

thm_2Elist_2Elist__INDUCT

(TMYeqlEwg8erRyDG45ytJXoVj4J4LtYMoMT)

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Definition 1 We define `c_2Emin_2E_3D` to be $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj_o } (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define `c_2Ebool_2E_2T` to be $(\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define `c_2Ebool_2E_21` to be $\lambda A. \lambda 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^{A-27a}))))$

Definition 4 We define `c_2Ebool_2E_2F` to be $(\text{ap } (\text{c_2Ebool_2E_21 } 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2. \lambda Q \in 2. \text{inj_o } (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define `c_2Ebool_2E_27E` to be $(\lambda V0t \in 2. (\text{ap } (\text{ap } (\text{c_2Emin_2E_3D_3D_3E } V0t) \text{ c_2Ebool_2E_2F})))$

Let `ty_2Elist_2Elist` : $\iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. \text{nonempty } A0 \Rightarrow \text{nonempty } (\text{ty_2Elist_2Elist } A0) \quad (1)$$

Let `c_2Elist_2ECONS` : $\iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. \lambda 27a. \text{nonempty } A. \lambda 27a. \Rightarrow \text{c_2Elist_2ECONS } A. \lambda 27a. \in (((\text{ty_2Elist_2Elist } A. \lambda 27a.) (\text{ty_2Elist_2Elist } A. \lambda 27a.) A. \lambda 27a.) A. \lambda 27a.) \quad (2)$$

Let `c_2Elist_2ENIL` : $\iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. \lambda 27a. \text{nonempty } A. \lambda 27a. \Rightarrow \text{c_2Elist_2ENIL } A. \lambda 27a. \in (\text{ty_2Elist_2Elist } A. \lambda 27a.) \quad (3)$$

Definition 7 We define `c_2Ebool_2E_2F_5C` to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (\text{ap } (\text{c_2Ebool_2E_21 } 2) (\lambda V2t \in 2.V2t))))$

Assume the following.

$$\text{True} \quad (4)$$

Assume the following.

$$\forall A. \lambda 27a. \text{nonempty } A. \lambda 27a. \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A. \lambda 27a. (p V0t)) \Leftrightarrow (p V0t))) \quad (5)$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow \\
& (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(\\
& p V0t))))))
\end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0P \in (2^{(ty_2Elist_2Elist A_27a)}), \\
& (((p (ap V0P (c_2Elist_2ENIL A_27a))) \wedge (\forall V1l \in (ty_2Elist_2Elist \\
& A_27a).(p (ap V0P V1l)) \Rightarrow (\forall V2a \in A_27a.(p (ap V0P (ap (ap (\\
& c_2Elist_2ECONS A_27a) V2a) V1l)))))) \Rightarrow (\forall V3l \in (ty_2Elist_2Elist \\
& A_27a).(p (ap V0P V3l))))))
\end{aligned} \tag{7}$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0P \in (2^{(ty_2Elist_2Elist A_27a)}), \\
& (((p (ap V0P (c_2Elist_2ENIL A_27a))) \wedge (\forall V1t \in (ty_2Elist_2Elist \\
& A_27a).(p (ap V0P V1t)) \Rightarrow (\forall V2h \in A_27a.(p (ap V0P (ap (ap (\\
& c_2Elist_2ECONS A_27a) V2h) V1t)))))) \Rightarrow (\forall V3l \in (ty_2Elist_2Elist \\
& A_27a).(p (ap V0P V3l))))))
\end{aligned}$$