

# thm\_2Emachine\_ieee\_2Efp64\_isNormal (TMXs9J6Lwb7fuMFicvopstW2ZScx8688Psh)

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Let  $c\_2Enum\_2EZERO\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2EZERO\_REP \in \omega \tag{1}$$

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Enum\_2Enum \tag{2}$$

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{\omega}) \tag{3}$$

**Definition 1** We define  $c\_2Emin\_2E3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 2** We define  $c\_2Enum\_2E0$  to be  $(ap\ c\_2Enum\_2EABS\_num\ c\_2Enum\_2EZERO\_REP)$ .

**Definition 3** We define  $c\_2Earithmetic\_2EZERO$  to be  $c\_2Enum\_2E0$ .

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \tag{4}$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega}) \tag{5}$$

**Definition 4** We define  $c\_2Ebool\_2ET$  to be  $(ap\ (ap\ (c\_2Emin\_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

**Definition 5** We define  $c\_2Ebool\_2E21$  to be  $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap\ (ap\ (c\_2Emin\_2E3D\ (2^{A-27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V1x \in 2.V1x))$

**Definition 6** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.(ap\ c\_2Enum\_2EABS\_num\ (ap\ (ap\ (c\_2Emin\_2E3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Let  $c\_2Earithmetic\_2E2B : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2E2B \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \tag{6}$$

**Definition 7** We define  $c\_Earithmetic\_EBIT1$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap (ap c\_Earithmetic\_2E$

**Definition 8** We define  $c\_Earithmetic\_ENUMERAL$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.V0x$ .

**Definition 9** We define  $c\_Earithmetic\_EBIT2$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap (ap c\_Earithmetic\_2E$

Let  $c\_Earithmetic\_EEXP : \iota$  be given. Assume the following.

$$c\_Earithmetic\_EEXP \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (7)$$

Let  $c\_Earithmetic\_EDIV : \iota$  be given. Assume the following.

$$c\_Earithmetic\_EDIV \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (8)$$

**Definition 10** We define  $c\_Ebit\_EDIV\_2EXP$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

Let  $c\_Earithmetic\_E\_2D : \iota$  be given. Assume the following.

$$c\_Earithmetic\_E\_2D \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (9)$$

Let  $c\_Earithmetic\_EMOD : \iota$  be given. Assume the following.

$$c\_Earithmetic\_EMOD \in ((ty\_2Enum\_2Enum^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum}) \quad (10)$$

**Definition 11** We define  $c\_Ebit\_EMOD\_2EXP$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

**Definition 12** We define  $c\_Ebit\_EBITS$  to be  $\lambda V0h \in ty\_2Enum\_2Enum.\lambda V1l \in ty\_2Enum\_2Enum.\lambda V$

**Definition 13** We define  $c\_Ebit\_EBIT$  to be  $\lambda V0b \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum.(ap$

Let  $ty\_2EfcP\_2Efinite\_image : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty\_2EfcP\_2Efinite\_image A0) \quad (11)$$

Let  $ty\_2Ebool\_2Eitself : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty\_2Ebool\_2Eitself A0) \quad (12)$$

Let  $c\_Ebool\_2Ethe\_value : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_Ebool\_2Ethe\_value A\_27a \in (ty\_2Ebool\_2Eitself A\_27a) \quad (13)$$

Let  $c\_2EfcP\_2Edimindex : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2EfcP\_2Edimindex A\_27a \in (ty\_2Enum\_2Enum^{(ty\_2Ebool\_2Eitself A\_27a)}) \quad (14)$$

**Definition 14** We define  $c\_Ebool\_2EF$  to be  $(ap (c\_Ebool\_2E.21 2)) (\lambda V0t \in 2.V0t)$ .

**Definition 15** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p P \Rightarrow Q)$  of type  $\iota$ .

**Definition 16** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2.(ap (ap c\_2Emin\_2E\_3D\_3D\_3E V0t) c\_2Ebool\_2E\_7E$

**Definition 17** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in$

**Definition 18** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x))$  then (the  $(\lambda x.x \in A \wedge$  of type  $\iota \Rightarrow \iota$ ).

**Definition 19** We define  $c\_2Ebool\_2E\_3F$  to be  $\lambda A\_27a : \iota.(\lambda V0P \in (2^{A\_27a}).(ap V0P (ap (c\_2Emin\_2E\_40$

**Definition 20** We define  $c\_2Eprim\_rec\_2E\_3C$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

**Definition 21** We define  $c\_2Ebool\_2E\_3F\_21$  to be  $\lambda A\_27a : \iota.(\lambda V0P \in (2^{A\_27a}).(ap (ap c\_2Ebool\_2E\_2F\_5C$

**Definition 22** We define  $c\_2Efcp\_2Efinite\_index$  to be  $\lambda A\_27a : \iota.(ap (c\_2Emin\_2E\_40 (A\_27a^{ty\_2Enum\_2Enum}$

Let  $ty\_2Efcp\_2Ecart : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty\_2Efcp\_2Ecart A0 A1) \quad (15)$$

Let  $c\_2Efcp\_2Edest\_cart : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2Efcp\_2Edest\_cart A\_27a A\_27b \in ((A\_27a^{(ty\_2Efcp\_2Efinite\_image A\_27b)})^{(ty\_2Efcp\_2Ecart A\_27a A\_27b)}) \quad (16)$$

**Definition 23** We define  $c\_2Efcp\_2Efcp\_index$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0x \in (ty\_2Efcp\_2Ecart A\_27a$

**Definition 24** We define  $c\_2Efcp\_2EFCP$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.(\lambda V0g \in (A\_27a^{ty\_2Enum\_2Enum}).(ap$

**Definition 25** We define  $c\_2Ewords\_2En2w$  to be  $\lambda A\_27a : \iota.\lambda V0n \in ty\_2Enum\_2Enum.(ap (c\_2Efcp\_2EFCP$

Let  $c\_2Ewords\_2EUINT\_MAX : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Ewords\_2EUINT\_MAX A\_27a \in (ty\_2Enum\_2Enum^{(ty\_2Ebool\_2Eitself A\_27a)}) \quad (17)$$

**Definition 26** We define  $c\_2Ewords\_2Eword\_T$  to be  $\lambda A\_27a : \iota.(ap (c\_2Ewords\_2En2w A\_27a) (ap (c\_2Ew$

Let  $ty\_2Ebinary\_ieee\_2Efloat : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty\_2Ebinary\_ieee\_2Efloat A0 A1) \quad (18)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Exponent : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27t.nonempty A\_27t \Rightarrow \forall A\_27w.nonempty A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Exponent A\_27t A\_27w \in ((ty\_2Efcp\_2Ecart 2 A\_27w)^{(ty\_2Ebinary\_ieee\_2Efloat A\_27t A\_27w)}) \quad (19)$$

**Definition 27** We define  $c\_Ebinary\_ieee\_Efloat\_is\_normal$  to be  $\lambda A\_27t : \iota.\lambda A\_27w : \iota.\lambda V0x \in (ty\_Ebin$

**Definition 28** We define  $c\_Ecombin\_Eo$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda A\_27c : \iota.\lambda V0f \in (A\_27b^{A\_27c}).\lambda V1$

Let  $ty\_Eone\_Eone : \iota$  be given. Assume the following.

$$nonempty\ ty\_Eone\_Eone \quad (20)$$

Let  $ty\_Efc\_Ebit0 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty\_Efc\_Ebit0\ A0) \quad (21)$$

Let  $ty\_Efc\_Ebit1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty\_Efc\_Ebit1\ A0) \quad (22)$$

Let  $c\_Ebool\_EARB : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_Ebool\_EARB\ A\_27a \in A\_27a \quad (23)$$

**Definition 29** We define  $c\_Ebool\_ECOND$  to be  $\lambda A\_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A\_27a.(\lambda V2t2 \in A\_27a.$

**Definition 30** We define  $c\_Earithmic\_EMIN$  to be  $\lambda V0m \in ty\_Eenum\_Eenum.\lambda V1n \in ty\_Eenum\_Eenum$

**Definition 31** We define  $c\_Ebool\_E\_5C\_2F$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c\_Ebool\_E\_21\ 2)\ (\lambda V2t \in$

**Definition 32** We define  $c\_Earithmic\_E\_3C\_3D$  to be  $\lambda V0m \in ty\_Eenum\_Eenum.\lambda V1n \in ty\_Eenum\_Eenum$

**Definition 33** We define  $c\_Ewords\_Eword\_bits$  to be  $\lambda A\_27a : \iota.\lambda V0h \in ty\_Eenum\_Eenum.\lambda V1l \in ty\_Eenum\_Eenum$

**Definition 34** We define  $c\_Ebit\_ESBIT$  to be  $\lambda V0b \in 2.\lambda V1n \in ty\_Eenum\_Eenum.(ap\ (ap\ (ap\ (c\_Ebool$

Let  $c\_Esum\_num\_ESUM : \iota$  be given. Assume the following.

$$c\_Esum\_num\_ESUM \in ((ty\_Eenum\_Eenum^{(ty\_Eenum\_Eenum^{ty\_Eenum\_Eenum})})^{ty\_Eenum\_Eenum}) \quad (24)$$

**Definition 35** We define  $c\_Ewords\_Ew2n$  to be  $\lambda A\_27a : \iota.\lambda V0w \in (ty\_Efc\_Ecart\ 2\ A\_27a).(ap\ (ap\ c$

**Definition 36** We define  $c\_Ewords\_Ew2w$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0w \in (ty\_Efc\_Ecart\ 2\ A\_27a$

**Definition 37** We define  $c\_Ewords\_Eword\_extract$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0h \in ty\_Eenum\_Eenum$

**Definition 38** We define  $c\_Ecombin\_EK$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.(\lambda V0x \in A\_27a.(\lambda V1y \in A\_27b.V0x)$

Let  $c\_Ebinary\_ieee\_Efloat\_Significand\_fupd : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27u.nonempty\ A\_27u \Rightarrow \forall A\_27v. \\ & nonempty\ A\_27w \Rightarrow c\_Ebinary\_ieee\_Efloat\_Significand\_fupd\ A\_27t\ A\_27u\ A\_27v \in \\ & ((ty\_Ebinary\_ieee\_Efloat\ A\_27t\ A\_27w)^{(ty\_Ebinary\_ieee\_Efloat\ A\_27t\ A\_27w)})^{(ty\_Ebinary\_ieee\_Efloat\ A\_27t\ A\_27w)} \end{aligned} \quad (25)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow \forall A\_27x. \\ & nonempty\ A\_27x \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Exponent\_fupd\ A\_27t \\ & A\_27w\ A\_27x \in (((ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27x)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)})^{(ty\_2Efloat\_Exponent\_fupd\ A\_27t\ A\_27w)}) \\ & \end{aligned} \quad (26)$$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Sign\_fupd : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Sign\_fupd\ A\_27t \\ & A\_27w \in (((ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)})^{(ty\_2Efloat\_Sign\_fupd\ A\_27t\ A\_27w)}) \\ & \end{aligned} \quad (27)$$

**Definition 39** We define  $c\_2Emachine\_ieee\_2Efp64\_to\_float$  to be  $\lambda V0w \in (ty\_2Efloat\_Exponent\_fupd\ 2\ (ty\_2Efloat\_Sign\_fupd\ 2\ w))$

**Definition 40** We define  $c\_2Emachine\_ieee\_2Efp64\_isNormal$  to be  $(ap\ (ap\ (c\_2Efloat\_Exponent\_fupd\ 2\ w)))\ w$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Significand : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Significand\ A\_27t \\ & A\_27w \in ((ty\_2Efloat\_Exponent\_fupd\ 2\ A\_27t)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)}) \\ & \end{aligned} \quad (28)$$

Let  $ty\_2Esum\_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty\_2Esum\_2Esum\ A0\ A1) \\ & \end{aligned} \quad (29)$$

**Definition 41** We define  $c\_2Ewords\_2Eword\_lsl$  to be  $\lambda A\_27a : \iota.\lambda V0w \in (ty\_2Efloat\_Exponent\_fupd\ 2\ A\_27a).\lambda V1x \in (ty\_2Efloat\_Significand\ A\_27a\ x).w\ lsl\ x$

**Definition 42** We define  $c\_2Ewords\_2Eword\_or$  to be  $\lambda A\_27a : \iota.\lambda V0v \in (ty\_2Efloat\_Exponent\_fupd\ 2\ A\_27a).\lambda V1x \in (ty\_2Efloat\_Significand\ A\_27a\ x).w\ or\ x$

**Definition 43** We define  $c\_2Ebool\_2ELET$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.(\lambda V0f \in (A\_27b^{A\_27a}).(\lambda V1x \in A\_27b).f\ x)$

**Definition 44** We define  $c\_2Ewords\_2Eword\_join$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0v \in (ty\_2Efloat\_Exponent\_fupd\ 2\ A\_27a).\lambda V1x \in (ty\_2Efloat\_Significand\ A\_27a\ x).w\ join\ x$

**Definition 45** We define  $c\_2Ewords\_2Eword\_concat$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda A\_27c : \iota.\lambda V0v \in (ty\_2Efloat\_Exponent\_fupd\ 2\ A\_27a).\lambda V1x \in (ty\_2Efloat\_Significand\ A\_27a\ x).w\ concat\ x$

Let  $c\_2Ebinary\_ieee\_2Efloat\_Sign : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27t.nonempty\ A\_27t \Rightarrow \forall A\_27w.nonempty\ A\_27w \Rightarrow c\_2Ebinary\_ieee\_2Efloat\_Sign\ A\_27t \\ & A\_27w \in ((ty\_2Efloat\_Exponent\_fupd\ 2\ ty\_2Eone\_2Eone)^{(ty\_2Ebinary\_ieee\_2Efloat\ A\_27t\ A\_27w)}) \\ & \end{aligned} \quad (30)$$

**Definition 46** We define  $c\_2Emachine\_ieee\_2Efloat\_to\_fp64$  to be  $\lambda V0x \in (ty\_2Ebinary\_ieee\_2Efloat\ (ty\_2Efloat\_Exponent\_fupd\ 2\ (ty\_2Efloat\_Sign\_fupd\ 2\ w)))\ x$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow \forall A.27c. \\
& nonempty\ A.27c \Rightarrow (\forall V0f \in (A.27b^{A.27a}).(\forall V1g \in (A.27a^{A.27c}). \\
& (\forall V2x \in A.27c.((ap\ (ap\ (ap\ (c.2Ecombin\_2Eo\ A.27c\ A.27b\ A.27a) \\
& V0f)\ V1g)\ V2x) = (ap\ V0f\ (ap\ V1g\ V2x))))))
\end{aligned} \tag{31}$$

Assume the following.

$$\begin{aligned}
& (\forall V0x \in (ty\_2Ebinary\_ieee\_2Efloat\ (ty\_2Efc\_2Ebit0\ ( \\
& ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1 \\
& ty\_2Eone\_2Eone))))))\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0 \\
& ty\_2Eone\_2Eone))))).((ap\ c.2Emachine\_ieee\_2Efp64\_to\_float \\
& (ap\ c.2Emachine\_ieee\_2Efloat\_to\_fp64\ V0x)) = V0x))
\end{aligned} \tag{32}$$

**Theorem 1**

$$\begin{aligned}
& ((\forall V0a \in (ty\_2Ebinary\_ieee\_2Efloat\ (ty\_2Efc\_2Ebit0 \\
& (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1 \\
& ty\_2Eone\_2Eone))))))\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0 \\
& ty\_2Eone\_2Eone))))).((p\ (ap\ c.2Emachine\_ieee\_2Efp64\_isNormal \\
& (ap\ c.2Emachine\_ieee\_2Efloat\_to\_fp64\ V0a))) \Leftrightarrow (p\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_is\_normal \\
& (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0 \\
& (ty\_2Efc\_2Ebit1\ ty\_2Eone\_2Eone))))))\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit1 \\
& (ty\_2Efc\_2Ebit0\ ty\_2Eone\_2Eone))))\ V0a)))) \wedge (\forall V1a \in ty\_2Enum\_2Enum. \\
& ((p\ (ap\ c.2Emachine\_ieee\_2Efp64\_isNormal\ (ap\ (c.2Ewords\_2En2w \\
& (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0 \\
& (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0\ ty\_2Eone\_2Eone))))))\ V1a))) \Leftrightarrow \\
& (p\ (ap\ (c.2Ebinary\_ieee\_2Efloat\_is\_normal\ (ty\_2Efc\_2Ebit0 \\
& (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit1 \\
& ty\_2Eone\_2Eone))))))\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit1\ (ty\_2Efc\_2Ebit0 \\
& ty\_2Eone\_2Eone))))))\ (ap\ c.2Emachine\_ieee\_2Efp64\_to\_float \\
& (ap\ (c.2Ewords\_2En2w\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0 \\
& (ty\_2Efc\_2Ebit0\ (ty\_2Efc\_2Ebit0\ ty\_2Eone\_2Eone))))))\ V1a))))))
\end{aligned}$$