

thm_2Emachine_ieee_2Efp32_mul_sub
(TMYXX72UU4Ba88TRFVTKwp6jo72LVm2bbQu)

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Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{1}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{2}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \tag{3}$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 3 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \tag{4}$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \tag{5}$$

Definition 4 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 5 We define $c_2Ebool_2E_21$ to be $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c_2Emin_2E_3D\ (2^{A-27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V1x \in 2.V1x)))$

Definition 6 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num\ (c_2Enum_2ESUC_REP\ m))$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \tag{6}$$

Definition 7 We define $c_Earithmetic_EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_Earithmetic_2EEXP$

Definition 8 We define $c_Earithmetic_ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 9 We define $c_Earithmetic_EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_Earithmetic_2EEXP$

Let $c_Earithmetic_2EEXP : \iota$ be given. Assume the following.

$$c_Earithmetic_2EEXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (7)$$

Let $c_Earithmetic_2EDIV : \iota$ be given. Assume the following.

$$c_Earithmetic_2EDIV \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (8)$$

Definition 10 We define $c_Ebit_2EDIV_2EXP$ to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Let $c_Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (9)$$

Let $c_Earithmetic_2EMOD : \iota$ be given. Assume the following.

$$c_Earithmetic_2EMOD \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (10)$$

Definition 11 We define $c_Ebit_2EMOD_2EXP$ to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 12 We define c_Ebit_2EBITS to be $\lambda V0h \in ty_2Enum_2Enum.\lambda V1l \in ty_2Enum_2Enum.\lambda V$

Definition 13 We define c_Ebit_2EBIT to be $\lambda V0b \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap$

Let $ty_2EfcP_2Efinite_image : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty_2EfcP_2Efinite_image A0) \quad (11)$$

Let $ty_2Ebool_2Eitself : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty_2Ebool_2Eitself A0) \quad (12)$$

Let $c_Ebool_2Ethe_value : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_Ebool_2Ethe_value A_27a \in (ty_2Ebool_2Eitself A_27a) \quad (13)$$

Let $c_2EfcP_2Edimindex : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2EfcP_2Edimindex A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself A_27a)}) \quad (14)$$

Definition 14 We define c_Ebool_2EF to be $(ap (c_Ebool_2E.21 2) (\lambda V0t \in 2.V0t))$.

Definition 15 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 16 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2E_7E))$

Definition 17 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.(ap (c_2Emin_2E_3D_3D_3E V2t) c_2Ebool_2E_7E))))$

Definition 18 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\mathbf{if} (\exists x \in A.p (ap P x)) \mathbf{then} (the (\lambda x.x \in A.\lambda y.p (ap P y)))$ of type $\iota \Rightarrow \iota$.

Definition 19 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_40 A_27a) P)))$

Definition 20 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (c_2Emin_2E_40 A_27a) P)$

Definition 21 We define $c_2Ebool_2E_3F_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap c_2Ebool_2E_2F_5C A_27a) P))$

Definition 22 We define $c_2Efcp_2Efinite_index$ to be $\lambda A_27a : \iota.(ap (c_2Emin_2E_40 A_27a) (ty_2Enum_2Enum A_27a))$

Let $ty_2Efcp_2Ecart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty_2Efcp_2Ecart A0 A1) \quad (15)$$

Let $c_2Efcp_2Edest_cart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Efcp_2Edest_cart A_27a A_27b \in ((A_27a)^{(ty_2Efcp_2Efinite_image A_27b)})^{(ty_2Efcp_2Ecart A_27a A_27b)} \quad (16)$$

Definition 23 We define $c_2Efcp_2Efcp_index$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in (ty_2Efcp_2Ecart A_27a A_27b)$

Definition 24 We define c_2Efcp_2EFCP to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0g \in (A_27a)^{(ty_2Enum_2Enum)})^{(ap (c_2Emin_2E_40 A_27a) g)}$

Definition 25 We define $c_2Ewords_2En2w$ to be $\lambda A_27a : \iota.\lambda V0n \in ty_2Enum_2Enum.(ap (c_2Efcp_2EFCP A_27a) n)$

Let $ty_2Eone_2Eone : \iota$ be given. Assume the following.

$$nonempty ty_2Eone_2Eone \quad (17)$$

Let $ty_2Ebinary_ieee_2Efloat : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty_2Ebinary_ieee_2Efloat A0 A1) \quad (18)$$

Let $c_2Ebinary_ieee_2Efloat_Sign : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty A_27t \Rightarrow \forall A_27w.nonempty A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_Sign A_27t A_27w \in ((ty_2Efcp_2Ecart 2 ty_2Eone_2Eone)^{(ty_2Ebinary_ieee_2Efloat A_27t A_27w)}) \quad (19)$$

Definition 26 We define $c_2Ewords_2Eword_xor$ to be $\lambda A_27a : \iota. \lambda V0v \in (ty_2EfcP_2Ecart\ 2\ A_27a). \lambda V1$
 Let $ty_2Erealax_2Ereal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Erealax_2Ereal \quad (20)$$

Let $c_2Ereal_2Ereal_of_num : \iota$ be given. Assume the following.

$$c_2Ereal_2Ereal_of_num \in (ty_2Erealax_2Ereal^{ty_2Enum_2Enum}) \quad (21)$$

Let $c_2Ereal_2Epow : \iota$ be given. Assume the following.

$$c_2Ereal_2Epow \in ((ty_2Erealax_2Ereal^{ty_2Enum_2Enum})^{ty_2Erealax_2Ereal}) \quad (22)$$

Let $c_2Ebinaary_2ieee_2Efloat_2Significand : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t. nonempty\ A_27t \Rightarrow \forall A_27w. nonempty\ A_27w \Rightarrow c_2Ebinaary_2ieee_2Efloat_2Significand\ A_27t\ A_27w \in ((ty_2EfcP_2Ecart\ 2\ A_27t)^{(ty_2Ebinaary_2ieee_2Efloat\ A_27t\ A_27w)}) \quad (23)$$

Definition 27 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A_27a. (\lambda V2t2 \in A_27a. ($

Definition 28 We define c_2Ebit_2ESBIT to be $\lambda V0b \in 2. \lambda V1n \in ty_2Enum_2Enum. (ap\ (ap\ (ap\ (c_2Ebooc$

Let $c_2Esum_num_2ESUM : \iota$ be given. Assume the following.

$$c_2Esum_num_2ESUM \in ((ty_2Enum_2Enum^{(ty_2Enum_2Enum^{ty_2Enum_2Enum})})^{ty_2Enum_2Enum}) \quad (24)$$

Definition 29 We define $c_2Ewords_2Ew2n$ to be $\lambda A_27a : \iota. \lambda V0w \in (ty_2EfcP_2Ecart\ 2\ A_27a). (ap\ (ap\ c$

Let $ty_2Ehreal_2Ehreal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ehreal_2Ehreal \quad (25)$$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow \forall A1. nonempty\ A1 \Rightarrow nonempty\ (ty_2Epair_2Eprod\ A0\ A1) \quad (26)$$

Let $c_2Erealax_2Ereal_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_REP_CLASS \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{ty_2Erealax}) \quad (27)$$

Definition 30 We define $c_2Erealax_2Ereal_REP$ to be $\lambda V0a \in ty_2Erealax_2Ereal. (ap\ (c_2Emin_2E40\ (t$

Let $c_2Erealax_2Etreal_inv : \iota$ be given. Assume the following.

$$c_2Erealax_2Etreal_inv \in ((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}) \quad (28)$$

Let $c_2Erealax_2Etreal_eq : \iota$ be given. Assume the following.

$$c_2Erealax_2Etreal_eq \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)}) \quad (29)$$

Let $c_2Erealax_2Ereal_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_ABS_CLASS \in (ty_2Erealax_2Ereal)^{(2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})} \quad (30)$$

Definition 31 We define $c_2Erealax_2Ereal_ABS$ to be $\lambda V0r \in (ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)$

Definition 32 We define $c_2Erealax_2Einv$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.(ap\ c_2Erealax_2Ereal_ABS$

Let $c_2Erealax_2Etreal_mul : \iota$ be given. Assume the following.

$$c_2Erealax_2Etreal_mul \in (((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)}) \quad (31)$$

Definition 33 We define $c_2Erealax_2Ereal_mul$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.\lambda V1T2 \in ty_2Erealax_2Ereal.$

Definition 34 We define $c_2Ereal_2E_2F$ to be $\lambda V0x \in ty_2Erealax_2Ereal.\lambda V1y \in ty_2Erealax_2Ereal.$

Let $c_2Erealax_2Etreal_add : \iota$ be given. Assume the following.

$$c_2Erealax_2Etreal_add \in (((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)}) \quad (32)$$

Definition 35 We define $c_2Erealax_2Ereal_add$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.\lambda V1T2 \in ty_2Erealax_2Ereal.$

Let $c_2Ewords_2EINT_MAX : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ewords_2EINT_MAX\ A_27a \in (ty_2Enum_2Enum)^{(ty_2Ebool_2Eitself\ A_27a)} \quad (33)$$

Let $c_2Ebinary_ieee_2Efloat_Exponent : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_Exponent\ A_27t\ A_27w \in ((ty_2EfcP_2Ecart\ 2\ A_27w)^{(ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)}) \quad (34)$$

Let $c_2Erealax_2Etreal_neg : \iota$ be given. Assume the following.

$$c_2Erealax_2Etreal_neg \in ((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}) \quad (35)$$

Definition 36 We define $c_2Erealax_2Ereal_neg$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.(ap\ c_2Erealax_2Ereal$

Definition 37 We define $c_2Ebinary_ieee_2Efloat_to_real$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_2Ebinary_$

Let $ty_2Ebinary_ieee_2Efloat_value : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ebinary_ieee_2Efloat_value \quad (36)$$

Let $c_2Ebinary_ieee_2Efloat : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Efloat \in (ty_2Ebinary_ieee_2Efloat_value^{ty_2Erealax_2Ereal}) \quad (37)$$

Let $c_2Ebinary_ieee_2ENaN : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2ENaN \in ty_2Ebinary_ieee_2Efloat_value \quad (38)$$

Let $c_2Ebinary_ieee_2EInfinity : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2EInfinity \in ty_2Ebinary_ieee_2Efloat_value \quad (39)$$

Let $c_2Ewords_2EUINT_MAX : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ewords_2EUINT_MAX\ A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself\ A_27a)}) \quad (40)$$

Definition 38 We define $c_2Ewords_2Eword_T$ to be $\lambda A_27a : \iota.(ap\ (c_2Ewords_2En2w\ A_27a)\ (ap\ (c_2Ew$

Definition 39 We define $c_2Ebinary_ieee_2Efloat_value$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_2Ebinary_$

Let $c_2Ebinary_ieee_2Efloat_value_CASE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ebinary_ieee_2Efloat_value_CASE\ A_27a \in (((A_27a^{A_27a})^{A_27a})^{(A_27a^{ty_2Erealax_2Ereal})})^{ty_2Ebinary_ieee_2Efloat_value} \quad (41)$$

Definition 40 We define $c_2Ebinary_ieee_2Efloat_is_infinite$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_2Ebin$

Definition 41 We define $c_2Ebool_2E5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E21\ 2)\ (\lambda V2t \in$

Definition 42 We define $c_2Ereal_2Ereal_sub$ to be $\lambda V0x \in ty_2Erealax_2Ereal.\lambda V1y \in ty_2Erealax_2E$

Let $ty_2Ebinary_ieee_2ERounding : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ebinary_ieee_2ERounding \quad (42)$$

Let $c_2Ebinary_ieee_2ERoundTowardNegative : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2ERoundTowardNegative \in ty_2Ebinary_ieee_2ERounding \quad (43)$$

Let $c_2Erealax_2Etrealm_lt : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealm_lt \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{(ty_2Epair_2Eprod\ ty_2Eh$$
 (44)

Definition 43 We define $c_Erealax_Ereal_lt$ to be $\lambda V0T1 \in ty_Erealax_Ereal.\lambda V1T2 \in ty_Erealax_Ereal.$

Definition 44 We define $c_Ereal_Ereal_lte$ to be $\lambda V0x \in ty_Erealax_Ereal.\lambda V1y \in ty_Erealax_Ereal.$

Definition 45 We define c_Ereal_Eabs to be $\lambda V0x \in ty_Erealax_Ereal.(ap (ap (ap (c_Ebool_ECONJ))$

Let $c_Ebinary_ieee_Elargest : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27t.nonempty A_27t \Rightarrow \forall A_27w.nonempty A_27w \Rightarrow c_Ebinary_ieee_Elargest \\ & A_27t A_27w \in (ty_Erealax_Ereal^{(ty_Ebool_Eitself (ty_Epair_Eprod A_27t A_27w))}) \end{aligned} \quad (45)$$

Definition 46 We define $c_Ebinary_ieee_Efloat_is_finite$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_Ebinary_ieee_Efloat_is_finite$

Let $c_Epair_EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_Epair_EABS_prod \\ & A_27a A_27b \in ((ty_Epair_Eprod A_27a A_27b)^{(2^{A_27b})^{A_27a}}) \end{aligned} \quad (46)$$

Definition 47 We define $c_Epair_E_2C$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in A_27a.\lambda V1y \in A_27b.(ap (c_Epair_E_2C$

Let $c_Epred_set_EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_Epred_set_EGSPEC \\ & A_27a A_27b \in ((2^{A_27a})^{(ty_Epair_Eprod A_27a 2)^{A_27b}}) \end{aligned} \quad (47)$$

Definition 48 We define $c_Ecombin_EK$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0x \in A_27a.(\lambda V1y \in A_27b.V0x))$

Definition 49 We define c_Ebool_EIN to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.(\lambda V1f \in (2^{A_27a}).(ap V1f V0x)))$

Definition 50 We define $c_Ebinary_ieee_Eis_closest$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0s \in (2^{(ty_Ebinary_ieee_Efloat_is_closest$

Definition 51 We define $c_Ebinary_ieee_Eclosest_such$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0p \in (2^{(ty_Ebinary_ieee_Efloat_is_closest$

Definition 52 We define $c_Ebinary_ieee_Eclosest$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(ap (c_Ebinary_ieee_Eclosest$

Let $c_Ebinary_ieee_Efloat_top : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27t.nonempty A_27t \Rightarrow \forall A_27w.nonempty A_27w \Rightarrow c_Ebinary_ieee_Efloat_top \\ & A_27t A_27w \in ((ty_Ebinary_ieee_Efloat A_27t A_27w)^{(ty_Ebool_Eitself (ty_Epair_Eprod A_27t A_27w))}) \end{aligned} \quad (48)$$

Definition 53 We define $c_Ereal_Ereal_gt$ to be $\lambda V0x \in ty_Erealax_Ereal.\lambda V1y \in ty_Erealax_Ereal.$

Let $c_Ebinary_ieee_Efloat_bottom : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27t.nonempty A_27t \Rightarrow \forall A_27w.nonempty A_27w \Rightarrow c_Ebinary_ieee_Efloat_bottom \\ & A_27t A_27w \in ((ty_Ebinary_ieee_Efloat A_27t A_27w)^{(ty_Ebool_Eitself (ty_Epair_Eprod A_27t A_27w))}) \end{aligned} \quad (49)$$

Definition 54 We define c_2Ebool_2ELET to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0f \in (A_27b^{A_27a}).(\lambda V1x \in A_27w$

Let $c_2Ebinary_ieee_2Efloat_minus_infinity : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_minus_infinity\ A_27t\ A_27w \in ((ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)^{(ty_2Ebool_2Eitself\ (ty_2Epair_2Eprod\ A_27t\ A_27w))}) \quad (50)$$

Definition 55 We define $c_2Ereal_2Ereal_ge$ to be $\lambda V0x \in ty_2Erealax_2Ereal.\lambda V1y \in ty_2Erealax_2Ereal$

Let $c_2Ebinary_ieee_2Efloat_plus_infinity : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_plus_infinity\ A_27t\ A_27w \in ((ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)^{(ty_2Ebool_2Eitself\ (ty_2Epair_2Eprod\ A_27t\ A_27w))}) \quad (51)$$

Let $c_2Ebinary_ieee_2Ethreshold : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Ethreshold\ A_27t\ A_27w \in (ty_2Erealax_2Ereal^{(ty_2Ebool_2Eitself\ (ty_2Epair_2Eprod\ A_27t\ A_27w))}) \quad (52)$$

Definition 56 We define $c_2Ewords_2Eword_lsb$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efcpcart\ 2\ A_27a).(\lambda V1$

Let $c_2Ebinary_ieee_2Erounding2num : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Erounding2num \in (ty_2Enum_2Enum^{ty_2Ebinary_ieee_2Erounding}) \quad (53)$$

Definition 57 We define $c_2Ebinary_ieee_2Erounding_CASE$ to be $\lambda A_27a : \iota.\lambda V0x \in ty_2Ebinary_ieee_2Erounding$

Definition 58 We define $c_2Ebinary_ieee_2Eround$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0mode \in ty_2Ebinary_ieee_2Eround$

Let $c_2Ebinary_ieee_2Efloat_plus_zero : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_plus_zero\ A_27t\ A_27w \in ((ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)^{(ty_2Ebool_2Eitself\ (ty_2Epair_2Eprod\ A_27t\ A_27w))}) \quad (54)$$

Let $c_2Ebinary_ieee_2Efloat_minus_zero : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_minus_zero\ A_27t\ A_27w \in ((ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)^{(ty_2Ebool_2Eitself\ (ty_2Epair_2Eprod\ A_27t\ A_27w))}) \quad (55)$$

Definition 59 We define $c_2Ebinary_ieee_2Efloat_is_zero$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_2Ebinary_ieee_2Efloat_is_zero$

Definition 60 We define $c_2Ebinary_ieee_2Efloat_round$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0mode \in ty_2Ebinary_ieee_2Efloat_round$

Let $ty_2Ebinary_ieee_2Eflags : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ebinary_ieee_2Eflags \quad (56)$$

Let $c_2Ebool_2EARB : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Ebool_2EARB\ A_27a \in A_27a \quad (57)$$

Let $c_2Ebinary_ieee_2Eflags_Underflow_AfterRounding_fupd : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Eflags_Underflow_AfterRounding_fupd \in ((ty_2Ebinary_ieee_2Eflags)^{ty_2Ebinary_ieee_2Eflags})^{(2^2)} \quad (58)$$

Let $c_2Ebinary_ieee_2Eflags_Underflow_BeforeRounding_fupd : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Eflags_Underflow_BeforeRounding_fupd \in ((ty_2Ebinary_ieee_2Eflags)^{ty_2Ebinary_ieee_2Eflags})^{(2^2)} \quad (59)$$

Let $c_2Ebinary_ieee_2Eflags_Precision_fupd : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Eflags_Precision_fupd \in ((ty_2Ebinary_ieee_2Eflags)^{ty_2Ebinary_ieee_2Eflags})^{(2^2)} \quad (60)$$

Let $c_2Ebinary_ieee_2Eflags_Overflow_fupd : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Eflags_Overflow_fupd \in ((ty_2Ebinary_ieee_2Eflags)^{ty_2Ebinary_ieee_2Eflags})^{(2^2)} \quad (61)$$

Let $c_2Ebinary_ieee_2Eflags_InvalidOp_fupd : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Eflags_InvalidOp_fupd \in ((ty_2Ebinary_ieee_2Eflags)^{ty_2Ebinary_ieee_2Eflags})^{(2^2)} \quad (62)$$

Let $c_2Ebinary_ieee_2Eflags_DivideByZero_fupd : \iota$ be given. Assume the following.

$$c_2Ebinary_ieee_2Eflags_DivideByZero_fupd \in ((ty_2Ebinary_ieee_2Eflags)^{ty_2Ebinary_ieee_2Eflags})^{(2^2)} \quad (63)$$

Definition 61 We define $c_2Ebinary_ieee_2Eclear_flags$ to be $(ap\ (ap\ c_2Ebinary_ieee_2Eflags_DivideByZero_fupd))$

Let $c_2Ewords_2EINT_MIN : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Ewords_2EINT_MIN\ A_27a \in (ty_2Enum_2Enum)^{(ty_2Ebool_2Eitself\ A_27a)} \quad (64)$$

Let $ty_2Esum_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow \forall A1. nonempty\ A1 \Rightarrow nonempty\ (ty_2Esum_2Esum\ A0\ A1) \quad (65)$$

Let $c_2Ewords_2Edimword : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ewords_2Edimword\ A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself\ A_27a)}) \quad (66)$$

Definition 62 We define $c_2Ewords_2Eword_2comp$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).$

Definition 63 We define $c_2Ewords_2Eword_2msb$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).$

Definition 64 We define $c_2Ewords_2Enzcv$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1b \in ($

Let $c_2Epair_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2ESND\ A_27a\ A_27b \in (A_27b^{(ty_2Epair_2Eprod\ A_27a\ A_27b)}) \quad (67)$$

Let $c_2Epair_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2EFST\ A_27a\ A_27b \in (A_27a^{(ty_2Epair_2Eprod\ A_27a\ A_27b)}) \quad (68)$$

Definition 65 We define $c_2Epair_2EUNCURRY$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in ((A_27c^{A_27a$

Definition 66 We define $c_2Ewords_2Eword_2ls$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1b$

Definition 67 We define $c_2Ebinary_2ieee_2Efloat_2round_2with_2flags$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0mode$

Let $ty_2Ebinary_2ieee_2Efp_2op : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Ebinary_2ieee_2Efp_2op\ A0\ A1) \quad (69)$$

Let $c_2Ebinary_2ieee_2EFP_2MulAdd : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$A_27t\ A_27w \in (((((ty_2Ebinary_2ieee_2Efp_2op\ A_27t\ A_27w)^{(ty_2Ebinary_2ieee_2Efloat\ A_27t\ A_27w)})^{(ty_2E$$

Definition 68 We define $c_2Ebinary_2ieee_2Efloat_2is_2nan$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_2Ebinary_2ieee_2Efloat_2is_2nan$

Definition 69 We define $c_2Ebinary_2ieee_2Efloat_2is_2signalling$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0x \in (ty_2Ebinary_2ieee_2Efloat_2is_2signalling$

Definition 70 We define $c_2Ebinary_2ieee_2Efloat_2some_2qnan$ to be $\lambda A_27t : \iota.\lambda A_27w : \iota.\lambda V0fp_2op \in (ty_2Ebinary_2ieee_2Efloat_2some_2qnan$

Definition 71 We define $c_2Ebinary_2ieee_2Einvalidop_2flags$ to be $(ap\ (ap\ c_2Ebinary_2ieee_2Eflags_2Inv$

Let $c_2Ebinary_ieee_2Efloat_Significand_fupd : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27u.nonempty\ A_27u \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_Significand_fupd\ A_27t\ A_27u\ A_27w \in \\ & ((ty_2Ebinary_ieee_2Efloat\ A_27u\ A_27w)^{(ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)}) \end{aligned} \quad (78)$$

Let $c_2Ebinary_ieee_2Efloat_Exponent_fupd : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow \forall A_27x.nonempty\ A_27x \Rightarrow c_2Ebinary_ieee_2Efloat_Exponent_fupd\ A_27t\ A_27w\ A_27x \in \\ & (((ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27x)^{(ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)})^{(ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)}) \end{aligned} \quad (79)$$

Let $c_2Ebinary_ieee_2Efloat_Sign_fupd : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27t.nonempty\ A_27t \Rightarrow \forall A_27w.nonempty\ A_27w \Rightarrow c_2Ebinary_ieee_2Efloat_Sign_fupd\ A_27t\ A_27w \in \\ & (((ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)^{(ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)})^{(ty_2Ebinary_ieee_2Efloat\ A_27t\ A_27w)}) \end{aligned} \quad (80)$$

Definition 80 We define $c_2Emachine_ieee_2Efp32_to_float$ to be $\lambda V0w \in (ty_2Efc_2Ecart\ 2\ (ty_2Efc_2Ecart\ 2\ A_27a)).\lambda V1w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1w$

Definition 81 We define $c_2Ewords_2Eword_lsl$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1w \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1w$

Definition 82 We define $c_2Ewords_2Eword_or$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1v$

Definition 83 We define $c_2Ewords_2Eword_join$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1v$

Definition 84 We define $c_2Ewords_2Eword_concat$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1v \in (ty_2Efc_2Ecart\ 2\ A_27a).\lambda V1v$

Definition 85 We define $c_2Emachine_ieee_2Efloat_to_fp32$ to be $\lambda V0x \in (ty_2Ebinary_ieee_2Efloat\ (ap\ c_2Emachine_ieee_2Efloat_to_fp32\ V0x)) = V0x$

Definition 86 We define $c_2Emachine_ieee_2Efp32_mul_sub$ to be $\lambda V0mode \in ty_2Ebinary_ieee_2Efloat_to_fp32$

Assume the following.

$$\begin{aligned} & (\forall V0x \in (ty_2Ebinary_ieee_2Efloat\ (ty_2Efc_2Ebit1\ (\\ & ty_2Efc_2Ebit1\ (ty_2Efc_2Ebit1\ (ty_2Efc_2Ebit0\ ty_2Eone_2Eone)))) \\ & (ty_2Efc_2Ebit0\ (ty_2Efc_2Ebit0\ (ty_2Efc_2Ebit0\ ty_2Eone_2Eone))))). \\ & ((ap\ c_2Emachine_ieee_2Efp32_to_float\ (ap\ c_2Emachine_ieee_2Efloat_to_fp32 \\ & V0x)) = V0x) \end{aligned} \quad (81)$$

Theorem 1

$$\begin{aligned}
 & ((\forall V0mode \in ty_2Ebinary_ieee_2Errounding. (\forall V1c \in \\
 & (ty_2Ebinary_ieee_2Efloat (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 \\
 & (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 \\
 & (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone))))). (\forall V2b \in \\
 & (ty_2Ebinary_ieee_2Efloat (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 \\
 & (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 \\
 & (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone))))). (\forall V3a \in \\
 & (ty_2Ebinary_ieee_2Efloat (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 \\
 & (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 \\
 & (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone))))). ((ap \\
 (ap (ap (ap c_2Emachine_ieee_2Efp32_mul_sub V0mode) (ap c_2Emachine_ieee_2Efloat_to_fp32 \\
 V3a)) (ap c_2Emachine_ieee_2Efloat_to_fp32 V2b)) (ap c_2Emachine_ieee_2Efloat_to_fp32 \\
 V1c)) = (ap c_2Emachine_ieee_2Efloat_to_fp32 (ap (c_2Epair_2ESND \\
 ty_2Ebinary_ieee_2Eflags (ty_2Ebinary_ieee_2Efloat (ty_2EfcP_2Ebit1 \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))))) \\
 (ap (ap (ap (ap (c_2Ebinary_ieee_2Efloat_mul_sub (ty_2EfcP_2Ebit1 \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) \\
 V0mode) V3a) V2b) V1c)))))) \wedge ((\forall V4mode \in ty_2Ebinary_ieee_2Errounding. \\
 (\forall V5c \in ty_2Enum_2Enum. (\forall V6b \in (ty_2Ebinary_ieee_2Efloat \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone))))). (\forall V7a \in (ty_2Ebinary_ieee_2Efloat \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone))))). ((ap (ap (ap (ap c_2Emachine_ieee_2Efp32_mul_sub \\
 V4mode) (ap c_2Emachine_ieee_2Efloat_to_fp32 V7a)) (ap c_2Emachine_ieee_2Efloat_to_fp32 \\
 V6b)) (ap (c_2Ewords_2En2w (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))))) \\
 V5c)) = (ap c_2Emachine_ieee_2Efloat_to_fp32 (ap (c_2Epair_2ESND \\
 ty_2Ebinary_ieee_2Eflags (ty_2Ebinary_ieee_2Efloat (ty_2EfcP_2Ebit1 \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))))) \\
 (ap (ap (ap (ap (c_2Ebinary_ieee_2Efloat_mul_sub (ty_2EfcP_2Ebit1 \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) \\
 V4mode) V7a) V6b) (ap c_2Emachine_ieee_2Efp32_to_float (ap \\
 (c_2Ewords_2En2w (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))))) V5c)))))) \wedge \\
 ((\forall V8mode \in ty_2Ebinary_ieee_2Errounding. (\forall V9c \in \\
 (ty_2Ebinary_ieee_2Efloat (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone))))). (\forall V10b \in \\
 ty_2Enum_2Enum. (\forall V11a \in (ty_2Ebinary_ieee_2Efloat (\\
 ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone))))). ((ap (ap (ap (ap c_2Emachine_ieee_2Efp32_mul_sub \\
 V8mode) (ap c_2Emachine_ieee_2Efloat_to_fp32 V11a)) (ap (\\
 c_2Ewords_2En2w (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 ty_2Eone_2Eone)))))) V10b)) \\
 (ap c_2Emachine_ieee_2Efloat_to_fp32 V9c)) = (ap c_2Emachine_ieee_2Efloat_to_fp32 \\
 (ap (c_2Epair_2ESND ty_2Ebinary_ieee_2Eflags (ty_2Ebinary_ieee_2Efloat \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))))) (ap (ap (ap (ap (c_2Ebinary_ieee_2Efloat_mul_sub \\
 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit1 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))) (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 (ty_2EfcP_2Ebit0 \\
 ty_2Eone_2Eone)))))) V8mode) V11a) (ap c_2Emachine_ieee_2Efp32_to_float
 \end{aligned}$$