

thm_2Ellist_2ELREPEAT__thm
(TMZHN5P784uc1dzfMTyfMfSG9MThsC9B6fM)

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Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{1}$$

Let $c_2Earithmetic_2E_2A : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2A \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \tag{2}$$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \tag{3}$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x))$ then (the $(\lambda x.x \in A \wedge P x)$) of type $\iota \Rightarrow \iota$.

Definition 3 We define $c_2Ebool_2E_3F$ to be $\lambda A.\lambda P \in (2^{A-27a}).(ap V0P (ap (c_2Emin_2E_40 A P)))$

Definition 4 We define $c_2Ebool_2E_T$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 5 We define $c_2Ebool_2E_21$ to be $\lambda A.\lambda P \in (2^{A-27a}).(ap (ap (c_2Emin_2E_3D (2^{A-27a})) P))$

Definition 6 We define $c_2Earithmetic_2EMODEQ$ to be $\lambda V0n \in ty_2Enum_2Enum.\lambda V1m1 \in ty_2Enum_2Enum$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in omega \tag{4}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{omega}) \tag{5}$$

Definition 7 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 8 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (6)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (7)$$

Definition 9 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num)$

Definition 10 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earithmetic_2EBIT1))$

Definition 11 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (8)$$

Let $ty_2Eoption_2Eoption : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Eoption_2Eoption\ A0) \quad (9)$$

Let $ty_2Ellist_2Ellist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Ellist_2Ellist\ A0) \quad (10)$$

Let $c_2Ellist_2Ellist_rep : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow c_2Ellist_2Ellist_rep\ A_27a \in \\ & (((ty_2Eoption_2Eoption\ A_27a)^{ty_2Enum_2Enum})^{(ty_2Ellist_2Ellist\ A_27a)}) \end{aligned} \quad (11)$$

Let $ty_2Eone_2Eone : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eone_2Eone \quad (12)$$

Definition 12 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o\ (p\ P \Rightarrow p\ Q)$ of type ι .

Definition 13 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2))\ (\lambda V2t \in 2.)))$

Let $ty_2Esum_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Esum_2Esum\ A0\ A1) \quad (13)$$

Let $c_2Esum_2EABS_sum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Esum_2EABS_sum\ A_27a\ A_27b \in ((ty_2Esum_2Esum\ A_27a\ A_27b)^{((2^{A_27b})^{A_27a})^2}) \quad (14)$$

Definition 14 We define c_Esum_2EINL to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0e \in A_27a. (ap (c_Esum_2EABS$
Let $c_Eoption_2Eoption_ABS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Eoption_2Eoption_ABS A_27a \in ((ty_2Eoption_2Eoption A_27a)^{(ty_2Esum_2Esum A_27a ty_2Eone_2Eone)}) \quad (15)$$

Definition 15 We define $c_Eoption_2ESOME$ to be $\lambda A_27a : \iota. \lambda V0x \in A_27a. (ap (c_Eoption_2Eoption_ABS$

Definition 16 We define c_Ebool_2EF to be $(ap (c_Ebool_2E21 2) (\lambda V0t \in 2. V0t))$.

Definition 17 We define c_Ebool_2ECOND to be $\lambda A_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A_27a. (\lambda V2t2 \in A_27a. ($

Let $c_Elist_2Elist_abs : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Elist_2Elist_abs A_27a \in ((ty_2Elist_2Elist A_27a)^{(ty_2Eoption_2Eoption A_27a)^{ty_2Eenum_2Eenum}}) \quad (16)$$

Definition 18 We define $c_Elist_2ELCONS$ to be $\lambda A_27a : \iota. \lambda V0h \in A_27a. \lambda V1t \in (ty_2Elist_2Elist A_27a$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty A0 \Rightarrow nonempty (ty_2Elist_2Elist A0) \quad (17)$$

Let $c_Elist_2ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Elist_2ECONS A_27a \in (((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)})^{A_27a}) \quad (18)$$

Let $c_Elist_2ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Elist_2ENIL A_27a \in (ty_2Elist_2Elist A_27a) \quad (19)$$

Let $c_Elist_2ELENGTH : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Elist_2ELENGTH A_27a \in (ty_2Eenum_2Eenum^{(ty_2Elist_2Elist A_27a)}) \quad (20)$$

Let $c_Earithmetic_2EMOD : \iota$ be given. Assume the following.

$$c_Earithmetic_2EMOD \in ((ty_2Eenum_2Eenum^{ty_2Eenum_2Eenum})^{ty_2Eenum_2Eenum}) \quad (21)$$

Let $c_Elist_2EEL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Elist_2EEL A_27a \in ((A_27a^{(ty_2Elist_2Elist A_27a)})^{ty_2Eenum_2Eenum}) \quad (22)$$

Definition 19 We define c_Eone_2Eone to be $(ap (c_Emin_2E40 ty_2Eone_2Eone) (\lambda V0x \in ty_2Eone_2Eone$

Definition 20 We define c_Ebool_2E7E to be $(\lambda V0t \in 2. (ap (ap c_Emin_2E3D_3D_3E V0t) c_Ebool_2E$

Definition 21 We define c_Esum_2EINR to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0e \in A_27b. (ap (c_Esum_2EABS$

Definition 22 We define $c_EOption_2ENONE$ to be $\lambda A_27a : \iota. (ap (c_EOption_2EOption_ABS A_27a) ($

Definition 23 We define c_Ellist_2ELNIL to be $\lambda A_27a : \iota. (ap (c_Ellist_2Ellist_abs A_27a) (\lambda V0n \in ty$

Let $c_Ellist_2ENULL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Ellist_2ENULL A_27a \in (2^{(ty_2Ellist_2Ellist A_27a)}) \quad (23)$$

Let $c_Ellist_2ELGENLIST : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Ellist_2ELGENLIST A_27a \in (((ty_2Ellist_2Ellist A_27a)^{(ty_2EOption_2EOption ty_2Enum_2Enum)})_{(A_27a^{ty_2Enum_2Enum})}) \quad (24)$$

Definition 24 We define $c_Ellist_2ELREPEAT$ to be $\lambda A_27a : \iota. \lambda V0l \in (ty_2Ellist_2Ellist A_27a). (ap (ap$

Definition 25 We define $c_Ecombin_2EO$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda A_27c : \iota. \lambda V0f \in (A_27b^{A_27c}). \lambda V1$

Let $c_Ellist_2EGENLIST : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Ellist_2EGENLIST A_27a \in (((ty_2Ellist_2Ellist A_27a)^{(ty_2Enum_2Enum)})_{(A_27a^{ty_2Enum_2Enum})}) \quad (25)$$

Let $c_Ellist_2EfromList : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Ellist_2EfromList A_27a \in ((ty_2Ellist_2Ellist A_27a)^{(ty_2Ellist_2Ellist A_27a)}) \quad (26)$$

Let $c_Ellist_2ELAPPEND : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_Ellist_2ELAPPEND A_27a \in (((ty_2Ellist_2Ellist A_27a)^{(ty_2Ellist_2Ellist A_27a)})_{(ty_2Ellist_2Ellist A_27a)}) \quad (27)$$

Definition 26 We define $c_Emarker_2EAbbrev$ to be $\lambda V0x \in 2.V0x$.

Definition 27 We define $c_Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum$

Definition 28 We define $c_Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_Ebool_2E_21 2) (\lambda V2t \in$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. ((ap (ap c_Earithmetic_2E_2B V0m) c_2Enum_2E0) = V0m)) \quad (28)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (ap (ap c_Earithmetic_2E_2B V0m) V1n) = (ap (ap c_Earithmetic_2E_2B V1n) V0m)))) \quad (29)$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1k \in ty_2Enum_2Enum. (\\
& (p (ap (ap (ap c_2Eprim_rec_2E_3C V1k) V0n)) \Rightarrow ((ap (ap c_2Earithmetic_2EMOD \\
& V1k) V0n) = V1k)))) \\
\end{aligned} \tag{30}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1e0 \in ty_2Enum_2Enum. \\
& (\forall V2e1 \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C \\
& c_2Enum_2E0) V0n)) \Rightarrow ((p (ap (ap (ap c_2Earithmetic_2EMODEQ V0n) \\
& V1e0) V2e1)) \Rightarrow ((ap (ap c_2Earithmetic_2EMOD V1e0) V0n) = (ap (ap \\
& c_2Earithmetic_2EMOD V2e1) V0n)))))) \\
\end{aligned} \tag{31}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1x0 \in ty_2Enum_2Enum. \\
& (\forall V2x1 \in ty_2Enum_2Enum. (\forall V3y0 \in ty_2Enum_2Enum. \\
& (\forall V4y1 \in ty_2Enum_2Enum. ((p (ap (ap (ap c_2Earithmetic_2EMODEQ \\
& V0n) V1x0) V2x1)) \Rightarrow ((p (ap (ap (ap c_2Earithmetic_2EMODEQ V0n) V3y0) \\
& V4y1)) \Rightarrow (p (ap (ap (ap c_2Earithmetic_2EMODEQ V0n) (ap (ap c_2Earithmetic_2E_2B \\
& V1x0) V3y0)) (ap (ap c_2Earithmetic_2E_2B V2x1) V4y1))))))))) \\
\end{aligned} \tag{32}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1x \in ty_2Enum_2Enum. (\\
& p (ap (ap (ap c_2Earithmetic_2EMODEQ V0n) V1x) V1x))) \\
\end{aligned} \tag{33}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. ((p (ap (ap c_2Eprim_rec_2E_3C \\
& c_2Enum_2E0) V0n)) \Rightarrow (p (ap (ap (ap c_2Earithmetic_2EMODEQ V0n) \\
& V0n) c_2Enum_2E0)))) \\
\end{aligned} \tag{34}$$

Assume the following.

$$\text{True} \tag{35}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p \\
& V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \\
\end{aligned} \tag{36}$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \tag{37}$$

Assume the following.

$$(\forall V0t \in 2. ((p V0t) \vee \neg (p V0t))) \tag{38}$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_27a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \quad (39)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (40)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow \\ & True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge ((\\ & (p\ V0t) \Rightarrow False) \Leftrightarrow (\neg(p\ V0t)))))) \end{aligned} \quad (41)$$

Assume the following.

$$\begin{aligned} & ((\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge \\ & ((\neg False) \Leftrightarrow True))) \end{aligned} \quad (42)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (43)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (44)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow (\neg(p\ V0t))) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow (\neg(\\ & p\ V0t)))))) \end{aligned} \quad (45)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t1 \in A_27a. (\forall V1t2 \in \\ & A_27a. (((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ A_27a)\ c_2Ebool_2ET)\ V0t1) \\ & V1t2) = V0t1) \wedge ((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ A_27a)\ c_2Ebool_2EF) \\ & V0t1)\ V1t2) = V1t2)))) \end{aligned} \quad (46)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow \\ & ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \end{aligned} \quad (47)$$

Assume the following.

$$2.((\forall V0x \in 2.(\forall V1x_27 \in 2.(\forall V2y \in 2.(\forall V3y_27 \in 2.(((p V0x) \Leftrightarrow (p V1x_27)) \wedge ((p V1x_27) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_27)))))) \Rightarrow ((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_27) \Rightarrow (p V3y_27)))))) \Rightarrow (48)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (((p (ap (c_2Elist_2ENULL A_27a) (c_2Elist_2ENIL A_27a))) \Leftrightarrow True) \wedge (\forall V0h \in A_27a.(\forall V1t \in (ty_2Elist_2Elist A_27a).((p (ap (c_2Elist_2ENULL A_27a) (ap (c_2Elist_2ECONS A_27a) V0h) V1t))) \Leftrightarrow False)))) \Rightarrow (49)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (((ap (c_2Elist_2ELENGTH A_27a) (c_2Elist_2ENIL A_27a)) = c_2Enum_2E0) \wedge (\forall V0h \in A_27a.(\forall V1t \in (ty_2Elist_2Elist A_27a).((ap (c_2Elist_2ELENGTH A_27a) (ap (ap (c_2Elist_2ECONS A_27a) V0h) V1t)) = (ap c_2Enum_2ESUC (ap (c_2Elist_2ELENGTH A_27a) V1t)))))) \Rightarrow (50)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0l \in (ty_2Elist_2Elist A_27a).((V0l = (c_2Elist_2ENIL A_27a)) \vee (\exists V1h \in A_27a.(\exists V2t \in (ty_2Elist_2Elist A_27a).(V0l = (ap (ap (c_2Elist_2ECONS A_27a) V1h) V2t)))))) \Rightarrow (51)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0a1 \in (ty_2Elist_2Elist A_27a).(\forall V1a0 \in A_27a.(\neg((c_2Elist_2ENIL A_27a) = (ap (ap (c_2Elist_2ECONS A_27a) V1a0) V0a1)))))) \Rightarrow (52)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0l1 \in (ty_2Elist_2Elist A_27a).(\forall V1l2 \in (ty_2Elist_2Elist A_27a).((V0l1 = V1l2) \Leftrightarrow (((ap (c_2Elist_2ELENGTH A_27a) V0l1) = (ap (c_2Elist_2ELENGTH A_27a) V1l2)) \wedge (\forall V2x \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C V2x) (ap (c_2Elist_2ELENGTH A_27a) V0l1))) \Rightarrow ((ap (ap (c_2Elist_2EEL A_27a) V2x) V0l1) = (ap (ap (c_2Elist_2EEL A_27a) V2x) V1l2)))))) \Rightarrow (53)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0f \in (A_27a^{ty_2Enum_2Enum}).(\forall V1n \in ty_2Enum_2Enum.((ap (c_2Elist_2ELENGTH A_27a) (ap (ap (c_2Elist_2EGENLIST A_27a) V0f) V1n)) = V1n))) \Rightarrow (54)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0f \in (A.27a^{ty_2Enum_2Enum}). \\ (\forall V1n \in ty_2Enum_2Enum. (\forall V2x \in ty_2Enum_2Enum. (\\ (p\ (ap\ (ap\ c.2Eprim_rec_2E.3C\ V2x)\ V1n)) \Rightarrow ((ap\ (ap\ (c.2Elist_2EEL \\ A.27a)\ V2x)\ (ap\ (ap\ (c.2Elist_2EGENLIST\ A.27a)\ V0f)\ V1n)) = (ap\ V0f \\ V2x)))))) \end{aligned} \quad (55)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0h \in A.27a. (\forall V1t \in \\ (ty_2Ellist_2Ellist\ A.27a). ((\neg((ap\ (ap\ (c.2Ellist_2ELCONS\ A.27a) \\ V0h)\ V1t) = (c.2Ellist_2ELNIL\ A.27a))) \wedge (\neg((c.2Ellist_2ELNIL \\ A.27a) = (ap\ (ap\ (c.2Ellist_2ELCONS\ A.27a)\ V0h)\ V1t)))))) \end{aligned} \quad (56)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0l1 \in (ty_2Ellist_2Ellist \\ A.27a). (\forall V1l2 \in (ty_2Ellist_2Ellist\ A.27a). (((ap\ (ap\ (\\ c.2Ellist_2ELAPPEND\ A.27a)\ V0l1)\ V1l2) = (c.2Ellist_2ELNIL\ A.27a)) \Leftrightarrow \\ ((V0l1 = (c.2Ellist_2ELNIL\ A.27a)) \wedge (V1l2 = (c.2Ellist_2ELNIL \\ A.27a)))))) \end{aligned} \quad (57)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (((ap\ (c.2Ellist_2EfromList\ A.27a) \\ (c.2Elist_2ENIL\ A.27a)) = (c.2Ellist_2ELNIL\ A.27a)) \wedge (\forall V0h \in \\ A.27a. (\forall V1t \in (ty_2Elist_2Elist\ A.27a). ((ap\ (c.2Ellist_2EfromList \\ A.27a)\ (ap\ (ap\ (c.2Elist_2ECONS\ A.27a)\ V0h)\ V1t)) = (ap\ (ap\ (c.2Ellist_2ELCONS \\ A.27a)\ V0h)\ (ap\ (c.2Ellist_2EfromList\ A.27a)\ V1t)))))) \end{aligned} \quad (58)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0f \in (A.27a^{ty_2Enum_2Enum}). \\ (\forall V1n \in ty_2Enum_2Enum. ((ap\ (ap\ (c.2Ellist_2ELGENLIST \\ A.27a)\ V0f)\ (c.2Eoption_2ENONE\ ty_2Enum_2Enum)) = (ap\ (ap\ (c.2Ellist_2ELAPPEND \\ A.27a)\ (ap\ (c.2Ellist_2EfromList\ A.27a)\ (ap\ (ap\ (c.2Elist_2EGENLIST \\ A.27a)\ V0f)\ V1n)))\ (ap\ (ap\ (c.2Ellist_2ELGENLIST\ A.27a)\ (ap\ (ap \\ (c.2Ecombin_2Eo\ ty_2Enum_2Enum\ A.27a\ ty_2Enum_2Enum)\ V0f)\ (ap \\ c.2Earithmetic_2E_2B\ V1n)))\ (c.2Eoption_2ENONE\ ty_2Enum_2Enum)))))) \end{aligned} \quad (59)$$

Assume the following.

$$\begin{aligned} (\forall V0n \in ty_2Enum_2Enum. (p\ (ap\ (ap\ c.2Eprim_rec_2E.3C\ c.2Enum_2E0) \\ (ap\ c.2Enum_2ESUC\ V0n)))) \end{aligned} \quad (60)$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \quad (61)$$

Assume the following.

$$(\forall V0A \in 2.((p V0A) \Rightarrow ((\neg(p V0A)) \Rightarrow False))) \quad (62)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p V0A) \vee (p V1B))) \Rightarrow False) \Leftrightarrow ((p V0A) \Rightarrow False) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))) \quad (63)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((\neg(p V0A)) \vee (p V1B))) \Rightarrow False) \Leftrightarrow ((p V0A) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))) \quad (64)$$

Assume the following.

$$(\forall V0A \in 2.(((\neg(p V0A)) \Rightarrow False) \Rightarrow (((p V0A) \Rightarrow False) \Rightarrow False))) \quad (65)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (p V1q) \Leftrightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee (p V1q) \vee (p V2r)) \wedge (((p V0p) \vee (\neg(p V2r)) \vee (\neg(p V1q)))) \wedge (((p V1q) \vee (\neg(p V2r)) \vee (\neg(p V0p)))) \wedge ((p V2r) \vee ((\neg(p V1q)) \vee (\neg(p V0p)))))))))) \quad (66)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (p V1q) \Rightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge (\neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p)))))))) \quad (67)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (p V0p)))) \quad (68)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (\neg(p V1q)))) \quad (69)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V0p)))) \quad (70)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V1q)))) \quad (71)$$

Assume the following.

$$(\forall V0p \in 2.(((\neg(\neg(p V0p))) \Rightarrow (p V0p))) \quad (72)$$

Theorem 1

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0l \in (ty_2Elist_2Elist A_27a).((ap (c_2Elist_2ELREPEAT A_27a) V0l) = (ap (ap (c_2Elist_2ELAPPEND A_27a) (ap (c_2Elist_2EfromList A_27a) V0l)) (ap (c_2Elist_2ELREPEAT A_27a) V0l))))$$