

thm_2Elist_2ENULL__GENLIST
(TMHrSJBwoetqBE7MTdNB86jv4LrjRw6g5rE)

October 26, 2020

Definition 1 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.$ **if** $(\exists x \in A.p (ap P x))$ **then** *(the* $(\lambda x.x \in A \wedge p x)$ *of type* $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ *of type* $\iota \Rightarrow \iota$.

Definition 3 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_40 A_27a) P)))$

Definition 4 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ *of type* ι .

Definition 5 We define $c_2Ebool_2E_2ET$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 6 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E_3D (2^{A_27a}) P) P)))$

Definition 7 We define $c_2Ebool_2E_5C_2E_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t))))$

Definition 8 We define $c_2Ebool_2E_2EF$ to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty_2Elist_2Elist A0) \quad (1)$$

Let $c_2Elist_2ENULL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Elist_2ENULL A_27a \in (2^{(ty_2Elist_2Elist A_27a)}) \quad (2)$$

Let $c_2Elist_2ESNOC : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Elist_2ESNOC A_27a \in (((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)})^{A_27a}) \quad (3)$$

Let $c_2Elist_2ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Elist_2ENIL A_27a \in (ty_2Elist_2Elist A_27a) \quad (4)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p V0t))) \quad (15)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A_27a.(p V0t)) \Leftrightarrow (p V0t))) \quad (16)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (17)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (18)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (19)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (((p (ap (c_2Elist_2ENULL A_27a) (c_2Elist_2ENIL A_27a))) \Leftrightarrow True) \wedge (\forall V0h \in A_27a.(\forall V1t \in (ty_2Elist_2Elist A_27a).(p (ap (c_2Elist_2ENULL A_27a) (ap (c_2Elist_2ECONS A_27a) V0h) V1t))) \Leftrightarrow False)))) \quad (20)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow ((\forall V0f \in (A_27a^{ty_2Enum_2Enum}). ((ap (ap (c_2Elist_2EGENLIST A_27a) V0f) c_2Enum_2E0) = (c_2Elist_2ENIL A_27a))) \wedge (\forall V1f \in (A_27a^{ty_2Enum_2Enum}).(\forall V2n \in ty_2Enum_2Enum.((ap (ap (c_2Elist_2EGENLIST A_27a) V1f) (ap c_2Enum_2ESUC V2n)) = (ap (ap (c_2Elist_2ESNOC A_27a) (ap V1f V2n)) (ap (ap (c_2Elist_2EGENLIST A_27a) V1f) V2n))))))) \quad (21)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0f \in (A_27a^{ty_2Enum_2Enum}). (\forall V1n \in ty_2Enum_2Enum.((ap (ap (c_2Elist_2EGENLIST A_27a) V0f) (ap c_2Enum_2ESUC V1n)) = (ap (ap (c_2Elist_2ECONS A_27a) (ap V0f c_2Enum_2E0)) (ap (ap (c_2Elist_2EGENLIST A_27a) (ap (ap (c_2Ecombin_2Eo ty_2Enum_2Enum A_27a ty_2Enum_2Enum) V0f) c_2Enum_2ESUC) V1n)))))) \quad (22)$$

Assume the following.

$$(\forall V0n \in ty_2Enum_2Enum.(\neg((ap c_2Enum_2ESUC V0n) = c_2Enum_2E0))) \quad (23)$$

Theorem 1

$$\begin{aligned} & \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0n \in \text{ty_2Enum_2Enum}. \\ & \quad \forall V1f \in (A_{27a}^{\text{ty_2Enum_2Enum}}). ((p \text{ (ap (c_2Elist_2ENULL} \\ A_{27a} \text{ (ap (ap (c_2Elist_2EGENLIST } A_{27a} \text{ V1f) V0n))))} \Leftrightarrow (V0n = \text{c_2Enum_2E0})))) \end{aligned}$$