

thm_2Elebesgue_2Emax_fn_seq_def_compute
 (TMbCAm-
 fWAAP5t9qsSiJvyFJZExZKFRG6ixy)

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Let $c_2Enum_2ZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$\text{nonempty } ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2ABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2ABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (3)$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be ($ap\ c_2Enum_2ABS_num\ c_2Enum_2ZERO_REP$).

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (4)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (5)$$

Definition 3 We define c_2Ebool_2ET to be ($ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x)$)

Definition 4 We define $c_2Ebool_2E_21$ to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (ap\ (ap\ (c_2Emin_2E_3D\ (2^{A-27a}))\ (\lambda V1x \in 2.V1x)))$

Definition 5 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap\ c_2Enum_2ABS_num\ m)$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (6)$$

Definition 6 We define $c_2Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EBIT2 n) V0)$

Definition 7 We define $\text{c_2Earithmetic_2EZERO}$ to be c_2Enum_2E0 .

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum ty_2Enum_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (7)$$

Definition 8 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EBIT1 n) V0)$

Definition 9 We define $c_2Earthmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum. V0x.$

Definition 10 We define $c_{\text{2Emin_2E_3D_3D_3E}}$ to be $\lambda P \in 2.\lambda Q \in 2.\text{inj_o} (p \Rightarrow p \ Q)$ of type ι .

Let $ty_2Eextreal_2Eextreal : \iota$ be given. Assume the following.

nonempty $\text{ty_}2\text{Extreal_}2\text{Extreal}$ (8)

Let $c_2Eextreal_2Eextreal_le : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_le \in ((2^{ty_2Eextreal_2Eextreal})^{ty_2Eextreal_2Eextreal}) \quad (9)$$

Definition 11 We define c_2Ebool_2EF to be $(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V0t \in 2.V0t))$.

Definition 12 We define $c_{\text{Ebool_E_2F_5C}}$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap(c_{\text{Ebool_E_21}}) 2)) (\lambda V2t \in$

Definition 13 We define $c_{\text{Emin}}.40$ to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p \ (ap \ P \ x)) \ \text{then} \ (\lambda x. x \in A \wedge \text{of type } \iota \rightarrow \iota)$.

Definition 15 We define c_2 to be $\lambda V0x : ty_2 \rightarrow extreal. \lambda V1y : ty_2 \rightarrow extreal. max$

Let $c_{\text{2Elebesgue_2Emax_fn_seq}} : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow c_2\text{Lebesgue_}2\text{Emax_fn_seq } A_{27a} \in \\ & ((ty_{-2}\text{Eextreal_}2\text{Eextreal}^{A_{-27a}})ty_{-2}\text{Enum_}2\text{Enum})((ty_{-2}\text{Eextreal_}2\text{Eextreal}^{A_{-27a}})ty_{-2}\text{Enum_}2\text{Enum})) \end{aligned} \quad (10)$$

Assume the following.

$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0f \in ((A_27a^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}).$
 $(\forall V1g \in (A_27a^{ty_2Enum_2Enum}).((\forall V2n \in ty_2Enum_2Enum.$
 $((ap\ V1g\ (ap\ c_2Enum_2ESUC\ V2n)) = (ap\ (ap\ V0f\ V2n)\ (ap\ c_2Enum_2ESUC$
 $V2n))) \Leftrightarrow ((\forall V3n \in ty_2Enum_2Enum.((ap\ V1g\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT1\ V3n))) = (ap\ (ap\ V0f\ (ap\ (ap\ c_2Earthmetic_2E_2D$
 $(ap\ c_2Earthmetic_2ENUMERAL\ (ap\ c_2Earthmetic_2EBIT1\ V3n))))$
 $(ap\ c_2Earthmetic_2ENUMERAL\ (ap\ c_2Earthmetic_2EBIT1\ c_2Earthmetic_2EZERO))))$
 $(ap\ c_2Earthmetic_2ENUMERAL\ (ap\ c_2Earthmetic_2EBIT1\ V3n)))))) \wedge$
 $(\forall V4n \in ty_2Enum_2Enum.((ap\ V1g\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT2\ V4n))) = (ap\ (ap\ V0f\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT1\ V4n)))\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT2\ V4n))))))))))$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (12)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty\ A_{27a} \Rightarrow & ((\forall V0g \in ((ty_2Eextreal_2Eextreal^{A_27a})^{ty_2Enum_2Enum}). \\ & (\forall V1x \in A_{27a}. ((ap (ap (ap (c_2Elebesgue_2Emax_fn_seq \\ A_{27a}) V0g) c_2Enum_2E0) V1x) = (ap (ap V0g c_2Enum_2E0) V1x)))) \wedge \\ & (\forall V2g \in ((ty_2Eextreal_2Eextreal^{A_27a})^{ty_2Enum_2Enum}). \\ & (\forall V3n \in ty_2Enum_2Enum. (\forall V4x \in A_{27a}. ((ap (ap (ap \\ (c_2Elebesgue_2Emax_fn_seq A_{27a}) V2g) (ap c_2Enum_2ESUC V3n)) \\ V4x) = (ap (ap c_2Eextreal_2Eextreal_max (ap (ap (ap (c_2Elebesgue_2Emax_fn_seq \\ A_{27a}) V2g) V3n) V4x)) (ap (ap V2g (ap c_2Enum_2ESUC V3n)) V4x))))))) \\ & (13) \end{aligned}$$

Theorem 1

$$\begin{aligned} \forall A_{27a}.nonempty\ A_{27a} \Rightarrow & ((\forall V0g \in ((ty_2Eextreal_2Eextreal^{A_27a})^{ty_2Enum_2Enum}). \\ & (\forall V1x \in A_{27a}. ((ap (ap (ap (c_2Elebesgue_2Emax_fn_seq \\ A_{27a}) V0g) c_2Enum_2E0) V1x) = (ap (ap V0g c_2Enum_2E0) V1x)))) \wedge \\ & ((\forall V2g \in ((ty_2Eextreal_2Eextreal^{A_27a})^{ty_2Enum_2Enum}). \\ & (\forall V3n \in ty_2Enum_2Enum. (\forall V4x \in A_{27a}. ((ap (ap (ap \\ (c_2Elebesgue_2Emax_fn_seq A_{27a}) V2g) (ap c_2Earithmetic_2ENUMERAL \\ (ap c_2Earithmetic_2EBIT1 V3n)) V4x) = (ap (ap c_2Eextreal_2Eextreal_max \\ (ap (ap (ap (c_2Elebesgue_2Emax_fn_seq A_{27a}) V2g) (ap (ap c_2Earithmetic_2E_2D \\ (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 V3n))) \\ (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) \\ V4x)) (ap (ap V2g (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\ V3n)) V4x))))))) \wedge (\forall V5g \in ((ty_2Eextreal_2Eextreal^{A_27a})^{ty_2Enum_2Enum}). \\ & (\forall V6n \in ty_2Enum_2Enum. (\forall V7x \in A_{27a}. ((ap (ap (ap \\ (c_2Elebesgue_2Emax_fn_seq A_{27a}) V5g) (ap c_2Earithmetic_2ENUMERAL \\ (ap c_2Earithmetic_2EBIT2 V6n)) V7x) = (ap (ap c_2Eextreal_2Eextreal_max \\ (ap (ap (ap (c_2Elebesgue_2Emax_fn_seq A_{27a}) V5g) (ap c_2Earithmetic_2ENUMERAL \\ (ap c_2Earithmetic_2EBIT1 V6n))) V7x)) (ap (ap V5g (ap c_2Earithmetic_2ENUMERAL \\ (ap c_2Earithmetic_2EBIT2 V6n))) V7x))))))) \\ & (14) \end{aligned}$$