



**Definition 7** We define  $c\_Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_Ebool\_2E\_21 2) (\lambda V2t \in 2$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg (p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg (p V0t)))))) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow ( \\ & (\forall V0a \in (ty\_2Epath\_2Epath A\_27a A\_27b).((ap (c\_2Epath\_2EtoPath \\ & A\_27a A\_27b) (ap (c\_2Epath\_2EfromPath A\_27a A\_27b) V0a)) = V0a)) \wedge \\ & (\forall V1r \in (ty\_2Epair\_2Eprod A\_27a (ty\_2Ellist\_2Ellist (ty\_2Epair\_2Eprod \\ & A\_27b A\_27a))).((p (ap (\lambda V2x \in (ty\_2Epair\_2Eprod A\_27a (ty\_2Ellist\_2Ellist \\ & (ty\_2Epair\_2Eprod A\_27b A\_27a))).c\_2Ebool\_2ET) V1r)) \Leftrightarrow ((ap ( \\ & c\_2Epath\_2EfromPath A\_27a A\_27b) (ap (c\_2Epath\_2EtoPath A\_27a \\ & A\_27b) V1r)) = V1r))) \end{aligned} \quad (7)$$

**Theorem 1**

$$\begin{aligned} & \forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow ( \\ & (\forall V0a \in (ty\_2Epath\_2Epath A\_27a A\_27b).((ap (c\_2Epath\_2EtoPath \\ & A\_27a A\_27b) (ap (c\_2Epath\_2EfromPath A\_27a A\_27b) V0a)) = V0a)) \wedge \\ & (\forall V1r \in (ty\_2Epair\_2Eprod A\_27a (ty\_2Ellist\_2Ellist (ty\_2Epair\_2Eprod \\ & A\_27b A\_27a))).((ap (c\_2Epath\_2EfromPath A\_27a A\_27b) (ap (c\_2Epath\_2EtoPath \\ & A\_27a A\_27b) V1r)) = V1r))) \end{aligned}$$