

thm_2Ellist_2ELFILTER__THM
(TMdSDjP8zfY6Fyhqg1ELJsUBTpLQk2NxBpT)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2))) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x)$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{1}$$

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \tag{2}$$

Definition 3 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p \Rightarrow Q)$ of type ι .

Definition 4 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x)) \mathbf{then} (the (\lambda x.x \in A \wedge p))$ of type $\iota \Rightarrow \iota$.

Definition 5 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_40 A))))$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in omega \tag{3}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{omega}) \tag{4}$$

Definition 6 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 7 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (5)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (6)$$

Definition 8 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap (ap (c_2Emin_2E_3D (2^{A_27a})))$

Definition 9 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap c_2Enum_2EABS_num ($

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (7)$$

Definition 10 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum. (ap (ap c_2Earithmetic$

Definition 11 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum. V0x$.

Let $ty_2Eone_2Eone : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eone_2Eone \quad (8)$$

Definition 12 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in$

Let $ty_2Esum_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow \forall A1. nonempty\ A1 \Rightarrow nonempty\ (ty_2Esum_2Esum\ A0\ A1) \quad (9)$$

Let $c_2Esum_2EABS_sum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow \forall A_27b. nonempty\ A_27b \Rightarrow c_2Esum_2EABS_sum\ A_27a\ A_27b \in ((ty_2Esum_2Esum\ A_27a\ A_27b)^{((2^{A_27b})^{A_27a})^2}) \quad (10)$$

Definition 13 We define c_2Esum_2EINL to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0e \in A_27a. (ap (c_2Esum_2EABS$

Let $ty_2Eoption_2Eoption : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow nonempty\ (ty_2Eoption_2Eoption\ A0) \quad (11)$$

Let $c_2Eoption_2Eoption_ABS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Eoption_2Eoption_ABS\ A_27a \in ((ty_2Eoption_2Eoption\ A_27a)^{(ty_2Esum_2Esum\ A_27a\ ty_2Eone_2Eone)}) \quad (12)$$

Definition 14 We define $c_2Eoption_2ESOME$ to be $\lambda A_27a : \iota. \lambda V0x \in A_27a. (ap (c_2Eoption_2Eoption$

Definition 15 We define c_Ebool_2EF to be $(ap (c_Ebool_2E_21\ 2) (\lambda V0t \in 2.V0t))$.

Definition 16 We define c_Ebool_2ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.($

Definition 17 We define c_Eone_2Eone to be $(ap (c_Emin_2E_40\ ty_2Eone_2Eone) (\lambda V0x \in ty_2Eone_2$

Definition 18 We define $c_Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_Emin_2E_3D_3D_3E\ V0t) c_Ebool_2E$

Definition 19 We define c_Esum_2EINR to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0e \in A_27b.(ap (c_Esum_2EABS$

Definition 20 We define $c_Eoption_2ENONE$ to be $\lambda A_27a : \iota.(ap (c_Eoption_2Eoption_ABS\ A_27a) ($

Definition 21 We define $c_Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_Ebool_2E_21\ 2) (\lambda V2t \in$

Definition 22 We define $c_Ellist_2Elrep_ok$ to be $\lambda A_27a : \iota.(\lambda V0a0 \in ((ty_2Eoption_2Eoption\ A_27a)^{ty-$

Let $ty_2Ellist_2Ellist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Ellist_2Ellist\ A0) \quad (13)$$

Let $c_2Ellist_2Ellist_rep : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow c_2Ellist_2Ellist_rep\ A_27a \in \\ & (((ty_2Eoption_2Eoption\ A_27a)^{ty_2Enum_2Enum})^{(ty_2Ellist_2Ellist\ A_27a)}) \end{aligned} \quad (14)$$

Let $c_2Ellist_2Ellist_abs : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow c_2Ellist_2Ellist_abs\ A_27a \in \\ & ((ty_2Ellist_2Ellist\ A_27a)^{(ty_2Eoption_2Eoption\ A_27a)^{ty_2Enum_2Enum}}) \end{aligned} \quad (15)$$

Definition 23 We define c_Ellist_2ELHD to be $\lambda A_27a : \iota.\lambda V0ll \in (ty_2Ellist_2Ellist\ A_27a).(ap (ap (c_2$

Let $c_2Eoption_2Eoption_CASE : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Eoption_2Eoption_CASE \\ & A_27a\ A_27b \in (((A_27b^{(A_27b^{A_27a})})^{A_27b})^{(ty_2Eoption_2Eoption\ A_27a)}) \end{aligned} \quad (16)$$

Definition 24 We define c_Ellist_2ELTL to be $\lambda A_27a : \iota.\lambda V0ll \in (ty_2Ellist_2Ellist\ A_27a).(ap (ap (ap$

Definition 25 We define $c_Ellist_2ELCONS$ to be $\lambda A_27a : \iota.\lambda V0h \in A_27a.\lambda V1t \in (ty_2Ellist_2Ellist\ A$

Definition 26 We define c_Ellist_2ELNIL to be $\lambda A_27a : \iota.(ap (c_2Ellist_2Ellist_abs\ A_27a) (\lambda V0n \in ty$

Definition 27 We define $c_Ellist_2Eexists$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(\lambda V1a0 \in (ty_2Ellist_2Ellis$

Let $c_2Ellist_2ELFILTER : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ellist_2ELFILTER\ A_27a \in (((ty_2Ellist_2Ellist\ A_27a)^{(ty_2Ellist_2Ellist\ A_27a)})^{(2^{A_27a})}) \quad (17)$$

Let $c_2Eoption_2ETHE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Eoption_2ETHE\ A_27a \in (A_27a^{(ty_2Eoption_2Eoption\ A_27a)}) \quad (18)$$

Assume the following.

$$True \quad (19)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p\ V0t1) \Rightarrow (p\ V1t2)) \Rightarrow (((p\ V1t2) \Rightarrow (p\ V0t1)) \Rightarrow ((p\ V0t1) \Leftrightarrow (p\ V1t2)))))) \quad (20)$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p\ V0t))) \quad (21)$$

Assume the following.

$$(\forall V0t \in 2. ((p\ V0t) \vee (\neg(p\ V0t)))) \quad (22)$$

Assume the following.

$$(\forall V0t \in 2. (((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \quad (23)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge ((p\ V0t) \Rightarrow False) \Leftrightarrow (\neg(p\ V0t)))))) \quad (24)$$

Assume the following.

$$((\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t)) \wedge ((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (25)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (26)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (27)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (28)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p V0A) \wedge (p V1B))) \Leftrightarrow ((\neg(p V0A) \vee \neg(p V1B)))) \wedge (((\neg(p V0A) \vee (p V1B)) \Leftrightarrow ((\neg(p V0A) \wedge \neg(p V1B)))))) \quad (29)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (30)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0P \in 2.(\forall V1Q \in 2. \\ & (\forall V2x \in A_27a.(\forall V3x_27 \in A_27a.(\forall V4y \in A_27a. \\ & (\forall V5y_27 \in A_27a.(((p V0P) \Leftrightarrow (p V1Q)) \wedge (((p V1Q) \Rightarrow (V2x = V3x_27)) \wedge \\ & ((\neg(p V1Q)) \Rightarrow (V4y = V5y_27)))) \Rightarrow ((ap (ap (ap (c_2Ebool_2ECOND \ A_27a) \\ & V0P) V2x) V4y) = (ap (ap (ap (c_2Ebool_2ECOND \ A_27a) V1Q) V3x_27) \\ & V5y_27)))))))))) \quad (31) \end{aligned}$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1y \in 2.(\forall V2z \in 2.(\forall V3w \in 2.(((p V0x) \Rightarrow (p V1y)) \wedge ((p V2z) \Rightarrow (p V3w))) \Rightarrow (((p V0x) \wedge (p V2z)) \Rightarrow ((p V1y) \wedge (p V3w)))))) \quad (32)$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1y \in 2.(\forall V2z \in 2.(\forall V3w \in 2.(((p V0x) \Rightarrow (p V1y)) \wedge ((p V2z) \Rightarrow (p V3w))) \Rightarrow (((p V0x) \vee (p V2z)) \Rightarrow ((p V1y) \vee (p V3w)))))) \quad (33)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}).(\forall V1Q \in \\ & (2^{A_27a}).((\forall V2x \in A_27a.((p (ap V0P V2x)) \Rightarrow (p (ap V1Q V2x)))) \Rightarrow \\ & ((\exists V3x \in A_27a.(p (ap V0P V3x))) \Rightarrow (\exists V4x \in A_27a.(p (\\ & ap V1Q V4x)))))) \quad (34) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow ((\forall V0t1 \in A_27a.(\forall V1t2 \in \\ & A_27a.((ap (ap (ap (c_2Ebool_2ECOND \ A_27a) c_2Ebool_2ET) V0t1) \\ & V1t2) = V0t1))) \wedge (\forall V2t1 \in A_27a.(\forall V3t2 \in A_27a.((ap \\ & (ap (ap (c_2Ebool_2ECOND \ A_27a) c_2Ebool_2EF) V2t1) V3t2) = V3t2)))) \quad (35) \end{aligned}$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & ((\forall V0a \in (ty_2Ellist_2Ellist\ A.27a).((ap\ (c_2Ellist_2Ellist_abs\ A.27a)\ (ap\ (c_2Ellist_2Ellist_rep\ A.27a)\ V0a)) = V0a)) \wedge (\forall V1r \in ((ty_2Eoption_2Eoption\ A.27a)^{ty_2Enum_2Enum}). \\ & ((p\ (ap\ (c_2Ellist_2Elrep_ok\ A.27a)\ V1r)) \Leftrightarrow ((ap\ (c_2Ellist_2Ellist_rep\ A.27a)\ (ap\ (c_2Ellist_2Ellist_abs\ A.27a)\ V1r)) = V1r)))) \end{aligned} \quad (36)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0h \in A.27a.(\forall V1t \in (ty_2Ellist_2Ellist\ A.27a).(((ap\ (c_2Ellist_2ELHD\ A.27a)\ (ap\ (ap\ (c_2Ellist_2ELCONS\ A.27a)\ V0h)\ V1t)) = (ap\ (c_2Eoption_2ESOME\ A.27a)\ V0h)) \wedge ((ap\ (c_2Ellist_2ELTL\ A.27a)\ (ap\ (ap\ (c_2Ellist_2ELCONS\ A.27a)\ V0h)\ V1t)) = (ap\ (c_2Eoption_2ESOME\ (ty_2Ellist_2Ellist\ A.27a)\ V1t)))))) \end{aligned} \quad (37)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0h1 \in A.27a.(\forall V1t1 \in (ty_2Ellist_2Ellist\ A.27a).(\forall V2h2 \in A.27a.(\forall V3t2 \in (ty_2Ellist_2Ellist\ A.27a).(((ap\ (ap\ (c_2Ellist_2ELCONS\ A.27a)\ V0h1)\ V1t1) = (ap\ (ap\ (c_2Ellist_2ELCONS\ A.27a)\ V2h2)\ V3t2)) \Leftrightarrow ((V0h1 = V2h2) \wedge (V1t1 = V3t2)))))) \end{aligned} \quad (38)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0P \in (2^{A.27a}).(\forall V1h \in A.27a.(\forall V2t \in (ty_2Ellist_2Ellist\ A.27a).(((p\ (ap\ (ap\ (c_2Ellist_2Eexists\ A.27a)\ V0P)\ (c_2Ellist_2ELNIL\ A.27a))) \Leftrightarrow False) \wedge ((p\ (ap\ (ap\ (c_2Ellist_2Eexists\ A.27a)\ V0P)\ (ap\ (ap\ (c_2Ellist_2ELCONS\ A.27a)\ V1h)\ V2t))) \Leftrightarrow ((p\ (ap\ V0P\ V1h)) \vee (p\ (ap\ (ap\ (c_2Ellist_2Eexists\ A.27a)\ V0P)\ V2t)))))) \end{aligned} \quad (39)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow & (\forall V0P \in (2^{A.27a}).(\forall V1ll \in (ty_2Ellist_2Ellist\ A.27a).(((ap\ (ap\ (c_2Ellist_2ELFILTER\ A.27a)\ V0P)\ V1ll) = (ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ (ty_2Ellist_2Ellist\ A.27a)\ (ap\ c_2Ebool_2E_7E\ (ap\ (ap\ (c_2Ellist_2Eexists\ A.27a)\ V0P)\ V1ll))) (c_2Ellist_2ELNIL\ A.27a)) (ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ (ty_2Ellist_2Ellist\ A.27a)\ (ap\ V0P)\ (ap\ (c_2Eoption_2ETHE\ A.27a)\ (ap\ (c_2Ellist_2ELHD\ A.27a)\ V1ll)))) (ap\ (ap\ (c_2Ellist_2ELCONS\ A.27a)\ (ap\ (c_2Eoption_2ETHE\ A.27a)\ (ap\ (c_2Ellist_2ELHD\ A.27a)\ V1ll)))) (ap\ (ap\ (c_2Ellist_2ELFILTER\ A.27a)\ V0P)\ (ap\ (c_2Eoption_2ETHE\ (ty_2Ellist_2Ellist\ A.27a)\ (ap\ (c_2Ellist_2ELTL\ A.27a)\ V1ll)))))) (ap\ (ap\ (c_2Ellist_2ELFILTER\ A.27a)\ V0P)\ (ap\ (c_2Eoption_2ETHE\ (ty_2Ellist_2Ellist\ A.27a)\ (ap\ (c_2Ellist_2ELTL\ A.27a)\ V1ll)))))) \end{aligned} \quad (40)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& (\forall V0v \in A_27b. (\forall V1f \in (A_27b^{A_27a}). ((ap\ (ap\ (ap\ (c_2Eoption_2Eoption_CASE \\
& A_27a\ A_27b)\ (c_2Eoption_2ENONE\ A_27a))\ V0v)\ V1f) = V0v))) \wedge (\forall V2x \in \\
& A_27a. (\forall V3v \in A_27b. (\forall V4f \in (A_27b^{A_27a}). ((ap\ (ap \\
& (ap\ (c_2Eoption_2Eoption_CASE\ A_27a\ A_27b)\ (ap\ (c_2Eoption_2ESOME \\
& A_27a)\ V2x))\ V3v)\ V4f) = (ap\ V4f\ V2x))))))
\end{aligned} \tag{41}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in \\
& A_27a. (((ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x) = (ap\ (c_2Eoption_2ESOME \\
& A_27a)\ V1y)) \Leftrightarrow (V0x = V1y))))
\end{aligned} \tag{42}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((ap\ (c_2Eoption_2ETHE \\
& A_27a)\ (ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x)) = V0x))
\end{aligned} \tag{43}$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& (\forall V0P \in (2^{A_27a}). ((ap\ (ap\ (c_2Ellist_2ELFILTER\ A_27a) \\
& V0P)\ (c_2Ellist_2ELNIL\ A_27a)) = (c_2Ellist_2ELNIL\ A_27a))) \wedge \\
& (\forall V1P \in (2^{A_27b}). (\forall V2h \in A_27b. (\forall V3t \in (ty_2Ellist_2Ellist \\
& A_27b). ((ap\ (ap\ (c_2Ellist_2ELFILTER\ A_27b)\ V1P)\ (ap\ (ap\ (c_2Ellist_2ELCONS \\
& A_27b)\ V2h)\ V3t)) = (ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ (ty_2Ellist_2Ellist \\
& A_27b))\ (ap\ V1P\ V2h))\ (ap\ (ap\ (c_2Ellist_2ELCONS\ A_27b)\ V2h)\ (ap \\
& (ap\ (c_2Ellist_2ELFILTER\ A_27b)\ V1P)\ V3t)))\ (ap\ (ap\ (c_2Ellist_2ELFILTER \\
& A_27b)\ V1P)\ V3t))))))
\end{aligned}$$