

thm_2Emeasure_2EIN__MEASURABLE__BOREL__SUB (TMEYeYFMRmPThgzht37oE5JP7iHgqsTkzaU)

October 26, 2020

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Ebool_2E_T$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A.\lambda a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c_2Emin_2E_3D (2^{A-27a})))$

Definition 4 We define $c_2Ebool_2E_F$ to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2E_F))$

Let $ty_2Erealax_2Ereal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Erealax_2Ereal \tag{1}$$

Let $ty_2Eenum_2Eenum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eenum_2Eenum \tag{2}$$

Let $c_2Ereal_2Ereal_of_num : \iota$ be given. Assume the following.

$$c_2Ereal_2Ereal_of_num \in (ty_2Erealax_2Ereal^{ty_2Eenum_2Eenum}) \tag{3}$$

Let $ty_2Ehreal_2Ehreal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ehreal_2Ehreal \tag{4}$$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Epair_2Eprod\ A0\ A1) \tag{5}$$

Let $c_2Erealax_2Ereal_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_REP_CLASS \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})^{ty_2Erealax_2Ereal}) \tag{6}$$

Definition 7 We define $c_2Emin_2E.40$ to be $\lambda A.\lambda P \in 2^A.$ if $(\exists x \in A.p (ap P x))$ then (the $(\lambda x.x \in A \wedge p$ of type $\iota \Rightarrow \iota$).

Definition 8 We define $c_2Erealax_2Ereal_REP$ to be $\lambda V0a \in ty_2Erealax_2Ereal.(ap (c_2Emin_2E.40 (ty$

Let $c_2Erealax_2Etrealm_neg : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealm_neg \in ((ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal) (ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)) \quad (7)$$

Let $c_2Erealax_2Etrealm_eq : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealm_eq \in ((2^{(ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)}) (ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)) \quad (8)$$

Let $c_2Erealax_2Ereal_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_ABS_CLASS \in (ty_2Erealax_2Ereal)^{(2^{(ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)})} \quad (9)$$

Definition 9 We define $c_2Erealax_2Ereal_ABS$ to be $\lambda V0r \in (ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal$

Definition 10 We define $c_2Erealax_2Ereal_neg$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.(ap c_2Erealax_2Ereal$

Let $ty_2Eextreal_2Eextreal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eextreal_2Eextreal \quad (10)$$

Let $c_2Eextreal_2EPosInf : \iota$ be given. Assume the following.

$$c_2Eextreal_2EPosInf \in ty_2Eextreal_2Eextreal \quad (11)$$

Let $c_2Eextreal_2ENegInf : \iota$ be given. Assume the following.

$$c_2Eextreal_2ENegInf \in ty_2Eextreal_2Eextreal \quad (12)$$

Let $c_2Eextreal_2Eextreal_sub : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_sub \in ((ty_2Eextreal_2Eextreal)^{ty_2Eextreal_2Eextreal})^{ty_2Eextreal_2Eextreal} \quad (13)$$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (14)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum)^{\omega} \quad (15)$$

Definition 11 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 12 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (16)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (17)$$

Definition 13 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap\ c_2Enum_2EABS_num$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum)^{ty_2Enum_2Enum})_{ty_2Enum_2Enum} \quad (18)$$

Definition 14 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum. (ap\ (ap\ c_2Earithmetic$

Definition 15 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum. V0x$.

Let $c_2Eextreal_2ENormal : \iota$ be given. Assume the following.

$$c_2Eextreal_2ENormal \in (ty_2Eextreal_2Eextreal)^{ty_2Erealax_2Ereal} \quad (19)$$

Definition 16 We define $c_2Eextreal_2Eextreal_of_num$ to be $\lambda V0n \in ty_2Enum_2Enum. (ap\ c_2Eextreal$

Let $c_2Eextreal_2Eextreal_ainv : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_ainv \in (ty_2Eextreal_2Eextreal)^{ty_2Eextreal_2Eextreal} \quad (20)$$

Let $c_2Eextreal_2Eextreal_mul : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_mul \in ((ty_2Eextreal_2Eextreal)^{ty_2Eextreal_2Eextreal})_{ty_2Eextreal_2Eextreal} \quad (21)$$

Let $c_2Eextreal_2Eextreal_add : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_add \in ((ty_2Eextreal_2Eextreal)^{ty_2Eextreal_2Eextreal})_{ty_2Eextreal_2Eextreal} \quad (22)$$

Let $c_2Emeasure_2Espace : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Emeasure_2Espace\ A_27a \in ((2^{A_27a})^{(ty_2Epair_2Eprod\ (2^{A_27a})\ (2^{(2^{A_27a})})})) \quad (23)$$

Definition 17 We define $c_2Epred_set_2EUNIV$ to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. c_2Ebool_2ET)$.

Let $c_2Eextreal_2Eextreal_le : \iota$ be given. Assume the following.

$$c_2Eextreal_2Eextreal_le \in ((ty_2Eextreal_2Eextreal)^{ty_2Eextreal_2Eextreal}) \quad (24)$$

Definition 18 We define $c_2Eextreal_2Eextreal_lt$ to be $\lambda V0x \in ty_2Eextreal_2Eextreal. \lambda V1y \in ty_2Eext$

Definition 19 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.($

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2EABS_prod A_27a A_27b \in ((ty_2Epair_2Eprod A_27a A_27b)^{(2^{A_27b})^{A_27a}}) \quad (25)$$

Definition 20 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0x \in A_27a. \lambda V1y \in A_27b. (ap (c_2Epair_2EABS_prod ($

Let $c_2Epred_set_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epred_set_2EGSPEC A_27a A_27b \in ((2^{A_27a})^{(ty_2Epair_2Eprod A_27a 2)^{A_27b}}) \quad (26)$$

Definition 21 We define c_2Ebool_2EIN to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. (\lambda V1f \in (2^{A_27a}). (ap V1f V0x)))$

Definition 22 We define $c_2Epred_set_2EIMAGE$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in (A_27b^{A_27a}). \lambda V1s \in (A_27a)$

Let $c_2Emeasure_2Esubsets : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Emeasure_2Esubsets A_27a \in (2^{(2^{A_27a})^{(ty_2Epair_2Eprod (2^{A_27a}) (2^{(2^{A_27a})})})}) \quad (27)$$

Definition 23 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap V0P (ap (c_2Emin_2E_40 ($

Definition 24 We define $c_2Epred_set_2EBIGUNION$ to be $\lambda A_27a : \iota. \lambda V0P \in (2^{(2^{A_27a})}). (ap (c_2Epred_set_2EGSPEC ($

Definition 25 We define $c_2Epred_set_2ESUBSET$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap (c_2Ebool_2E_3F ($

Definition 26 We define $c_2Epred_set_2EINJ$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in (A_27b^{A_27a}). \lambda V1s \in (A_27a)$

Definition 27 We define $c_2Epred_set_2Ecountable$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). (ap (c_2Ebool_2E_3F ($

Definition 28 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.($

Definition 29 We define $c_2Epred_set_2EUNION$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap (c_2Ebool_2E_3F ($

Definition 30 We define $c_2Epred_set_2EDIFF$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap (c_2Ebool_2E_3F ($

Definition 31 We define $c_2Epred_set_2EEMPTY$ to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. c_2Ebool_2EF)$.

Definition 32 We define $c_2Emeasure_2Esubset_class$ to be $\lambda A_27a : \iota. \lambda V0sp \in (2^{A_27a}). \lambda V1sts \in (2^{(2^{A_27a})})$

Definition 33 We define $c_2Emeasure_2Ealgebra$ to be $\lambda A_27a : \iota. \lambda V0a \in (ty_2Epair_2Eprod (2^{A_27a}) (2^{(2^{A_27a})}))$

Definition 34 We define $c_2Emeasure_2Esigma_algebra$ to be $\lambda A_27a : \iota. \lambda V0a \in (ty_2Epair_2Eprod (2^{A_27a}) (2^{(2^{A_27a})}))$

Definition 35 We define $c_2Epred_set_2EBIGINTER$ to be $\lambda A_27a : \iota. \lambda V0P \in (2^{(2^{A_27a})}). (ap (c_2Epred_set_2EGSPEC ($

Definition 36 We define $c_2Emeasure_2Esigma$ to be $\lambda A_27a : \iota.\lambda V0sp \in (2^{A_27a}).\lambda V1st \in (2^{(2^{A_27a})}).(ap$

Definition 37 We define $c_2Emeasure_2EBorel$ to be $(ap (ap (c_2Emeasure_2Esigma ty_2Eextreal_2Eextreal$

Definition 38 We define $c_2Epred_set_2EPREIMAGE$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b^{A_27a}).\lambda V$

Definition 39 We define $c_2Epred_set_2EINTER$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap (c_$

Definition 40 We define $c_2Epred_set_2EFUNSET$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0P \in (2^{A_27a}).\lambda V1Q \in ($

Definition 41 We define $c_2Emeasure_2Emeasurable$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0a \in (ty_2Epair_2Epro$

Assume the following.

$$True \tag{28}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow \\ & True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge ((\\ & (p V0t) \Rightarrow False) \Leftrightarrow (\neg (p V0t)))))) \end{aligned} \tag{29}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \tag{30}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \tag{31}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg (p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(\\ & p V0t)))))) \end{aligned} \tag{32}$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow \\ & ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \end{aligned} \tag{33}$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in 2.(\forall V1x_27 \in 2.(\forall V2y \in 2.(\forall V3y_27 \in \\ & 2.(((p V0x) \Leftrightarrow (p V1x_27)) \wedge ((p V1x_27) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_27)))))) \Rightarrow \\ & (((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_27) \Rightarrow (p V3y_27)))))) \end{aligned} \tag{34}$$

Assume the following.

$$\begin{aligned}
& (((ap\ c_2Eextreal_2Eextreal_ainv\ c_2Eextreal_2ENegInf) = c_2Eextreal_2EPosInf) \wedge \\
& (((ap\ c_2Eextreal_2Eextreal_ainv\ c_2Eextreal_2EPosInf) = c_2Eextreal_2ENegInf) \wedge \\
& (\forall V0x \in ty_2Erealax_2Ereal. ((ap\ c_2Eextreal_2Eextreal_ainv \\
& (ap\ c_2Eextreal_2ENormal\ V0x)) = (ap\ c_2Eextreal_2ENormal\ (ap \\
& \quad c_2Erealax_2Ereal_neg\ V0x))))))
\end{aligned} \tag{35}$$

Assume the following.

$$\begin{aligned}
& (\forall V0x \in ty_2Eextreal_2Eextreal. (\forall V1y \in ty_2Eextreal_2Eextreal. \\
& ((ap\ (ap\ c_2Eextreal_2Eextreal_sub\ V0x)\ V1y) = (ap\ (ap\ c_2Eextreal_2Eextreal_add \\
& \quad V0x)\ (ap\ c_2Eextreal_2Eextreal_ainv\ V1y))))))
\end{aligned} \tag{36}$$

Assume the following.

$$\begin{aligned}
& (\forall V0x \in ty_2Eextreal_2Eextreal. ((ap\ c_2Eextreal_2Eextreal_ainv \\
& V0x) = (ap\ (ap\ c_2Eextreal_2Eextreal_mul\ (ap\ c_2Eextreal_2Eextreal_ainv \\
& \quad (ap\ c_2Eextreal_2Eextreal_of_num\ (ap\ c_2Earithmetic_2ENUMERAL \\
& \quad \quad (ap\ c_2Earithmetic_2EBIT1\ c_2Earithmetic_2EZERO))))))\ V0x)))
\end{aligned} \tag{37}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0a \in (ty_2Epair_2Eprod \\
& \quad (2^{A_27a})\ (2^{(2^{A_27a})})). (\forall V1f \in (ty_2Eextreal_2Eextreal^{A_27a}). \\
& (\forall V2g \in (ty_2Eextreal_2Eextreal^{A_27a}). (\forall V3z \in ty_2Erealax_2Ereal. \\
& \quad ((p\ (ap\ (c_2Emeasure_2Esigma_algebra\ A_27a)\ V0a)) \wedge ((p\ (ap\ (\\
& \quad \quad ap\ (c_2Ebool_2EIN\ (ty_2Eextreal_2Eextreal^{A_27a})\ V1f)\ (ap\ (ap \\
& \quad \quad \quad (c_2Emeasure_2Emeasurable\ A_27a\ ty_2Eextreal_2Eextreal)\ V0a) \\
& \quad \quad \quad c_2Emeasure_2EBorel)))) \wedge (\forall V4x \in A_27a. ((p\ (ap\ (ap\ (c_2Ebool_2EIN \\
& \quad \quad A_27a)\ V4x)\ (ap\ (c_2Emeasure_2Espace\ A_27a)\ V0a))) \Rightarrow ((ap\ V2g\ V4x) = \\
& \quad \quad (ap\ (ap\ c_2Eextreal_2Eextreal_mul\ (ap\ c_2Eextreal_2ENormal \\
& \quad \quad \quad V3z))\ (ap\ V1f\ V4x)))))) \Rightarrow (p\ (ap\ (ap\ (c_2Ebool_2EIN\ (ty_2Eextreal_2Eextreal^{A_27a}) \\
& \quad \quad \quad V2g)\ (ap\ (ap\ (c_2Emeasure_2Emeasurable\ A_27a\ ty_2Eextreal_2Eextreal) \\
& \quad \quad \quad \quad V0a)\ c_2Emeasure_2EBorel))))))
\end{aligned} \tag{38}$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0a \in (\text{ty_2Epair_2Eprod} \\
& (2^{A_{27a}}) (2^{(2^{A_{27a}})})). (\forall V1f \in (\text{ty_2Eextreal_2Eextreal}^{A_{27a}}). \\
& (\forall V2g \in (\text{ty_2Eextreal_2Eextreal}^{A_{27a}}). (\forall V3h \in (\\
& \text{ty_2Eextreal_2Eextreal}^{A_{27a}}). (((p (ap (c_2Emeasure_2Esigma_algebra \\
& A_{27a}) V0a)) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal}^{A_{27a}}) \\
& V1f) (ap (ap (c_2Emeasure_2Emeasurable A_{27a} ty_2Eextreal_2Eextreal) \\
V0a) c_2Emeasure_2EBorel)))) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal}^{A_{27a}}) \\
& V2g) (ap (ap (c_2Emeasure_2Emeasurable A_{27a} ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel)))) \wedge (\forall V4x \in A_{27a}. ((p (ap (ap (\\
& c_2Ebool_2EIN A_{27a}) V4x) (ap (c_2Emeasure_2Espace A_{27a}) V0a))) \Rightarrow \\
& ((ap V3h V4x) = (ap (ap c_2Eextreal_2Eextreal_add (ap V1f V4x) \\
& (ap V2g V4x)))))) \Rightarrow (p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal}^{A_{27a}}) \\
& V3h) (ap (ap (c_2Emeasure_2Emeasurable A_{27a} ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel)))))))))
\end{aligned} \tag{39}$$

Theorem 1

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0a \in (\text{ty_2Epair_2Eprod} \\
& (2^{A_{27a}}) (2^{(2^{A_{27a}})})). (\forall V1f \in (\text{ty_2Eextreal_2Eextreal}^{A_{27a}}). \\
& (\forall V2g \in (\text{ty_2Eextreal_2Eextreal}^{A_{27a}}). (\forall V3h \in (\\
& \text{ty_2Eextreal_2Eextreal}^{A_{27a}}). (((p (ap (c_2Emeasure_2Esigma_algebra \\
& A_{27a}) V0a)) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal}^{A_{27a}}) \\
& V1f) (ap (ap (c_2Emeasure_2Emeasurable A_{27a} ty_2Eextreal_2Eextreal) \\
V0a) c_2Emeasure_2EBorel)))) \wedge ((p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal}^{A_{27a}}) \\
& V2g) (ap (ap (c_2Emeasure_2Emeasurable A_{27a} ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel)))) \wedge (\forall V4x \in A_{27a}. ((p (ap (ap (\\
& c_2Ebool_2EIN A_{27a}) V4x) (ap (c_2Emeasure_2Espace A_{27a}) V0a))) \Rightarrow \\
& ((ap V3h V4x) = (ap (ap c_2Eextreal_2Eextreal_sub (ap V1f V4x) \\
& (ap V2g V4x)))))) \Rightarrow (p (ap (ap (c_2Ebool_2EIN (ty_2Eextreal_2Eextreal}^{A_{27a}}) \\
& V3h) (ap (ap (c_2Emeasure_2Emeasurable A_{27a} ty_2Eextreal_2Eextreal) \\
& V0a) c_2Emeasure_2EBorel)))))))))
\end{aligned}$$