

thm\_2Emeasure\_2ECARATHEODORY  
(TMYcWVqtpFCkvMCn-  
nUUW2fwCAumDABJWW2t)

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**Definition 1** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 2** We define  $c\_2Ebool\_2E\_2T$  to be  $(ap (ap (c\_2Emin\_2E\_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

**Definition 3** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x))$  then (the  $(\lambda x.x \in A \wedge p x)$  of type  $\iota \Rightarrow \iota$ ).

**Definition 4** We define  $c\_2Ebool\_2E\_3F$  to be  $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap V0P (ap (c\_2Emin\_2E\_40 A P))))$

**Definition 5** We define  $c\_2Ecombin\_2E\_2EK$  to be  $\lambda A.\lambda 27a : \iota.\lambda A.\lambda 27b : \iota.(\lambda V0x \in A.\lambda V1y \in A.\lambda V2z \in A.(ap V0x (ap V1y (ap V2z (c\_2Emin\_2E\_40 A P))))))$

**Definition 6** We define  $c\_2Ecombin\_2E\_2ES$  to be  $\lambda A.\lambda 27a : \iota.\lambda A.\lambda 27b : \iota.\lambda A.\lambda 27c : \iota.(\lambda V0f \in ((A.\lambda 27c^{A-27b})^{A-27a}))$

**Definition 7** We define  $c\_2Ecombin\_2E\_2EI$  to be  $\lambda A.\lambda 27a : \iota.(ap (ap (c\_2Ecombin\_2E\_2ES A 27a (A.\lambda 27a^{A-27a})) A 27a))$

**Definition 8** We define  $c\_2Ebool\_2E\_2IN$  to be  $\lambda A.\lambda 27a : \iota.(\lambda V0x \in A.\lambda V1f \in (2^{A-27a}).(ap V1f V0x))$

**Definition 9** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p \Rightarrow q)$  of type  $\iota$ .

**Definition 10** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c\_2Emin\_2E\_3D (2^{A-27a})) P P))))$

**Definition 11** We define  $c\_2Ebool\_2E\_5C\_2F$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in 2.V2t))))$

**Definition 12** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in 2.V2t))))$

Let  $ty\_2Epair\_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty\_2Epair\_2Eprod A0 A1) \tag{1}$$

Let  $c\_2Epair\_2EABS\_prod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.\lambda 27a.nonempty A.\lambda 27b.nonempty A.\lambda 27c \Rightarrow c\_2Epair\_2EABS\_prod A.\lambda 27a A.\lambda 27b \in ((ty\_2Epair\_2Eprod A.\lambda 27a A.\lambda 27b)^{(2^{A-27b})^{A-27a}}) \tag{2}$$

**Definition 13** We define  $c\_2Epair\_2E\_2C$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0x \in A\_27a. \lambda V1y \in A\_27b. (ap (c\_2Epred\_set\_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota)$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epred\_set\_2EGSPEC\ A\_27a\ A\_27b \in ((2^{A\_27a})^{(ty\_2Epair\_2Eprod\ A\_27a\ 2)^{A\_27b}})$$
(3)

**Definition 14** We define  $c\_2Epred\_set\_2EUNION$  to be  $\lambda A\_27a : \iota. \lambda V0s \in (2^{A\_27a}). \lambda V1t \in (2^{A\_27a}). (ap (c\_2Ebool\_2EF$

**Definition 15** We define  $c\_2Ebool\_2EF$  to be  $(ap (c\_2Ebool\_2E\_21\ 2) (\lambda V0t \in 2.V0t))$ .

**Definition 16** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2. (ap (ap\ c\_2Emin\_2E\_3D\_3D\_3E\ V0t)\ c\_2Ebool\_2E\_7E$

**Definition 17** We define  $c\_2Epred\_set\_2EDIFF$  to be  $\lambda A\_27a : \iota. \lambda V0s \in (2^{A\_27a}). \lambda V1t \in (2^{A\_27a}). (ap (c\_2Ebool\_2E\_7E$

**Definition 18** We define  $c\_2Epred\_set\_2EEMPTY$  to be  $\lambda A\_27a : \iota. (\lambda V0x \in A\_27a. c\_2Ebool\_2EF)$ .

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Enum\_2Enum$$
(4)

**Definition 19** We define  $c\_2Epred\_set\_2EUNIV$  to be  $\lambda A\_27a : \iota. (\lambda V0x \in A\_27a. c\_2Ebool\_2ET)$ .

**Definition 20** We define  $c\_2Epred\_set\_2EIMAGE$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (A\_27b^{A\_27a}). \lambda V1s \in (A\_27b^{A\_27a})$

**Definition 21** We define  $c\_2Epred\_set\_2EBIGUNION$  to be  $\lambda A\_27a : \iota. \lambda V0P \in (2^{(2^{A\_27a})}). (ap (c\_2Epred\_set\_2EIMAGE$

Let  $ty\_2Erealx\_2Ereal : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Erealx\_2Ereal$$
(5)

Let  $c\_2Emeasure\_2Emeasure : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Emeasure\ A\_27a \in ((ty\_2Erealx\_2Ereal^{(2^{A\_27a})})^{(ty\_2Epair\_2Eprod\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealx\_2Ereal^{(2^{A\_27a})})$$
(6)

**Definition 22** We define  $c\_2Ecombin\_2Eo$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda A\_27c : \iota. \lambda V0f \in (A\_27b^{A\_27c}). \lambda V1g \in (A\_27c^{A\_27a})$

Let  $c\_2Enum\_2EZERO\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2EZERO\_REP \in \omega$$
(7)

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{\omega})$$
(8)

**Definition 23** We define  $c\_2Enum\_2E0$  to be  $(ap\ c\_2Enum\_2EABS\_num\ c\_2Enum\_2EZERO\_REP)$ .

Let  $c\_2Ereal\_2Esum : \iota$  be given. Assume the following.

$$c\_2Ereal\_2Esum \in ((ty\_2Erealax\_2Ereal^{(ty\_2Erealax\_2Ereal^{ty\_2Enum\_2Enum})})^{(ty\_2Epair\_2Eprod\ ty\_2Enum\_2Enum)}) \quad (9)$$

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \quad (10)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega}) \quad (11)$$

**Definition 24** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.(ap\ c\_2Enum\_2EABS\_num$

**Definition 25** We define  $c\_2Eprim\_rec\_2E\_3C$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

**Definition 26** We define  $c\_2Earithmetic\_2E\_3E$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

**Definition 27** We define  $c\_2Earithmetic\_2E\_3E\_3D$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

Let  $ty\_2Ehreal\_2Ehreal : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Ehreal\_2Ehreal \quad (12)$$

Let  $c\_2Erealax\_2Ereal\_REP\_CLASS : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Ereal\_REP\_CLASS \in ((2^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)})^{ty\_2Erealax}) \quad (13)$$

**Definition 28** We define  $c\_2Erealax\_2Ereal\_REP$  to be  $\lambda V0a \in ty\_2Erealax\_2Ereal.(ap\ (c\_2Emin\_2E\_40\ ($

Let  $c\_2Erealax\_2Etrealm\_neg : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Etrealm\_neg \in ((ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)^{ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal}) \quad (14)$$

Let  $c\_2Erealax\_2Etrealm\_eq : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Etrealm\_eq \in ((2^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)})^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal)}) \quad (15)$$

Let  $c\_2Erealax\_2Ereal\_ABS\_CLASS : \iota$  be given. Assume the following.

$$c\_2Erealax\_2Ereal\_ABS\_CLASS \in (ty\_2Erealax\_2Ereal^{(2^{(ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)})}) \quad (16)$$

**Definition 29** We define  $c\_2Erealax\_2Ereal\_ABS$  to be  $\lambda V0r \in (ty\_2Epair\_2Eprod\ ty\_2Ehreal\_2Ehreal\ ty\_2Ehreal\_2Ehreal)$

**Definition 30** We define  $c\_2Erealax\_2Ereal\_neg$  to be  $\lambda V0T1 \in ty\_2Erealax\_2Ereal.(ap\ c\_2Erealax\_2Ereal$



Let  $c\_2Emetric\_2Edist : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emetric\_2Edist\ A\_27a \in ((ty\_2Erealax\_2Ereal^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)})) \quad (24)$$

Let  $ty\_2Etopology\_2Etopology : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty\_2Etopology\_2Etopology\ A0) \quad (25)$$

Let  $c\_2Etopology\_2Etopology : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Etopology\_2Etopology\ A\_27a \in ((ty\_2Etopology\_2Etopology\ A\_27a)^{(2^{(2^A-27a)})}) \quad (26)$$

**Definition 39** We define  $c\_2Emetric\_2Emtop$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Emetric\_2Emetric\ A\_27a).(ap$

Let  $c\_2Enets\_2Etends : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Enets\_2Etends\ A\_27a\ A\_27b \in (((2^{(ty\_2Epair\_2Eprod\ (ty\_2Etopology\_2Etopology\ A\_27a)\ (2^{A-27b})^{A-27b})}))^{A\_27a})^{(A\_27a^{A-27b})}) \quad (27)$$

**Definition 40** We define  $c\_2Eseq\_2E\_2D\_2D\_3E$  to be  $\lambda V0x \in (ty\_2Erealax\_2Ereal^{ty\_2Enum\_2Enum}).\lambda V1x$

**Definition 41** We define  $c\_2Eseq\_2Esums$  to be  $\lambda V0f \in (ty\_2Erealax\_2Ereal^{ty\_2Enum\_2Enum}).\lambda V1s \in ty\_2$

Let  $c\_2Emeasure\_2Emeasurable\_sets : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Emeasurable\_sets\ A\_27a \in (((2^{(2^A-27a)})^{(ty\_2Epair\_2Eprod\ (2^A-27a)\ (ty\_2Epair\_2Eprod\ (2^{(2^A-27a)})\ (ty\_2Erealax\_2Ereal^{(2^A-27a)}))})) \quad (28)$$

**Definition 42** We define  $c\_2Epred\_set\_2EINTER$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^A-27a).\lambda V1t \in (2^A-27a).(ap$

**Definition 43** We define  $c\_2Epred\_set\_2EDISJOINT$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^A-27a).\lambda V1t \in (2^A-27a).(ap$

**Definition 44** We define  $c\_2Epred\_set\_2EFUNSET$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0P \in (2^A-27a).\lambda V1Q \in ($

**Definition 45** We define  $c\_2Emeasure\_2Ecountably\_additive$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod$

**Definition 46** We define  $c\_2Emeasure\_2Epositive$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod\ (2^A-27a)\ (ty$

Let  $c\_2Emeasure\_2Em\_space : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Em\_space\ A\_27a \in (((2^A-27a)^{(ty\_2Epair\_2Eprod\ (2^A-27a)\ (ty\_2Epair\_2Eprod\ (2^{(2^A-27a)})\ (ty\_2Erealax\_2Ereal^{(2^A-27a)}))})) \quad (29)$$

Let  $c\_2Emeasure\_2Esubsets : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Emeasure\_2Esubsets\ A\_27a \in ((2^{(2^A-27a)})^{(ty\_2Epair\_2Eprod\ (2^A-27a)\ (2^{(2^A-27a)})})) \quad (30)$$

**Definition 47** We define  $c\_2Epred\_set\_2ESUBSET$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).\lambda V1t \in (2^{A\_27a}).(ap$

**Definition 48** We define  $c\_2Epred\_set\_2EINJ$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0f \in (A\_27b^{A\_27a}).\lambda V1s \in (2^{A\_27a})$

**Definition 49** We define  $c\_2Epred\_set\_2Ecountable$  to be  $\lambda A\_27a : \iota.\lambda V0s \in (2^{A\_27a}).(ap (c\_2Ebool\_2E3F$

Let  $c\_2Emeasure\_2Espace : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow c\_2Emeasure\_2Espace A\_27a \in ((2^{A\_27a})^{(ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))}) \quad (31)$$

**Definition 50** We define  $c\_2Emeasure\_2Esubset\_class$  to be  $\lambda A\_27a : \iota.\lambda V0sp \in (2^{A\_27a}).\lambda V1sts \in (2^{(2^{A\_27a})})$

**Definition 51** We define  $c\_2Emeasure\_2Ealgebra$  to be  $\lambda A\_27a : \iota.\lambda V0a \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 52** We define  $c\_2Emeasure\_2Esigma\_algebra$  to be  $\lambda A\_27a : \iota.\lambda V0a \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 53** We define  $c\_2Emeasure\_2Emeasure\_space$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 54** We define  $c\_2Eseq\_2Esuminf$  to be  $\lambda V0f \in (ty\_2Erealax\_2Ereal^{ty\_2Eenum\_2Eenum}).(ap (c\_2E$

**Definition 55** We define  $c\_2Eseq\_2Esummable$  to be  $\lambda V0f \in (ty\_2Erealax\_2Ereal^{ty\_2Eenum\_2Eenum}).(ap (c\_2E$

**Definition 56** We define  $c\_2Emeasure\_2Ecountably\_subadditive$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 57** We define  $c\_2Emeasure\_2Eincreasing$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 58** We define  $c\_2Emeasure\_2Eouter\_measure\_space$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 59** We define  $c\_2Epred\_set\_2EBIGINTER$  to be  $\lambda A\_27a : \iota.\lambda V0P \in (2^{(2^{A\_27a})}).(ap (c\_2Epred\_set\_2E$

**Definition 60** We define  $c\_2Emeasure\_2Esigma$  to be  $\lambda A\_27a : \iota.\lambda V0sp \in (2^{A\_27a}).\lambda V1st \in (2^{(2^{A\_27a})}).(ap$

**Definition 61** We define  $c\_2Ereal\_2Esup$  to be  $\lambda V0P \in (2^{ty\_2Erealax\_2Ereal}).(ap (c\_2Emin\_2E40 ty\_2Ereal$

**Definition 62** We define  $c\_2Ereal\_2Einf$  to be  $\lambda V0p \in (2^{ty\_2Erealax\_2Ereal}).(ap c\_2Erealax\_2Ereal\_neg (ap$

**Definition 63** We define  $c\_2Emeasure\_2Einf\_measure$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 64** We define  $c\_2Epred\_set\_2EPOW$  to be  $\lambda A\_27a : \iota.\lambda V0set \in (2^{A\_27a}).(ap (c\_2Epred\_set\_2E$

**Definition 65** We define  $c\_2Emeasure\_2Elambda\_system$  to be  $\lambda A\_27a : \iota.\lambda V0gen \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

**Definition 66** We define  $c\_2Emeasure\_2Eadditive$  to be  $\lambda A\_27a : \iota.\lambda V0m \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (2^{(2^{A\_27a})}))$

Assume the following.

$$True \quad (32)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. ((p V0t1) \Rightarrow (p V1t2)) \Rightarrow ((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))) \quad (33)$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \quad (34)$$

Assume the following.

$$(\forall V0t \in 2. ((p V0t) \vee \neg(p V0t))) \quad (35)$$

Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A\_27a. (p V0t)) \Leftrightarrow (p V0t))) \quad (36)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. ((p V0t1) \wedge (p V1t2)) \Leftrightarrow ((p V1t2) \wedge (p V0t1)))) \quad (37)$$

Assume the following.

$$(\forall V0t \in 2. (((p V0t) \Rightarrow False) \Rightarrow \neg(p V0t))) \quad (38)$$

Assume the following.

$$(\forall V0t \in 2. (\neg(p V0t) \Rightarrow ((p V0t) \Rightarrow False))) \quad (39)$$

Assume the following.

$$(\forall V0t \in 2. (((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))) \quad (40)$$

Assume the following.

$$(\forall V0t \in 2. (((True \vee (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \vee True) \Leftrightarrow True) \wedge (((False \vee (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee False) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee (p V0t)) \Leftrightarrow (p V0t)))) \quad (41)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow \neg(p V0t)))) \quad (42)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (43)$$

Assume the following.

$$\forall A.27a.nonempty \ A.27a \Rightarrow (\forall V0x \in A.27a.((V0x = V0x) \Leftrightarrow True)) \quad (44)$$

Assume the following.

$$\forall A.27a.nonempty \ A.27a \Rightarrow (\forall V0x \in A.27a.(\forall V1y \in A.27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (45)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))) \quad (46)$$

Assume the following.

$$\forall A.27a.nonempty \ A.27a \Rightarrow (\forall V0P \in (2^{A.27a}).((\neg(\forall V1x \in A.27a.(p \ (ap \ V0P \ V1x)))) \Leftrightarrow (\exists V2x \in A.27a.(\neg(p \ (ap \ V0P \ V2x))))) \quad (47)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p \ V0A) \vee (p \ V1B) \vee (p \ V2C)) \Leftrightarrow (((p \ V0A) \vee (p \ V1B)) \vee (p \ V2C))))) \quad (48)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((p \ V0A) \vee (p \ V1B)) \Leftrightarrow ((p \ V1B) \vee (p \ V0A)))) \quad (49)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p \ V0A) \wedge (p \ V1B))) \Leftrightarrow ((\neg(p \ V0A) \vee \neg(p \ V1B)))) \wedge (((\neg(p \ V0A) \vee (p \ V1B)) \Leftrightarrow ((\neg(p \ V0A) \wedge \neg(p \ V1B))))) \quad (50)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p \ V0t1) \Rightarrow ((p \ V1t2) \Rightarrow (p \ V2t3))) \Leftrightarrow (((p \ V0t1) \wedge (p \ V1t2)) \Rightarrow (p \ V2t3)))) \quad (51)$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1x.27 \in 2.(\forall V2y \in 2.(\forall V3y.27 \in 2.(((p \ V0x) \Leftrightarrow (p \ V1x.27)) \wedge ((p \ V1x.27) \Rightarrow ((p \ V2y) \Leftrightarrow (p \ V3y.27)))) \Rightarrow (((p \ V0x) \Rightarrow (p \ V2y)) \Leftrightarrow ((p \ V1x.27) \Rightarrow (p \ V3y.27))))) \quad (52)$$



Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. ((ap\ (c\_2Ecombin\_2EI\ A\_27a)\ V0x) = V0x)) \quad (53)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in (2^{A\_27a}). (\forall V1y \in (2^{(2^{A\_27a})}). ((ap\ (c\_2Emeasure\_2Espace\ A\_27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A\_27a})\ (2^{(2^{A\_27a})}))\ V0x)\ V1y)) = V0x))) \quad (54)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in (2^{A\_27a}). (\forall V1y \in (2^{(2^{A\_27a})}). ((ap\ (c\_2Emeasure\_2Esubsets\ A\_27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A\_27a})\ (2^{(2^{A\_27a})}))\ V0x)\ V1y)) = V1y))) \quad (55)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0sp \in (2^{A\_27a}). (\forall V1sts \in (2^{(2^{A\_27a})}). (\forall V2mu \in (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}). ((ap\ (c\_2Emeasure\_2Em\_space\ A\_27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))))\ V0sp)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))\ V1sts)\ V2mu))) = V0sp)))) \quad (56)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0sp \in (2^{A\_27a}). (\forall V1sts \in (2^{(2^{A\_27a})}). (\forall V2mu \in (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}). ((ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A\_27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))))\ V0sp)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))\ V1sts)\ V2mu))) = V1sts)))) \quad (57)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0sp \in (2^{A\_27a}). (\forall V1sts \in (2^{(2^{A\_27a})}). (\forall V2mu \in (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}). ((ap\ (c\_2Emeasure\_2Emeasure\ A\_27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A\_27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))))\ V0sp)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{(2^{A\_27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A\_27a})}))\ V1sts)\ V2mu))) = V2mu)))) \quad (58)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0a \in (ty\_2Epair\_2Eprod \\ (2^{A.27a})\ (2^{(2^{A.27a})}))).((ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A.27a}) \\ (2^{(2^{A.27a})})))\ (ap\ (c\_2Emeasure\_2Espace\ A.27a)\ V0a))\ (ap\ (c\_2Emeasure\_2Esubsets \\ A.27a)\ V0a)) = V0a) \end{aligned} \quad (59)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0gsig \in (ty\_2Epair\_2Eprod \\ (2^{A.27a})\ (2^{(2^{A.27a})}))).(\forall V1lam \in (ty\_2Erealax\_2Ereal^{(2^{A.27a})})). \\ (((p\ (ap\ (c\_2Emeasure\_2Esigma\_algebra\ A.27a)\ V0gsig)) \wedge (p\ (ap \\ (c\_2Emeasure\_2Eouter\_measure\_space\ A.27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C \\ (2^{A.27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A.27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A.27a})})))) \\ (ap\ (c\_2Emeasure\_2Espace\ A.27a)\ V0gsig))\ (ap\ (ap\ (c\_2Epair\_2E\_2C \\ (2^{(2^{A.27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A.27a})})))\ (ap\ (c\_2Emeasure\_2Esubsets \\ A.27a)\ V0gsig))\ V1lam)))) \Rightarrow (p\ (ap\ (c\_2Emeasure\_2Emeasure\_space \\ A.27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{A.27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A.27a})}) \\ (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))))\ (ap\ (c\_2Emeasure\_2Espace\ A.27a) \\ V0gsig))\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ (2^{(2^{A.27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))) \\ (ap\ (ap\ (c\_2Emeasure\_2Elambda\_system\ A.27a)\ V0gsig)\ V1lam)) \\ V1lam)))))) \end{aligned} \quad (60)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\ (2^{A.27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A.27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))). \\ (((p\ (ap\ (c\_2Emeasure\_2Ealgebra\ A.27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C \\ (2^{A.27a})\ (2^{(2^{A.27a})})))\ (ap\ (c\_2Emeasure\_2Em\_space\ A.27a) \\ V0m))\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m)))) \wedge (( \\ p\ (ap\ (c\_2Emeasure\_2Epositive\ A.27a)\ V0m)) \wedge (p\ (ap\ (c\_2Emeasure\_2Eadditive \\ A.27a)\ V0m)))) \Rightarrow (p\ (ap\ (c\_2Emeasure\_2Eincreasing\ A.27a)\ V0m)))) \end{aligned} \quad (61)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\ (2^{A.27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A.27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))). \\ (((p\ (ap\ (c\_2Emeasure\_2Ealgebra\ A.27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C \\ (2^{A.27a})\ (2^{(2^{A.27a})})))\ (ap\ (c\_2Emeasure\_2Em\_space\ A.27a) \\ V0m))\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m)))) \wedge (( \\ p\ (ap\ (c\_2Emeasure\_2Epositive\ A.27a)\ V0m)) \wedge (p\ (ap\ (c\_2Emeasure\_2Ecountably\_additive \\ A.27a)\ V0m)))) \Rightarrow (p\ (ap\ (c\_2Emeasure\_2Eadditive\ A.27a)\ V0m)))) \end{aligned} \quad (62)$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A\_27a}) (ty\_2Epair\_2Eprod (2^{(2^{A\_27a})}) (ty\_2Erealax\_2Ereal(2^{A\_27a}))))). \\
& (\forall V1s \in (2^{A\_27a}).((p (ap (c\_2Emeasure\_2Ealgebra\ A\_27a) \\
& (ap (ap (c\_2Epair\_2E\_2C (2^{A\_27a}) (2^{(2^{A\_27a})})) (ap (c\_2Emeasure\_2Em\_space \\
& A\_27a) V0m)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A\_27a) V0m)))))) \wedge \\
& ((p (ap (c\_2Emeasure\_2Epositive\ A\_27a) V0m)) \wedge ((p (ap (c\_2Emeasure\_2Ecountably\_additive \\
& A\_27a) V0m)) \wedge (p (ap (ap (c\_2Ebool\_2EIN (2^{A\_27a}) V1s) (ap (c\_2Emeasure\_2Emeasurable\_sets \\
& A\_27a) V0m)))))) \Rightarrow ((ap (ap (c\_2Emeasure\_2Einf\_measure\ A\_27a) \\
& V0m) V1s) = (ap (ap (c\_2Emeasure\_2Emeasure\ A\_27a) V0m) V1s)))))) \\
& (63)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0m0 \in (ty\_2Epair\_2Eprod \\
& (2^{A\_27a}) (ty\_2Epair\_2Eprod (2^{(2^{A\_27a})}) (ty\_2Erealax\_2Ereal(2^{A\_27a}))))). \\
& (\forall V1m1 \in (ty\_2Epair\_2Eprod (2^{A\_27a}) (ty\_2Epair\_2Eprod \\
& (2^{(2^{A\_27a})}) (ty\_2Erealax\_2Ereal(2^{(2^{A\_27a})}))))).((p (ap (c\_2Emeasure\_2Esigma\_algebra \\
& A\_27a) (ap (ap (c\_2Epair\_2E\_2C (2^{A\_27a}) (2^{(2^{A\_27a})})) (ap (c\_2Emeasure\_2Em\_space \\
& A\_27a) V0m0)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A\_27a) V0m0)))))) \wedge \\
& ((p (ap (ap (c\_2Epred\_set\_2ESUBSET (2^{A\_27a}) (ap (c\_2Emeasure\_2Emeasurable\_sets \\
& A\_27a) V0m0)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A\_27a) V1m1)))))) \wedge \\
& (((ap (c\_2Emeasure\_2Emeasure\ A\_27a) V0m0) = (ap (c\_2Emeasure\_2Emeasure \\
& A\_27a) V1m1)) \wedge (p (ap (c\_2Emeasure\_2Emeasure\_space\ A\_27a) V1m1)))))) \Rightarrow \\
& (p (ap (c\_2Emeasure\_2Emeasure\_space\ A\_27a) V0m0)))))) \\
& (64)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0sp \in (2^{A\_27a}).(\forall V1sts \in \\
& (2^{(2^{A\_27a})}).((p (ap (ap (c\_2Emeasure\_2Esubset\_class\ A\_27a) \\
& V0sp) V1sts)) \Rightarrow (p (ap (c\_2Emeasure\_2Esigma\_algebra\ A\_27a) (ap \\
& (ap (c\_2Emeasure\_2Esigma\ A\_27a) V0sp) V1sts)))))) \\
& (65)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0sp \in (2^{A\_27a}).(p (ap \\
& (c\_2Emeasure\_2Esigma\_algebra\ A\_27a) (ap (ap (c\_2Epair\_2E\_2C \\
& (2^{A\_27a}) (2^{(2^{A\_27a})})) V0sp) (ap (c\_2Epred\_set\_2EPOW\ A\_27a) \\
& V0sp)))))) \\
& (66)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A.27a}) (ty\_2Epair\_2Eprod (2^{(2^{A.27a})}) (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))))). \\
& (((p (ap (c\_2Emeasure\_2Ealgebra\ A.27a) (ap (ap (c\_2Epair\_2E\_2C \\
& (2^{A.27a}) (2^{(2^{A.27a})}))) (ap (c\_2Emeasure\_2Em\_space\ A.27a) \\
& V0m)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A.27a) V0m)))) \wedge (( \\
& p (ap (c\_2Emeasure\_2Epositive\ A.27a) V0m)) \wedge (p (ap (c\_2Emeasure\_2Eincreasing \\
& A.27a) V0m)))) \Rightarrow (p (ap (c\_2Emeasure\_2Eouter\_measure\_space \\
& A.27a) (ap (ap (c\_2Epair\_2E\_2C (2^{A.27a}) (ty\_2Epair\_2Eprod (2^{(2^{A.27a})}) \\
& (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))) (ap (c\_2Emeasure\_2Em\_space \\
& A.27a) V0m)) (ap (ap (c\_2Epair\_2E\_2C (2^{(2^{A.27a})}) (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))) \\
& (ap (c\_2Epred\_set\_2EPOW\ A.27a) (ap (c\_2Emeasure\_2Em\_space \\
& A.27a) V0m)))) (ap (c\_2Emeasure\_2Einf\_measure\ A.27a) V0m))))))
\end{aligned} \tag{67}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0a \in (2^{(2^{A.27a})}). (\forall V1b \in \\
& (ty\_2Epair\_2Eprod (2^{A.27a}) (2^{(2^{A.27a})}))). ((p (ap (c\_2Emeasure\_2Esigma\_algebra \\
& A.27a) V1b)) \wedge (p (ap (ap (c\_2Epred\_set\_2ESUBSET (2^{A.27a}) V0a) \\
& (ap (c\_2Emeasure\_2Esubsets\ A.27a) V1b)))) \Rightarrow (p (ap (ap (c\_2Epred\_set\_2ESUBSET \\
& (2^{A.27a}) (ap (c\_2Emeasure\_2Esubsets\ A.27a) (ap (ap (c\_2Emeasure\_2Esigma \\
& A.27a) (ap (c\_2Emeasure\_2Espace\ A.27a) V1b)) V0a))) (ap (c\_2Emeasure\_2Esubsets \\
& A.27a) V1b))))))
\end{aligned} \tag{68}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m \in (ty\_2Epair\_2Eprod \\
& (2^{A.27a}) (ty\_2Epair\_2Eprod (2^{(2^{A.27a})}) (ty\_2Erealax\_2Ereal^{(2^{A.27a})}))))). \\
& (((p (ap (c\_2Emeasure\_2Ealgebra\ A.27a) (ap (ap (c\_2Epair\_2E\_2C \\
& (2^{A.27a}) (2^{(2^{A.27a})}))) (ap (c\_2Emeasure\_2Em\_space\ A.27a) \\
& V0m)) (ap (c\_2Emeasure\_2Emeasurable\_sets\ A.27a) V0m)))) \wedge (( \\
& p (ap (c\_2Emeasure\_2Epositive\ A.27a) V0m)) \wedge ((p (ap (c\_2Emeasure\_2Eincreasing \\
& A.27a) V0m)) \wedge (p (ap (c\_2Emeasure\_2Eadditive\ A.27a) V0m)))) \Rightarrow \\
& (p (ap (ap (c\_2Epred\_set\_2ESUBSET (2^{A.27a}) (ap (c\_2Emeasure\_2Emeasurable\_sets \\
& A.27a) V0m)) (ap (ap (c\_2Emeasure\_2Elambda\_system\ A.27a) (ap \\
& (ap (c\_2Epair\_2E\_2C (2^{A.27a}) (2^{(2^{A.27a})}))) (ap (c\_2Emeasure\_2Em\_space \\
& A.27a) V0m)) (ap (c\_2Epred\_set\_2EPOW\ A.27a) (ap (c\_2Emeasure\_2Em\_space \\
& A.27a) V0m)))) (ap (c\_2Emeasure\_2Einf\_measure\ A.27a) V0m))))))
\end{aligned} \tag{69}$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \tag{70}$$

Assume the following.

$$(\forall V0A \in 2. ((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \tag{71}$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (((\neg((p V0A) \vee (p V1B))) \Rightarrow False) \Leftrightarrow ((p V0A) \Rightarrow False) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))) \quad (72)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (((\neg(\neg(p V0A)) \vee (p V1B))) \Rightarrow False) \Leftrightarrow ((p V0A) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))) \quad (73)$$

Assume the following.

$$(\forall V0A \in 2. (((\neg(p V0A)) \Rightarrow False) \Rightarrow (((p V0A) \Rightarrow False) \Rightarrow False))) \quad (74)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \Leftrightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee ((p V1q) \vee (p V2r))) \wedge (((p V0p) \vee (\neg(p V2r)) \vee (\neg(p V1q)))) \wedge (((p V1q) \vee (\neg(p V2r)) \vee (\neg(p V0p)))) \wedge ((p V2r) \vee ((\neg(p V1q)) \vee (\neg(p V0p)))))))))) \quad (75)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \wedge (p V2r)) \Leftrightarrow (((p V0p) \vee (\neg(p V1q)) \vee (\neg(p V2r))) \wedge (((p V1q) \vee (\neg(p V0p))) \wedge ((p V2r) \vee (\neg(p V0p)))))))) \quad (76)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \vee (p V2r)) \Leftrightarrow (((p V0p) \vee (\neg(p V1q))) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge ((p V1q) \vee ((p V2r) \vee (\neg(p V0p)))))))) \quad (77)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \Rightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge ((\neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p)))))))) \quad (78)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (((p V0p) \Leftrightarrow (\neg(p V1q))) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge ((\neg(p V1q)) \vee (\neg(p V0p)))))) \quad (79)$$

**Theorem 1**

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0m0 \in (ty\_2Epair\_2Eprod \\
& (2^{A-27a})\ (ty\_2Epair\_2Eprod\ (2^{(2^{A-27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A-27a})}))). \\
& (((p\ (ap\ (c\_2Emeasure\_2Ealgebra\ A.27a)\ (ap\ (ap\ (c\_2Epair\_2E\_2C \\
& (2^{A-27a})\ (2^{(2^{A-27a})})))\ (ap\ (c\_2Emeasure\_2Em\_space\ A.27a) \\
& V0m0))\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m0)))) \wedge \\
& ((p\ (ap\ (c\_2Emeasure\_2Epositive\ A.27a)\ V0m0)) \wedge (p\ (ap\ (c\_2Emeasure\_2Ecountably\_additive \\
& A.27a)\ V0m0)))) \Rightarrow (\exists V1m \in (ty\_2Epair\_2Eprod\ (2^{A-27a})\ (ty\_2Epair\_2Eprod \\
& (2^{(2^{A-27a})})\ (ty\_2Erealax\_2Ereal^{(2^{A-27a})}))). (\forall V2s \in \\
& (2^{A-27a}). ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (2^{A-27a})\ V2s)\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets \\
& A.27a)\ V0m0)))) \Rightarrow ((ap\ (ap\ (c\_2Emeasure\_2Emeasure\ A.27a)\ V1m)\ V2s) = \\
& (ap\ (ap\ (c\_2Emeasure\_2Emeasure\ A.27a)\ V0m0)\ V2s)))) \wedge (((ap\ (ap \\
& (c\_2Epair\_2E\_2C\ (2^{A-27a})\ (2^{(2^{A-27a})})))\ (ap\ (c\_2Emeasure\_2Em\_space \\
& A.27a)\ V1m))\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V1m)) = \\
& (ap\ (ap\ (c\_2Emeasure\_2Esigma\ A.27a)\ (ap\ (c\_2Emeasure\_2Em\_space \\
& A.27a)\ V0m0))\ (ap\ (c\_2Emeasure\_2Emeasurable\_sets\ A.27a)\ V0m0)))) \wedge \\
& (p\ (ap\ (c\_2Emeasure\_2Emeasure\_space\ A.27a)\ V1m))))))
\end{aligned}$$