarrow \forall A_27b. nonempty\ A_27b \Rightarrow c_2Epred_set_2EGSPEC \\ A_27a\ A_27b \in ((2^{A_27a})^{(ty_2Epair_2Eprod\ A_27a\ 2)^{A_27b}}) \end{aligned} \quad (15)$$

Definition 18 We define $c_2Epred_set_2EIMAGE$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in (A_27b^{A_27a}). \lambda V1s \in A_27b. (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27b))\ V0f\ V1s$

Definition 19 We define $c_2Epred_set_2EBIGUNION$ to be $\lambda A_27a : \iota. \lambda V0P \in (2^{(2^{A_27a})}). (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27a))\ V0P$

Definition 20 We define $c_2Epred_set_2EEMPTY$ to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. c_2Ebool_2EF)$.

Definition 21 We define $c_2Epred_set_2EINTER$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27a))\ V0s\ V1t$

Definition 22 We define $c_2Epred_set_2EDISJOINT$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27a))\ V0s\ V1t$

Let $ty_2Ehreal_2Ehreal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ehreal_2Ehreal \quad (16)$$

Let $c_2Erealx_2Ereal_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Erealx_2Ereal_REP_CLASS \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{ty_2Erealx_2Ereal_REP_CLASS}) \quad (17)$$

Definition 23 We define $c_2Erealx_2Ereal_REP$ to be $\lambda V0a \in ty_2Erealx_2Ereal. (ap\ (c_2Emin_2E_40\ ty_2Erealx_2Ereal))\ V0a$

Let $c_2Erealx_2Etreal_lt : \iota$ be given. Assume the following.

$$c_2Erealx_2Etreal_lt \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)}) \quad (18)$$

Definition 24 We define $c_2Erealx_2Ereal_lt$ to be $\lambda V0T1 \in ty_2Erealx_2Ereal. \lambda V1T2 \in ty_2Erealx_2Ereal. (ap\ (c_2Emin_2E_40\ ty_2Erealx_2Ereal))\ V0T1\ V1T2$

Definition 25 We define $c_2Ereal_2Ereal_lte$ to be $\lambda V0x \in ty_2Erealx_2Ereal. \lambda V1y \in ty_2Erealx_2Ereal. (ap\ (c_2Emin_2E_40\ ty_2Erealx_2Ereal))\ V0x\ V1y$

Definition 26 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap\ (c_2Ebool_2E_21\ 2))\ V0t1\ V1t2))$

Definition 27 We define $c_2Epred_set_2EINSERT$ to be $\lambda A_27a : \iota. \lambda V0x \in A_27a. \lambda V1s \in (2^{A_27a}). (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27a))\ V0x\ V1s$

Definition 28 We define $c_2Epred_set_2EFINITE$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). (ap\ (c_2Ebool_2E_21\ 2))\ V0s$

Let $c_2Emeasure_2Emeasurable_sets : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow c_2Emeasure_2Emeasurable_sets \\ A_27a \in & ((2^{(2^{A_27a})})^{(ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2Epair_2Eprod\ (2^{(2^{A_27a})})\ (ty_2Erealx_2Ereal^{(2^{A_27a})})))}) \end{aligned} \quad (19)$$

Definition 29 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (20)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (21)$$

Definition 30 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (22)$$

Definition 31 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earithmetic$

Definition 32 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 33 We define $c_2Emeasure_2Eindicator_fn$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).(\lambda V1x \in A_27a.(ap$

Let $c_2Eextreal_2Eextreal_mul : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_mul \in ((ty_2Eextreal_2Eextreal^{ty_2Eextreal_2Eextreal})^{ty_2Eextreal_2Eextreal}) \quad (23)$$

Let $c_2Eextreal_2Eextreal_add : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_add \in ((ty_2Eextreal_2Eextreal^{ty_2Eextreal_2Eextreal})^{ty_2Eextreal_2Eextreal}) \quad (24)$$

Let $c_2Epred_set_2EITSET : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epred_set_2EITSET \\ A_27a\ A_27b \in & (((A_27b^{A_27b})^{(2^{A_27a})})^{((A_27b^{A_27b})^{A_27a})}) \end{aligned} \quad (25)$$

Definition 34 We define $c_2Eextreal_2EEXTREAL_SUM_IMAGE$ to be $\lambda A_27a : \iota.\lambda V0f \in (ty_2Eextreal$

Definition 35 We define $c_2Emeasure_2Epos_simple_fn$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^A$

Let $c_2Epair_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2ESND\ A_27a\ A_27b \in (A_27b^{(ty_2Epair_2Eprod\ A_27a\ A_27b)})$$
(26)

Let $c_2Epair_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2EFST\ A_27a\ A_27b \in (A_27a^{(ty_2Epair_2Eprod\ A_27a\ A_27b)})$$
(27)

Definition 36 We define $c_2Epair_2EUNCURRY$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in ((A_27c)^{A_27a})$

Definition 37 We define $c_2Elebesgue_2Epsfs$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^{A_27a}))\ (ty_2Epair_2Eprod\ (2^{A_27a}))$

Let $c_2Emeasure_2Emeasure : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Emeasure_2Emeasure\ A_27a \in ((ty_2Erealax_2Ereal^{(2^{A_27a})})^{(ty_2Epair_2Eprod\ (2^{A_27a}))}\ (ty_2Epair_2Eprod\ (2^{(2^{A_27a})}))\ (ty_2Erealax_2Ereal^{(2^{A_27a})}))$$
(28)

Let $c_2Erealax_2Etrealmul : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealmul \in (((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}$$
(29)

Let $c_2Erealax_2Etrealeq : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealeq \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}$$
(30)

Let $c_2Erealax_2Ereal_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_ABS_CLASS \in (ty_2Erealax_2Ereal^{(2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}$$
(31)

Definition 38 We define $c_2Erealax_2Ereal_ABS$ to be $\lambda V0r \in (ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)$

Definition 39 We define $c_2Erealax_2Erealmul$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.\lambda V1T2 \in ty_2Erealax_2Ereal$

Let $c_2Erealax_2Etrealmul_add : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealmul_add \in (((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}$$
(32)

Definition 40 We define $c_2Erealax_2Ereal_add$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.\lambda V1T2 \in ty_2Erealax_2Ereal$

Definition 41 We define $c_2Ereal_sigma_2EREAL_SUM_IMAGE$ to be $\lambda A_27a : \iota.\lambda V0f \in (ty_2Erealax_2Ereal)$

Definition 42 We define $c_2Elebesgue_2Epos_simple_fn_integral$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^{A_27a}))\ (ty_2Epair_2Eprod\ (2^{A_27a}))$

Definition 43 We define $c_2E\text{lebesgue_2Epsfis}$ to be $\lambda A_27a : \iota. \lambda V0m \in (ty_2E\text{pair_2Eprod } (2^{A-27a}) (ty_2E$

Definition 44 We define $c_2E\text{real_2Esup}$ to be $\lambda V0P \in (2^{ty_2E\text{realax_2Ereal}}). (ap (c_2E\text{min_2E40 } ty_2E\text{real}$

Definition 45 We define $c_2E\text{extreal_2Eextreal_sup}$ to be $\lambda V0p \in (2^{ty_2E\text{extreal_2Eextreal}}). (ap (ap (ap (c_2E$

Definition 46 We define $c_2E\text{lebesgue_2Epos_fn_integral}$ to be $\lambda A_27a : \iota. \lambda V0m \in (ty_2E\text{pair_2Eprod } (2^{A-27a})$

Definition 47 We define $c_2E\text{pred_set_2EUNIV}$ to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a.c_2E\text{bool_2ET})$.

Let $c_2E\text{measure_2Esubsets} : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2E\text{measure_2Esubsets } A_27a \in ((2^{(2^{A-27a})}) (ty_2E\text{pair_2Eprod } (2^{A-27a}) (2^{(2^{A-27a})})) \quad (33)$$

Definition 48 We define $c_2E\text{pred_set_2ESUBSET}$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A-27a}). \lambda V1t \in (2^{A-27a}). (ap (c_2E$

Definition 49 We define $c_2E\text{pred_set_2EINJ}$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in (A_27b^{A-27a}). \lambda V1s \in (2^{A-27a})$

Definition 50 We define $c_2E\text{pred_set_2Ecountable}$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A-27a}). (ap (c_2E\text{bool_2E3F}$

Definition 51 We define $c_2E\text{pred_set_2EUNION}$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A-27a}). \lambda V1t \in (2^{A-27a}). (ap (c_2E$

Let $c_2E\text{measure_2Espace} : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2E\text{measure_2Espace } A_27a \in ((2^{A-27a}) (ty_2E\text{pair_2Eprod } (2^{A-27a}) (2^{(2^{A-27a})}))) \quad (34)$$

Definition 52 We define $c_2E\text{pred_set_2EDIFF}$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A-27a}). \lambda V1t \in (2^{A-27a}). (ap (c_2E$

Definition 53 We define $c_2E\text{measure_2Esubset_class}$ to be $\lambda A_27a : \iota. \lambda V0sp \in (2^{A-27a}). \lambda V1sts \in (2^{(2^{A-27a})})$

Definition 54 We define $c_2E\text{measure_2Ealgebra}$ to be $\lambda A_27a : \iota. \lambda V0a \in (ty_2E\text{pair_2Eprod } (2^{A-27a}) (2^{(2^{A-27a})})$

Definition 55 We define $c_2E\text{measure_2Esigma_algebra}$ to be $\lambda A_27a : \iota. \lambda V0a \in (ty_2E\text{pair_2Eprod } (2^{A-27a})$

Definition 56 We define $c_2E\text{pred_set_2EBIGINTER}$ to be $\lambda A_27a : \iota. \lambda V0P \in (2^{(2^{A-27a})}). (ap (c_2E\text{pred_s}$

Definition 57 We define $c_2E\text{measure_2Esigma}$ to be $\lambda A_27a : \iota. \lambda V0sp \in (2^{A-27a}). \lambda V1st \in (2^{(2^{A-27a})}). (ap ($

Definition 58 We define $c_2E\text{measure_2EBorel}$ to be $(ap (ap (c_2E\text{measure_2Esigma } ty_2E\text{extreal_2Eextreal}$

Definition 59 We define $c_2E\text{pred_set_2EPREIMAGE}$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in (A_27b^{A-27a}). \lambda V$

Definition 60 We define $c_2E\text{pred_set_2EFUNSET}$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0P \in (2^{A-27a}). \lambda V1Q \in ($

Definition 61 We define $c_2E\text{measure_2Emeasurable}$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0a \in (ty_2E\text{pair_2Eprod}$

Definition 62 We define $c_2E\text{lebesgue_2Eintegrable}$ to be $\lambda A_27a : \iota. \lambda V0m \in (ty_2E\text{pair_2Eprod } (2^{A-27a})$

Definition 63 We define $c_2Ecombin_2Eo$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in (A_27b^{A_27c}).\lambda V1$.

Let $c_2Ereal_2Esum : \iota$ be given. Assume the following.

$$c_2Ereal_2Esum \in ((ty_2Erealax_2Ereal^{(ty_2Erealax_2Ereal^{ty_2Eenum_2Eenum})})^{(ty_2Epair_2Eprod\ ty_2Eenum_2Eenum)}) (35)$$

Definition 64 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Eenum_2Eenum.\lambda V1n \in ty_2Eenum_2Eenum$.

Definition 65 We define $c_2Earithmetic_2E_3E$ to be $\lambda V0m \in ty_2Eenum_2Eenum.\lambda V1n \in ty_2Eenum_2Eenum$.

Definition 66 We define $c_2Earithmetic_2E_3E_3D$ to be $\lambda V0m \in ty_2Eenum_2Eenum.\lambda V1n \in ty_2Eenum_2Eenum$.

Let $c_2Erealax_2Etrealm_neg : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealm_neg \in ((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}) (36)$$

Definition 67 We define $c_2Erealax_2Ereal_neg$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.(ap\ c_2Erealax_2Ereal$.

Definition 68 We define $c_2Ereal_2Ereal_sub$ to be $\lambda V0x \in ty_2Erealax_2Ereal.\lambda V1y \in ty_2Erealax_2Ereal$.

Definition 69 We define c_2Ereal_2Eabs to be $\lambda V0x \in ty_2Erealax_2Ereal.(ap\ (ap\ (ap\ (c_2Ebool_2ECONI$

Let $ty_2Emetric_2Emetric : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Emetric_2Emetric\ A0) (37)$$

Let $c_2Emetric_2Emetric : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Emetric_2Emetric\ A_27a \in ((ty_2Emetric_2Emetric\ A_27a)^{(ty_2Erealax_2Ereal^{(ty_2Epair_2Eprod\ A_27a\ A_27a)})}) (38)$$

Definition 70 We define $c_2Emetric_2Emr1$ to be $(ap\ (c_2Emetric_2Emetric\ ty_2Erealax_2Ereal)\ (ap\ (c$

Let $c_2Emetric_2Edist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Emetric_2Edist\ A_27a \in ((ty_2Erealax_2Ereal^{(ty_2Epair_2Eprod\ A_27a\ A_27a)}) (39)$$

Let $ty_2Etopology_2Etopology : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Etopology_2Etopology\ A0) (40)$$

Let $c_2Etopology_2Etopology : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Etopology_2Etopology\ A_27a \in ((ty_2Etopology_2Etopology\ A_27a)^{(2^{(2^{A_27a})})}) (41)$$

Definition 71 We define $c_2Emetric_2Emtop$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Emetric_2Emetric\ A_27a).(ap$

Let $c_2Enets_2Etends : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Enets_2Etends \\ & A_27a\ A_27b \in (((2^{(ty_2Epair_2Eprod\ (ty_2Etopology_2Etopology\ A_27a)\ (2^{A_27b})^{A_27b})}))_{A_27a})_{(A_27a)^{A_27b}}) \end{aligned} \quad (42)$$

Definition 72 We define $c_2Eseq_2E_2D_2D_3E$ to be $\lambda V0x \in (ty_2Erealax_2Ereal^{ty_2Enum_2Enum}).\lambda V1x$

Definition 73 We define c_2Eseq_2Esums to be $\lambda V0f \in (ty_2Erealax_2Ereal^{ty_2Enum_2Enum}).\lambda V1s \in ty_2E$

Definition 74 We define $c_2Emeasure_2Ecountably_additive$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod$

Definition 75 We define $c_2Emeasure_2Epositive$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2E$

Definition 76 We define $c_2Emeasure_2Emeasure_space$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2E$

Assume the following.

$$True \quad (43)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p\ V0t1) \Rightarrow (p\ V1t2)) \Rightarrow (((p \\ & V1t2) \Rightarrow (p\ V0t1)) \Rightarrow ((p\ V0t1) \Leftrightarrow (p\ V1t2)))))) \end{aligned} \quad (44)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p\ V0t))) \quad (45)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in \\ & A_27a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \end{aligned} \quad (46)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (47)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow \\ & True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge ((\\ & (p\ V0t) \Rightarrow False) \Leftrightarrow (\neg (p\ V0t)))))) \end{aligned} \quad (48)$$

Assume the following.

$$\begin{aligned} & ((\forall V0t \in 2.((\neg (\neg (p\ V0t))) \Leftrightarrow (p\ V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge \\ & ((\neg False) \Leftrightarrow True))) \end{aligned} \quad (49)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.(V0x = V0x)) \quad (50)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (51)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg(\\ & p\ V0t)))))) \end{aligned} \quad (52)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p\ V0A) \vee (\\ & (p\ V1B) \wedge (p\ V2C))) \Leftrightarrow (((p\ V0A) \vee (p\ V1B)) \wedge ((p\ V0A) \vee (p\ V2C)))))) \end{aligned} \quad (53)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p\ V1B) \wedge \\ & (p\ V2C)) \vee (p\ V0A)) \Leftrightarrow (((p\ V1B) \vee (p\ V0A)) \wedge ((p\ V2C) \vee (p\ V0A)))))) \end{aligned} \quad (54)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p\ V0t1) \Rightarrow \\ & (p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \end{aligned} \quad (55)$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in 2.(\forall V1x_27 \in 2.(\forall V2y \in 2.(\forall V3y_27 \in \\ & 2.(((p\ V0x) \Leftrightarrow (p\ V1x_27)) \wedge ((p\ V1x_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y_27)))) \Rightarrow \\ & (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x_27) \Rightarrow (p\ V3y_27)))))) \end{aligned} \quad (56)$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in ty_2Eextreal_2Eextreal.(\forall V1y \in ty_2Erealax_2Ereal. \\ & ((p\ (ap\ (ap\ c_2Eextreal_2Eextreal_lt\ c_2Eextreal_2ENegInf) \\ & (ap\ c_2Eextreal_2ENormal\ V1y))) \wedge ((p\ (ap\ (ap\ c_2Eextreal_2Eextreal_lt \\ & (ap\ c_2Eextreal_2ENormal\ V1y))\ c_2Eextreal_2EPosInf)) \wedge ((p\ (\\ & ap\ (ap\ c_2Eextreal_2Eextreal_lt\ c_2Eextreal_2ENegInf)\ c_2Eextreal_2EPosInf)) \wedge \\ & ((\neg(p\ (ap\ (ap\ c_2Eextreal_2Eextreal_lt\ V0x)\ c_2Eextreal_2ENegInf)))) \wedge \\ & ((\neg(p\ (ap\ (ap\ c_2Eextreal_2Eextreal_lt\ c_2Eextreal_2EPosInf) \\ & V0x))) \wedge (((\neg(V0x = c_2Eextreal_2EPosInf)) \Leftrightarrow (p\ (ap\ (ap\ c_2Eextreal_2Eextreal_lt \\ & V0x)\ c_2Eextreal_2EPosInf))) \wedge ((\neg(V0x = c_2Eextreal_2ENegInf)) \Leftrightarrow \\ & (p\ (ap\ (ap\ c_2Eextreal_2Eextreal_lt\ c_2Eextreal_2ENegInf)\ V0x)))))) \end{aligned} \quad (57)$$

Assume the following.

$$\begin{aligned}
& (\forall V0x \in ty_2Eextreal_2Eextreal. (\forall V1y \in ty_2Eextreal_2Eextreal. \\
& (((p (ap (ap (ap c_2Eextreal_2Eextreal_le (ap c_2Eextreal_2Eextreal_of_num \\
& \quad c_2Enum_2E0)) V0x)) \wedge (p (ap (ap c_2Eextreal_2Eextreal_le (ap \\
& \quad c_2Eextreal_2Eextreal_of_num c_2Enum_2E0)) V1y))) \Rightarrow (p (ap \\
& \quad (ap c_2Eextreal_2Eextreal_le (ap c_2Eextreal_2Eextreal_of_num \\
& \quad c_2Enum_2E0)) (ap (ap c_2Eextreal_2Eextreal_add V0x) V1y))))))
\end{aligned} \tag{58}$$

Assume the following.

$$\begin{aligned}
& (\forall V0w \in ty_2Eextreal_2Eextreal. (\forall V1x \in ty_2Eextreal_2Eextreal. \\
& \quad (\forall V2y \in ty_2Eextreal_2Eextreal. (\forall V3z \in ty_2Eextreal_2Eextreal. \\
& \quad (((p (ap (ap c_2Eextreal_2Eextreal_lt V0w) V1x)) \wedge (p (ap (ap c_2Eextreal_2Eextreal_lt \\
& \quad V2y) V3z))) \Rightarrow (p (ap (ap c_2Eextreal_2Eextreal_lt (ap (ap c_2Eextreal_2Eextreal_add \\
& \quad V0w) V2y)) (ap (ap c_2Eextreal_2Eextreal_add V1x) V3z))))))
\end{aligned} \tag{59}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0m \in (ty_2Epair_2Eprod \\
& \quad (2^{A_27a}) (ty_2Epair_2Eprod (2^{(2^{A_27a})}) (ty_2Erealax_2Ereal^{(2^{A_27a})}))). \\
& \quad (\forall V1f \in (ty_2Eextreal_2Eextreal^{A_27a}). (\forall V2g \in (\\
& \quad ty_2Eextreal_2Eextreal^{A_27a}). (((p (ap (c_2Emeasure_2Emeasure_space \\
& \quad A_27a) V0m)) \wedge ((\forall V3x \in A_27a. ((p (ap (ap c_2Eextreal_2Eextreal_le \\
& \quad (ap c_2Eextreal_2Eextreal_of_num c_2Enum_2E0)) (ap V1f) V3x))) \wedge \\
& \quad (p (ap (ap c_2Eextreal_2Eextreal_le (ap c_2Eextreal_2Eextreal_of_num \\
& \quad c_2Enum_2E0)) (ap V2g) V3x)))))) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal^{A_27a})) \\
& \quad V1f) (ap (ap (c_2Emeasure_2Emeasurable A_27a ty_2Eextreal_2Eextreal) \\
& \quad (ap (ap (c_2Epair_2E_2C (2^{A_27a}) (2^{(2^{A_27a})})) (ap (c_2Emeasure_2Em_space \\
& \quad A_27a) V0m)) (ap (c_2Emeasure_2Emeasurable_sets A_27a) V0m))) \\
& \quad c_2Emeasure_2EBorel))) \wedge (p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal^{A_27a})) \\
& \quad V2g) (ap (ap (c_2Emeasure_2Emeasurable A_27a ty_2Eextreal_2Eextreal) \\
& \quad (ap (ap (c_2Epair_2E_2C (2^{A_27a}) (2^{(2^{A_27a})})) (ap (c_2Emeasure_2Em_space \\
& \quad A_27a) V0m)) (ap (c_2Emeasure_2Emeasurable_sets A_27a) V0m))) \\
& \quad c_2Emeasure_2EBorel)))))) \Rightarrow ((ap (ap (c_2Elebesgue_2Epos_fn_integral \\
& \quad A_27a) V0m) (\lambda V4x \in A_27a. (ap (ap c_2Eextreal_2Eextreal_add \\
& \quad (ap V1f) V4x)) (ap V2g) V4x))) = (ap (ap c_2Eextreal_2Eextreal_add \\
& \quad (ap (ap (c_2Elebesgue_2Epos_fn_integral A_27a) V0m) V1f)) (\\
& \quad ap (ap (c_2Elebesgue_2Epos_fn_integral A_27a) V0m) V2g))))))
\end{aligned} \tag{60}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty_2Epair_2Eprod \\
& (2^{A.27a}) (ty_2Epair_2Eprod (2^{(2^{A.27a})}) (ty_2Erealx_2Ereal^{(2^{A.27a})}))). \\
& (\forall V1f \in (ty_2Eextreal_2Eextreal^{A.27a}).(((p (ap (c_2Emeasure_2Emeasure_space \\
& A.27a) V0m)) \wedge (\forall V2x \in A.27a.(p (ap (ap c_2Eextreal_2Eextreal_le \\
& (ap c_2Eextreal_2Eextreal_of_num\ c_2Enum_2E0)) (ap V1f V2x)))))) \Rightarrow \\
& ((p (ap (ap (c_2Elebesgue_2Eintegrable\ A.27a) V0m) V1f)) \Leftrightarrow ((p (\\
& ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal^{A.27a}) V1f) (ap \\
& (ap (c_2Emeasure_2Emeasurable\ A.27a\ ty_2Eextreal_2Eextreal) \\
& (ap (ap (c_2Epair_2E.2C (2^{A.27a}) (2^{(2^{A.27a})})) (ap (c_2Emeasure_2Em_space \\
& A.27a) V0m)) (ap (c_2Emeasure_2Emeasurable_sets\ A.27a) V0m))) \\
& c_2Emeasure_2EBorel))) \wedge (\neg((ap (ap (c_2Elebesgue_2Epos_fn_integral \\
& A.27a) V0m) V1f) = c_2Eextreal_2EPosInf))))))
\end{aligned} \tag{61}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0a \in (ty_2Epair_2Eprod \\
& (2^{A.27a}) (2^{(2^{A.27a})})).(\forall V1f \in (ty_2Eextreal_2Eextreal^{A.27a}). \\
& (\forall V2g \in (ty_2Eextreal_2Eextreal^{A.27a}).(\forall V3h \in (\\
& ty_2Eextreal_2Eextreal^{A.27a}).(((p (ap (c_2Emeasure_2Esigma_algebra \\
& A.27a) V0a)) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal^{A.27a}) \\
& V1f) (ap (ap (c_2Emeasure_2Emeasurable\ A.27a\ ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel))) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal^{A.27a}) \\
& V2g) (ap (ap (c_2Emeasure_2Emeasurable\ A.27a\ ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel))) \wedge (\forall V4x \in A.27a.((p (ap (ap (\\
& c_2Ebool_2EIN\ A.27a) V4x) (ap (c_2Emeasure_2Espace\ A.27a) V0a)))) \Rightarrow \\
& ((ap V3h V4x) = (ap (ap c_2Eextreal_2Eextreal_add (ap V1f V4x)) \\
& (ap V2g V4x))))))))) \Rightarrow (p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal^{A.27a}) \\
& V3h) (ap (ap (c_2Emeasure_2Emeasurable\ A.27a\ ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel))))))
\end{aligned} \tag{62}$$

Assume the following.

$$(\forall V0t \in 2.((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \tag{63}$$

Assume the following.

$$(\forall V0A \in 2.((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \tag{64}$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\
& (((p\ V0A) \Rightarrow False) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False))))))
\end{aligned} \tag{65}$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2.(\forall V1B \in 2.(((\neg((\neg(p\ V0A)) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\
& ((p\ V0A) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False))))))
\end{aligned} \tag{66}$$

Assume the following.

$$(\forall V0A \in 2.((\neg(p V0A)) \Rightarrow False) \Rightarrow ((p V0A) \Rightarrow False) \Rightarrow False)) \quad (67)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (\\ & (p V1q) \Leftrightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee ((p V1q) \vee (p V2r))) \wedge (((p V0p) \vee (\neg(\\ & p V2r)) \vee (\neg(p V1q)))) \wedge (((p V1q) \vee (\neg(p V2r)) \vee (\neg(p V0p)))) \wedge ((p V2r) \vee \\ & ((\neg(p V1q)) \vee (\neg(p V0p)))))))))) \end{aligned} \quad (68)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (\\ & (p V1q) \wedge (p V2r))) \Leftrightarrow (((p V0p) \vee (\neg(p V1q)) \vee (\neg(p V2r))) \wedge (((p V1q) \vee \\ & (\neg(p V0p))) \wedge ((p V2r) \vee (\neg(p V0p)))))))) \end{aligned} \quad (69)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (\\ & (p V1q) \vee (p V2r))) \Leftrightarrow (((p V0p) \vee (\neg(p V1q))) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge \\ & ((p V1q) \vee ((p V2r) \vee (\neg(p V0p)))))))) \end{aligned} \quad (70)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (\\ & (p V1q) \Rightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge ((\\ & \neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p)))))))) \end{aligned} \quad (71)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(((p V0p) \Leftrightarrow (\neg(p V1q))) \Leftrightarrow (((p V0p) \vee \\ & (p V1q)) \wedge ((\neg(p V1q)) \vee (\neg(p V0p)))))) \end{aligned} \quad (72)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (p V0p))) \quad (73)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (\neg(p V1q)))) \quad (74)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V0p)))) \quad (75)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V1q)))) \quad (76)$$

Assume the following.

$$(\forall V0p \in 2.((\neg(\neg(p V0p))) \Rightarrow (p V0p))) \quad (77)$$

Theorem 1

$$\begin{aligned} & \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0m \in (\text{ty_2Epair_2Eprod} \\ & (2^{A_{27a}}) (\text{ty_2Epair_2Eprod } (2^{(2^{A_{27a}})}) (\text{ty_2Erealax_2Ereal}^{(2^{A_{27a}})}))) \\ & (\forall V1f \in (\text{ty_2Eextreal_2Eextreal}^{A_{27a}}). (\forall V2g \in (\\ & \text{ty_2Eextreal_2Eextreal}^{A_{27a}}). (((p (\text{ap } (\text{c_2Emeasure_2Emeasure_space} \\ & A_{27a}) V0m)) \wedge ((p (\text{ap } (\text{ap } (\text{c_2ELebesgue_2Eintegrable } A_{27a}) V0m) \\ & V1f)) \wedge ((p (\text{ap } (\text{ap } (\text{c_2ELebesgue_2Eintegrable } A_{27a}) V0m) V2g)) \wedge \\ & ((\forall V3x \in A_{27a}. (p (\text{ap } (\text{ap } \text{c_2Eextreal_2Eextreal_le } (\text{ap} \\ & \text{c_2Eextreal_2Eextreal_of_num } \text{c_2Enum_2E0})) (\text{ap } V1f V3x)))))) \wedge \\ & (\forall V4x \in A_{27a}. (p (\text{ap } (\text{ap } \text{c_2Eextreal_2Eextreal_le } (\text{ap } \text{c_2Eextreal_2Eextreal_of_num} \\ & \text{c_2Enum_2E0})) (\text{ap } V2g V4x)))))) \Rightarrow (p (\text{ap } (\text{ap } (\text{c_2ELebesgue_2Eintegrable} \\ & A_{27a}) V0m) (\lambda V5x \in A_{27a}. (\text{ap } (\text{ap } \text{c_2Eextreal_2Eextreal_add} \\ & (\text{ap } V1f V5x)) (\text{ap } V2g V5x)))))) \end{aligned}$$