

thm_2Emarker_2Emove__left__disj
(TMLbB2G5EKWUREwXxMXpwZ1MF93o7qch5Hk)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Ebool_2E_2ET$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c_2Emin_2E_3D (2^{A-27a}))$

Definition 4 We define $c_2Ebool_2E_2EF$ to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t))$

Definition 7 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t))$

Definition 8 We define $c_2Emarker_2Estmarker$ to be $\lambda A.\lambda 27a : \iota.\lambda V0x \in A.27a.V0x$.

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow \\ & (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0x \in A.27a.((V0x = V0x) \Leftrightarrow True)) \quad (2)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p V0A) \vee (\\ & (p V1B) \vee (p V2C))) \Leftrightarrow (((p V0A) \vee (p V1B)) \vee (p V2C)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2.(\forall V1B \in 2.(((p V0A) \vee (p V1B)) \Leftrightarrow ((p V1B) \vee \\ & (p V0A)))) \end{aligned} \quad (4)$$

Theorem 1

$$\begin{aligned} & (\forall V_0 p \in 2. (\forall V_1 q \in 2. (\forall V_2 m \in 2. (((p \vee V_0 p) \vee \\ & (p \text{ (ap (c_2Emarker_2Estmarker 2) V_2 m))) \Leftrightarrow ((p \text{ (ap (c_2Emarker_2Estmarker} \\ & 2) V_2 m)) \vee (p \vee V_0 p))) \wedge (((p \text{ (ap (c_2Emarker_2Estmarker 2) V_2 m)) \vee} \\ & (p \vee V_0 p)) \vee (p \vee V_1 q))) \Leftrightarrow ((p \text{ (ap (c_2Emarker_2Estmarker 2) V_2 m)) \vee ((} \\ & p \vee V_0 p) \vee (p \vee V_1 q))) \wedge ((p \vee V_0 p) \vee ((p \text{ (ap (c_2Emarker_2Estmarker 2) } \\ & V_2 m)) \vee (p \vee V_1 q))) \Leftrightarrow ((p \text{ (ap (c_2Emarker_2Estmarker 2) V_2 m)) \vee ((p} \\ & \vee V_0 p) \vee (p \vee V_1 q)))))) \end{aligned}$$