

# thm\_2Eone\_2Eone\_\_Axiom (TMPPrXqTH2qbN8zeG6obrjrnXBdk8v4HoZXD)

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**Definition 1** We define `c_2Emin_2E_40` to be  $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p \text{ (ap } P \ x)) \text{ then (the } (\lambda x. x \in A \wedge p \text{ of type } \iota \Rightarrow \iota).$

**Definition 2** We define `c_2Emin_2E_3D` to be  $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj\_o } (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define `c_2Ebool_2E_3F` to be  $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } V0P \text{ (ap (c_2Emin_2E_40 } A$

**Definition 4** We define `c_2Emin_2E_3D_3D_3E` to be  $\lambda P \in 2. \lambda Q \in 2. \text{inj\_o } (p \Rightarrow q)$  of type  $\iota$ .

**Definition 5** We define `c_2Ebool_2E_T` to be  $(\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^2)) (\lambda V0x \in 2. V0x)) (\lambda V1x \in 2. V1x$

**Definition 6** We define `c_2Ebool_2E_21` to be  $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^{A-27a}$

**Definition 7** We define `c_2Ebool_2E_2F_5C` to be  $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (\text{ap } (\text{c_2Ebool_2E_21 } 2) (\lambda V2t \in 2$

**Definition 8** We define `c_2Ebool_2E_3F_21` to be  $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } \text{c_2Ebool_2E_2F_5C$

Let `ty_2Eone_2Eone` :  $\iota$  be given. Assume the following.

$$\text{nonempty ty\_2Eone\_2Eone} \tag{1}$$

**Definition 9** We define `c_2Eone_2Eone` to be  $(\text{ap } (\text{c_2Emin_2E_40 } \text{ty\_2Eone\_2Eone}) (\lambda V0x \in \text{ty\_2Eone\_2Eone}$

Assume the following.

$$\text{True} \tag{2}$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p \ V0t1) \Rightarrow (p \ V1t2)) \Rightarrow (((p \ V1t2) \Rightarrow (p \ V0t1)) \Rightarrow ((p \ V0t1) \Leftrightarrow (p \ V1t2)))))) \tag{3}$$

Assume the following.

$$\forall A. 27a. \text{nonempty } A. 27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A. 27a. (p \ V0t)) \Leftrightarrow (p \ V0t))) \tag{4}$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (5)$$

Assume the following.

$$(\forall V0v \in ty\_2Eone\_2Eone. (V0v = c\_2Eone\_2Eone)) \quad (6)$$

**Theorem 1**

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0e \in A\_27a. (p\ (ap\ (c\_2Ebool\_2E\_3F\_21\ (A\_27a^{ty\_2Eone\_2Eone}))\ (\lambda V1fn \in (A\_27a^{ty\_2Eone\_2Eone}).\ (ap\ (ap\ (c\_2Emin\_2E\_3D\ A\_27a)\ (ap\ V1fn\ c\_2Eone\_2Eone))\ V0e))))))$$