

thm_2Elist_2ELUPDATE_compute (TMPqDJEervrA8PqZRct2By65xvAsKhxZm4M)

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Let $c_2Enum_2ZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$\text{nonempty } ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2ABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2ABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (3)$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2ABS_num\ c_2Enum_2ZERO_REP)$.

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (4)$$

Let $c_2Enum_2SUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2SUC_REP \in (\omega^{\omega}) \quad (5)$$

Definition 3 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$.

Definition 4 We define $c_2Ebool_2E_21$ to be $\lambda A. \lambda P \in (2^{A-27a}). (ap\ (ap\ (c_2Emin_2E_3D\ (2^{A-27a}))\ P))$.

Definition 5 We define c_2Enum_2SUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap\ c_2Enum_2ABS_num\ m)$.

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (6)$$

Definition 6 We define $c_2Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EBIT2 n) V0)$

Definition 7 We define $c_2EArithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum^{ty_2Enum_2Enum}})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (7)$$

Definition 8 We define $c_2Earthmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap (ap c_2Earthmetic_2EBIT1$

Definition 9 We define $c_2Earthmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum. V0x$.

Definition 10 We define $c_{\text{2Emin_2E_3D_3D_3E}}$ to be $\lambda P \in 2.\lambda Q \in 2.\text{inj_o} (p \Rightarrow p Q)$ of type ι .

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. \text{nonempty } A \Rightarrow \text{nonempty } (\text{ty_2Elist_2Elist } A) \quad (8)$$

Let $c_2Elist_2ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2Elist_2ECONS\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{A_27a}) \quad (9)$$

Let $c_2Elist_2ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A _27a. nonempty\ A _27a \Rightarrow c_2Elist_2ENIL\ A _27a \in (ty_2Elist_2Elist\ A _27a) \quad (10)$$

Let $c_2Elist_2ELUPDATE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2Elist_2ELUPDATE\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{ty_2Enum_2Enum})^{A_27a}) \quad (11)$$

Definition 11 We define $c_Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_Ebool_2E_21 2) (\lambda V2t \in$

Assume the following.

$\forall A.27a.\text{nonempty } A.27a \Rightarrow (\forall V0f \in ((A.27a^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}).$
 $(\forall V1g \in (A.27a^{ty_2Enum_2Enum}).((\forall V2n \in ty_2Enum_2Enum.$
 $((ap\ V1g\ (ap\ c_2Enum_2ESUC\ V2n)) = (ap\ (ap\ V0f\ V2n)\ (ap\ c_2Enum_2ESUC$
 $V2n)))) \Leftrightarrow ((\forall V3n \in ty_2Enum_2Enum.((ap\ V1g\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT1\ V3n))) = (ap\ (ap\ V0f\ (ap\ (ap\ c_2Earthmetic_2E_2D$
 $(ap\ c_2Earthmetic_2ENUMERAL\ (ap\ c_2Earthmetic_2EBIT1\ V3n))))$
 $(ap\ c_2Earthmetic_2ENUMERAL\ (ap\ c_2Earthmetic_2EBIT1\ c_2Earthmetic_2EZERO))))))$
 $(ap\ c_2Earthmetic_2ENUMERAL\ (ap\ c_2Earthmetic_2EBIT1\ V3n)))) \wedge$
 $((\forall V4n \in ty_2Enum_2Enum.((ap\ V1g\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT2\ V4n))) = (ap\ (ap\ V0f\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT1\ V4n)))\ (ap\ c_2Earthmetic_2ENUMERAL$
 $(ap\ c_2Earthmetic_2EBIT2\ V4n))))))))))$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow ((\forall V0e \in A_27a. (\forall V1n \in \\ & ty_2Enum_2Enum. ((ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V0e) V1n) \\ & (c_2Elist_2ENIL A_27a)) = (c_2Elist_2ENIL A_27a)))) \wedge ((\forall V2e \in \\ & A_27a. (\forall V3x \in A_27a. (\forall V4l \in (ty_2Elist_2Elist A_27a). \\ & ((ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V2e) c_2Enum_2E0) (ap (\\ & ap (c_2Elist_2ECONS A_27a) V3x) V4l)) = (ap (ap (c_2Elist_2ECONS \\ & A_27a) V2e) V4l))))))) \wedge ((\forall V5e \in A_27a. (\forall V6n \in ty_2Enum_2Enum. \\ & (\forall V7x \in A_27a. (\forall V8l \in (ty_2Elist_2Elist A_27a). (\\ & (ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V5e) (ap c_2Enum_2ESUC V6n) \\ & (ap (ap (c_2Elist_2ECONS A_27a) V7x) V8l)) = (ap (ap (c_2Elist_2ECONS \\ & A_27a) V7x) (ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V5e) V6n) V8l))))))))))) \\ & (14) \end{aligned}$$

Theorem 1

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow ((\forall V0e \in A_27a. (\forall V1n \in \\ & ty_2Enum_2Enum. ((ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V0e) V1n) \\ & (c_2Elist_2ENIL A_27a)) = (c_2Elist_2ENIL A_27a)))) \wedge ((\forall V2e \in \\ & A_27a. (\forall V3x \in A_27a. (\forall V4l \in (ty_2Elist_2Elist A_27a). \\ & ((ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V2e) c_2Enum_2E0) (ap (\\ & ap (c_2Elist_2ECONS A_27a) V3x) V4l)) = (ap (ap (c_2Elist_2ECONS \\ & A_27a) V2e) V4l))))))) \wedge ((\forall V5e \in A_27a. (\forall V6n \in ty_2Enum_2Enum. \\ & (\forall V7x \in A_27a. (\forall V8l \in (ty_2Elist_2Elist A_27a). (\\ & (ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V5e) (ap c_2Earithmetic_2ENUMERAL \\ & (ap c_2Earithmetic_2EBIT1 V6n)) (ap (ap (c_2Elist_2ECONS A_27a) \\ & V7x) V8l)) = (ap (ap (c_2Elist_2ECONS A_27a) V7x) (ap (ap (ap (c_2Elist_2ELUPDATE \\ & A_27a) V5e) (ap (ap c_2Earithmetic_2E_2D (ap c_2Earithmetic_2ENUMERAL \\ & (ap c_2Earithmetic_2EBIT1 V6n)) (ap c_2Earithmetic_2ENUMERAL \\ & (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) V8l))))))) \wedge \\ & (\forall V9e \in A_27a. (\forall V10n \in ty_2Enum_2Enum. (\forall V11x \in \\ & A_27a. (\forall V12l \in (ty_2Elist_2Elist A_27a). ((ap (ap (ap (c_2Elist_2ELUPDATE \\ & A_27a) V9e) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT2 \\ & V10n)) (ap (ap (c_2Elist_2ECONS A_27a) V11x) V12l)) = (ap (ap (c_2Elist_2ECONS \\ & A_27a) V11x) (ap (ap (ap (c_2Elist_2ELUPDATE A_27a) V9e) (ap c_2Earithmetic_2ENUMERAL \\ & (ap c_2Earithmetic_2EBIT1 V10n)) V12l))))))))))) \end{aligned}$$