

thm_2Epath_2Esimulation_trace_inclusion (TMM3KWv3kWqmm6ppb36KB2YwiqdziXemJkc)

October 26, 2020

Definition 1 We define `c_2Emin_2E_40` to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p \text{ (ap } P \ x)) \text{ then (the } (\lambda x. x \in A \wedge p \text{ of type } \iota \Rightarrow \iota).$

Definition 2 We define `c_2Emin_2E_3D` to be $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj_o } (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define `c_2Ebool_2E_2ET` to be $(\text{ap } (\text{ap } (c_2Emin_2E_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x))$

Definition 4 We define `c_2Ebool_2EBOUNDED` to be $(\lambda V0v \in 2. c_2Ebool_2E_2ET)$.

Let `c_2Enum_2EZERO_REP` : ι be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \text{omega} \tag{1}$$

Let `ty_2Enum_2Enum` : ι be given. Assume the following.

$$\text{nonempty } ty_2Enum_2Enum \tag{2}$$

Let `c_2Enum_2EABS_num` : ι be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\text{omega}}) \tag{3}$$

Definition 5 We define `c_2Enum_2E0` to be $(\text{ap } c_2Enum_2EABS_num \ c_2Enum_2EZERO_REP)$.

Definition 6 We define `c_2Earithmetic_2EZERO` to be `c_2Enum_2E0`.

Let `c_2Enum_2EREP_num` : ι be given. Assume the following.

$$c_2Enum_2EREP_num \in (\text{omega}^{ty_2Enum_2Enum}) \tag{4}$$

Let `c_2Enum_2ESUC_REP` : ι be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\text{omega}^{\text{omega}}) \tag{5}$$

Definition 7 We define `c_2Ebool_2E_21` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (c_2Emin_2E_3D \ (2^{A-27a}))))$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (6)$$

Definition 9 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earithmetic_2E_2B$

Definition 10 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $ty_2Eoption_2Eoption : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Eoption_2Eoption\ A0) \quad (7)$$

Let $ty_2Ellist_2Ellist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Ellist_2Ellist\ A0) \quad (8)$$

Let $c_2Ellist_2Ellist_rep : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ellist_2Ellist_rep\ A_27a \in ((ty_2Eoption_2Eoption\ A_27a)^{ty_2Enum_2Enum})^{(ty_2Ellist_2Ellist\ A_27a)} \quad (9)$$

Let $c_2Ellist_2Ellist_abs : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ellist_2Ellist_abs\ A_27a \in ((ty_2Ellist_2Ellist\ A_27a)^{(ty_2Eoption_2Eoption\ A_27a)^{ty_2Enum_2Enum}}) \quad (10)$$

Let $ty_2Eone_2Eone : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eone_2Eone \quad (11)$$

Definition 11 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o\ (p\ P \Rightarrow p\ Q)$ of type ι .

Definition 12 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in 2.$

Let $ty_2Esum_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Esum_2Esum\ A0\ A1) \quad (12)$$

Let $c_2Esum_2EABS_sum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Esum_2EABS_sum\ A_27a\ A_27b \in ((ty_2Esum_2Esum\ A_27a\ A_27b)^{((2^{A_27b})^{A_27a})^2}) \quad (13)$$

Definition 13 We define c_2Esum_2EINL to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0e \in A_27a.(ap\ (c_2Esum_2EABS_sum$

Let $c_2Eoption_2Eoption_ABS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Eoption_2Eoption_ABS\ A_27a \in ((ty_2Eoption_2Eoption\ A_27a)^{(ty_2Esum_2Esum\ A_27a\ ty_2Eone_2Eone)}) \quad (14)$$

Definition 14 We define $c_2Eoption_2ESOME$ to be $\lambda A_27a : \iota. \lambda V0x \in A_27a. (ap\ (c_2Eoption_2Eoption_ABS\ A_27a)\ V0x)$

Definition 15 We define c_2Eone_2Eone to be $(ap\ (c_2Emin_2E40\ ty_2Eone_2Eone)\ (\lambda V0x \in ty_2Eone_2Eone.\ V0x))$

Definition 16 We define c_2Ebool_2EF to be $(ap\ (c_2Ebool_2E21\ 2)\ (\lambda V0t \in 2.V0t))$.

Definition 17 We define c_2Ebool_2E7E to be $(\lambda V0t \in 2. (ap\ (ap\ c_2Emin_2E3D_3D_3E\ V0t)\ c_2Ebool_2E7E))$

Definition 18 We define c_2Esum_2EINR to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0e \in A_27b. (ap\ (c_2Esum_2EABS\ A_27a\ A_27b)\ V0e)$

Definition 19 We define $c_2Eoption_2ENONE$ to be $\lambda A_27a : \iota. (ap\ (c_2Eoption_2Eoption_ABS\ A_27a)\ 0)$

Definition 20 We define $c_2Ellist_2ELHD$ to be $\lambda A_27a : \iota. \lambda V0ll \in (ty_2Ellist_2Ellist\ A_27a). (ap\ (ap\ (c_2Eoption_2Eoption_ABS\ A_27a)\ V0ll))$

Let $c_2Eoption_2Eoption_CASE : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Eoption_2Eoption_CASE\ A_27a\ A_27b \in (((A_27b^{(A_27b^{A_27a}})})^{A_27b})^{(ty_2Eoption_2Eoption\ A_27a)}) \quad (15)$$

Definition 21 We define $c_2Ellist_2ELTL$ to be $\lambda A_27a : \iota. \lambda V0ll \in (ty_2Ellist_2Ellist\ A_27a). (ap\ (ap\ (ap\ (c_2Eoption_2Eoption_ABS\ A_27a)\ V0ll)\ V0ll))$

Definition 22 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A_27a. (\lambda V2t2 \in A_27a. (ap\ (c_2Eoption_2Eoption_ABS\ A_27a)\ V2t2))))$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Epair_2Eprod\ A0\ A1) \quad (16)$$

Let $ty_2Epath_2Epath : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Epath_2Epath\ A0\ A1) \quad (17)$$

Let $c_2Epath_2EfromPath : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epath_2EfromPath\ A_27a\ A_27b \in ((ty_2Epair_2Eprod\ A_27a\ (ty_2Ellist_2Ellist\ (ty_2Epair_2Eprod\ A_27b\ A_27a)))^{(ty_2Epath_2Epath\ A_27a\ A_27b)}) \quad (18)$$

Let $c_2Epair_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2EFST\ A_27a\ A_27b \in (A_27a^{(ty_2Epair_2Eprod\ A_27a\ A_27b)}) \quad (19)$$

Let $c_2Epath_2Etail : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epath_2Etail \\ & A_27a\ A_27b \in ((ty_2Epath_2Epath\ A_27a\ A_27b)^{(ty_2Epath_2Epath\ A_27a\ A_27b)}) \end{aligned} \quad (20)$$

Let $c_2Epath_2Efirst_label : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epath_2Efirst_label \\ & A_27a\ A_27b \in (A_27b)^{(ty_2Epath_2Epath\ A_27a\ A_27b)} \end{aligned} \quad (21)$$

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (22)$$

Definition 23 We define $c_2Ellist_2ELCONS$ to be $\lambda A_27a : \iota. \lambda V0h \in A_27a. \lambda V1t \in (ty_2Ellist_2Ellist\ A_27a)$

Definition 24 We define $c_2Ellist_2ELNIL$ to be $\lambda A_27a : \iota. (ap\ (c_2Ellist_2Ellist_abs\ A_27a)\ (\lambda V0n \in ty_2Ellist_2Ellist\ A_27a))$

Definition 25 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap\ V0P\ (ap\ (c_2Emin_2E_40\ A_27a)\ (c_2Ebool_2E_3F\ A_27a))))$

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2EABS_prod \\ & A_27a\ A_27b \in ((ty_2Epair_2Eprod\ A_27a\ A_27b)^{(2^{A_27b})^{A_27a}}) \end{aligned} \quad (23)$$

Definition 26 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0x \in A_27a. \lambda V1y \in A_27b. (ap\ (c_2Epair_2EABS_prod\ A_27a\ A_27b)\ (V0x\ V1y))$

Let $c_2Epath_2EtoPath : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epath_2EtoPath \\ & A_27a\ A_27b \in ((ty_2Epath_2Epath\ A_27a\ A_27b)^{(ty_2Epair_2Eprod\ A_27a\ A_27b)\ (ty_2Ellist_2Ellist\ (ty_2Epair_2Eprod\ A_27a\ A_27b))}) \end{aligned} \quad (24)$$

Definition 27 We define $c_2Epath_2Estopped_at$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0x \in A_27a. (ap\ (c_2Epath_2EtoPath\ A_27a\ A_27b)\ (V0x\ V0x))$

Definition 28 We define $c_2Epath_2Eis_stopped$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0p \in (ty_2Epath_2Epath\ A_27a\ A_27b)$

Definition 29 We define $c_2Epath_2Efirst$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0p \in (ty_2Epath_2Epath\ A_27a\ A_27b)$

Let $c_2Epair_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2ESND \\ & A_27a\ A_27b \in (A_27b)^{(ty_2Epair_2Eprod\ A_27a\ A_27b)} \end{aligned} \quad (25)$$

Definition 30 We define c_2Epath_2Epcns to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0x \in A_27a. \lambda V1r \in A_27b. \lambda V2p \in (ty_2Epath_2Epath\ A_27a\ A_27b)$

Definition 31 We define $c_2Epair_2EUNCURRY$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda A_27c : \iota. \lambda V0f \in ((A_27c)^{A_27a})^{A_27b}$

Let $c_2Eoption_2EOPTION_MAP : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow \forall A_27b.nonempty \ A_27b \Rightarrow c_2Eoption_2EOPTION_MAP \\ & A_27a \ A_27b \in (((ty_2Eoption_2Eoption \ A_27b)^{(ty_2Eoption_2Eoption \ A_27a)} (A_27b^{A_27a})) \end{aligned} \quad (26)$$

Definition 32 We define $c_2Ecombin_2EK$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. (\lambda V0x \in A_27a. (\lambda V1y \in A_27b. V0x))$

Definition 33 We define $c_2Ecombin_2Eo$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda A_27c : \iota. \lambda V0f \in (A_27b^{A_27c}). \lambda V1g \in (A_27c^{A_27a})$

Let $c_2Eoption_2EOPTION_BIND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow \forall A_27b.nonempty \ A_27b \Rightarrow c_2Eoption_2EOPTION_BIND \\ & A_27a \ A_27b \in (((ty_2Eoption_2Eoption \ A_27a)^{(ty_2Eoption_2Eoption \ A_27a)^{A_27b}}) (ty_2Eoption_2Eoption \ A_27b) \end{aligned} \quad (27)$$

Let $c_2Earithmetic_2EFUNPOW : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow c_2Earithmetic_2EFUNPOW \ A_27a \in \\ & (((A_27a^{A_27a})^{ty_2Enum_2Enum}) (A_27a^{A_27a})) \end{aligned} \quad (28)$$

Definition 34 We define $c_2Ellist_2ELUNFOLD$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in ((ty_2Eoption_2Eoption \ A_27b)^{(ty_2Eoption_2Eoption \ A_27a)})$

Let $c_2Epath_2Elabels : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow \forall A_27b.nonempty \ A_27b \Rightarrow c_2Epath_2Elabels \\ & A_27a \ A_27b \in ((ty_2Ellist_2Ellist \ A_27b)^{(ty_2Epath_2Epath \ A_27a \ A_27b)}) \end{aligned} \quad (29)$$

Definition 35 We define $c_2Epath_2Eunfold$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda A_27c : \iota. \lambda V0proj \in (A_27a^{A_27c})$

Definition 36 We define c_2Ebool_2EIN to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. (\lambda V1f \in (2^{A_27a}). (ap \ V1f \ V0x)))$

Let $c_2Epred_set_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty \ A_27a \Rightarrow \forall A_27b.nonempty \ A_27b \Rightarrow c_2Epred_set_2EGSPEC \\ & A_27a \ A_27b \in ((2^{A_27a})^{((ty_2Epair_2Eprod \ A_27a \ 2)^{A_27b})}) \end{aligned} \quad (30)$$

Definition 37 We define $c_2Epred_set_2EUNIV$ to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. c_2Ebool_2EET)$.

Definition 38 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap \ (c_2Ebool_2E_21 \ 2) \ (\lambda V2t \in 2. (c_2Ebool_2E_21 \ 2) \ V2t))))$

Definition 39 We define $c_2Epred_set_2EUNION$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap \ (c_2Epred_set_2EGSPEC \ A_27a) \ V1t)$

Definition 40 We define $c_2Epath_2Eokpath_f$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in (((2^{A_27a})^{A_27b})^{A_27a})$.

Definition 41 We define $c_2Epred_set_2ESUBSET$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A_27a}). \lambda V1t \in (2^{A_27a}). (ap \ (c_2Epred_set_2EGSPEC \ A_27a) \ V1t)$

Definition 42 We define $c_2Epred_set_2EBIGUNION$ to be $\lambda A_27a : \iota. \lambda V0P \in (2^{(2^{A_27a})}). (ap \ (c_2Epred_set_2EGSPEC \ A_27a) \ V0P)$

Definition 43 We define $c_2\text{EfixedPoint_2Egfp}$ to be $\lambda A_27a : \iota.\lambda V0f \in ((2^{A_27a})^{(2^{A_27a})}) . (ap (c_2\text{Epred_2Egfp} (V0f)))$

Definition 44 We define $c_2\text{Epath_2Eokpath}$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0R \in (((2^{A_27a})^{A_27b})^{A_27a}) . (ap (c_2\text{Epath_2Eokpath} (V0R)))$

Assume the following.

$$True \quad (31)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. ((p V0t1) \Rightarrow (p V1t2)) \Rightarrow ((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))) \quad (32)$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \quad (33)$$

Assume the following.

$$(\forall V0t \in 2. (((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))))) \quad (34)$$

Assume the following.

$$(\forall V0t \in 2. (((True \vee (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \vee True) \Leftrightarrow True) \wedge (((False \vee (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee False) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee (p V0t)) \Leftrightarrow (p V0t)))))) \quad (35)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow \neg (p V0t)))))) \quad (36)$$

Assume the following.

$$((\forall V0t \in 2. ((\neg(\neg(p V0t))) \Leftrightarrow (p V0t)) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True)))) \quad (37)$$

Assume the following.

$$\forall A_27a. \text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. (V0x = V0x)) \quad (38)$$

Assume the following.

$$\forall A_27a. \text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (39)$$

Assume the following.

$$\forall A_27a. \text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (40)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow \neg(p V0t)) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow \neg(p V0t)))))) \quad (41)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in (2^{A.27a}).(\forall V1Q \in (2^{A.27a}).((\forall V2x \in A.27a.((p (ap V0P V2x)) \wedge (p (ap V1Q V2x)))) \Leftrightarrow ((\forall V3x \in A.27a.(p (ap V0P V3x)) \wedge (\forall V4x \in A.27a.(p (ap V1Q V4x)))))))))) \quad (42)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in (2^{A.27a}).(\forall V1Q \in 2.(((\forall V2x \in A.27a.(p (ap V0P V2x))) \wedge (p V1Q)) \Leftrightarrow (\forall V3x \in A.27a.((p (ap V0P V3x)) \wedge (p V1Q)))))) \quad (43)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in 2.(\forall V1Q \in (2^{A.27a}).(((p V0P) \wedge (\forall V2x \in A.27a.(p (ap V1Q V2x)))) \Leftrightarrow (\forall V3x \in A.27a.((p V0P) \wedge (p (ap V1Q V3x))))))) \quad (44)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in 2.(\forall V1Q \in (2^{A.27a}).(((\forall V2x \in A.27a.((p V0P) \vee (p (ap V1Q V2x)))) \Leftrightarrow ((p V0P) \vee (\forall V3x \in A.27a.(p (ap V1Q V3x))))))) \quad (45)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p V1B) \wedge (p V2C)) \vee (p V0A)) \Leftrightarrow (((p V1B) \vee (p V0A)) \wedge ((p V2C) \vee (p V0A)))))) \quad (46)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (47)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in 2.(\forall V1Q \in 2.(\forall V2x \in A.27a.(\forall V3x.27 \in A.27a.(\forall V4y \in A.27a.(\forall V5y.27 \in A.27a.(((p V0P) \Leftrightarrow (p V1Q)) \wedge (((p V1Q) \Rightarrow (V2x = V3x.27)) \wedge ((\neg(p V1Q)) \Rightarrow (V4y = V5y.27)))))) \Rightarrow ((ap (ap (ap (c.2Ebool_2ECOND A.27a) V0P) V2x) V4y) = (ap (ap (ap (c.2Ebool_2ECOND A.27a) V1Q) V3x.27) V5y.27)))))) \quad (48)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}). (\forall V1a \in \\ A_27a. ((\exists V2x \in A_27a. ((V2x = V1a) \wedge (p\ (ap\ V0P\ V2x)))) \Leftrightarrow (p\ (\\ ap\ V0P\ V1a)))))) \end{aligned} \quad (49)$$

Assume the following.

$$(\forall V0v \in 2. ((p\ (ap\ c_2Ebool_2EBOUNDED\ V0v)) \Leftrightarrow True)) \quad (50)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ ((ap\ (c_2Ellist_2ELHD\ A_27a)\ (c_2Ellist_2ELNIL\ A_27a)) = (c_2Eoption_2ENONE \\ A_27a)) \wedge (\forall V0h \in A_27b. (\forall V1t \in (ty_2Ellist_2Ellist \\ A_27b). ((ap\ (c_2Ellist_2ELHD\ A_27b)\ (ap\ (ap\ (c_2Ellist_2ELCONS \\ A_27b)\ V0h)\ V1t)) = (ap\ (c_2Eoption_2ESOME\ A_27b)\ V0h)))))) \end{aligned} \quad (51)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ ((ap\ (c_2Ellist_2ELTL\ A_27a)\ (c_2Ellist_2ELNIL\ A_27a)) = (c_2Eoption_2ENONE \\ (ty_2Ellist_2Ellist\ A_27a))) \wedge (\forall V0h \in A_27b. (\forall V1t \in \\ (ty_2Ellist_2Ellist\ A_27b). ((ap\ (c_2Ellist_2ELTL\ A_27b)\ (ap \\ (ap\ (c_2Ellist_2ELCONS\ A_27b)\ V0h)\ V1t)) = (ap\ (c_2Eoption_2ESOME \\ (ty_2Ellist_2Ellist\ A_27b)\ V1t)))))) \end{aligned} \quad (52)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0h \in A_27a. (\forall V1t \in \\ (ty_2Ellist_2Ellist\ A_27a). ((\neg((ap\ (ap\ (c_2Ellist_2ELCONS\ A_27a) \\ V0h)\ V1t) = (c_2Ellist_2ELNIL\ A_27a)))) \wedge (\neg((c_2Ellist_2ELNIL \\ A_27a) = (ap\ (ap\ (c_2Ellist_2ELCONS\ A_27a)\ V0h)\ V1t)))))) \end{aligned} \quad (53)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0R \in ((2^{(ty_2Ellist_2Ellist\ A_27b)})^{A_27a}). (\forall V1f \in \\
& \quad ((ty_2Eoption_2Eoption\ (ty_2Epair_2Eprod\ A_27a\ A_27b))^{A_27a}). \\
& \quad (\forall V2s \in A_27a. (\forall V3ll \in (ty_2Ellist_2Ellist\ A_27b). \\
& \quad ((p\ (ap\ (ap\ V0R\ V2s)\ V3ll)) \wedge (\forall V4s \in A_27a. (\forall V5ll \in \\
& \quad (ty_2Ellist_2Ellist\ A_27b). ((p\ (ap\ (ap\ V0R\ V4s)\ V5ll)) \Rightarrow (((ap \\
& \quad V1f\ V4s) = (c_2Eoption_2ENONE\ (ty_2Epair_2Eprod\ A_27a\ A_27b)))) \wedge \\
& \quad (V5ll = (c_2Ellist_2ELNIL\ A_27b))) \vee (\exists V6s_27 \in A_27a. (\exists V7x \in \\
& \quad A_27b. (\exists V8ll_27 \in (ty_2Ellist_2Ellist\ A_27b). (((ap\ V1f \\
& \quad V4s) = (ap\ (c_2Eoption_2ESOME\ (ty_2Epair_2Eprod\ A_27a\ A_27b)) \\
& \quad (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V6s_27)\ V7x))) \wedge (((ap\ (c_2Ellist_2ELHD \\
& \quad A_27b)\ V5ll) = (ap\ (c_2Eoption_2ESOME\ A_27b)\ V7x)) \wedge (((ap\ (c_2Ellist_2ELTL \\
& \quad A_27b)\ V5ll) = (ap\ (c_2Eoption_2ESOME\ (ty_2Ellist_2Ellist\ A_27b)) \\
& \quad V8ll_27)) \wedge (p\ (ap\ (ap\ V0R\ V6s_27)\ V8ll_27)))))))))) \Rightarrow ((ap\ (ap \\
& \quad (c_2Ellist_2ELUNFOLD\ A_27b\ A_27a)\ V1f)\ V2s) = V3ll))))))
\end{aligned} \tag{54}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in \\
& \quad A_27a. (((ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x) = (ap\ (c_2Eoption_2ESOME \\
& \quad A_27a)\ V1y)) \Leftrightarrow (V0x = V1y))))
\end{aligned} \tag{55}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\neg((c_2Eoption_2ENONE \\
& \quad A_27a) = (ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x))))
\end{aligned} \tag{56}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in 2. (\forall V1x \in A_27a. \\
& \quad (\forall V2y \in A_27a. (((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ (ty_2Eoption_2Eoption \\
& \quad A_27a))\ V0P)\ (ap\ (c_2Eoption_2ESOME\ A_27a)\ V1x))\ (c_2Eoption_2ENONE \\
& \quad A_27a)) = (c_2Eoption_2ENONE\ A_27a)) \Leftrightarrow (\neg(p\ V0P))) \wedge (((ap\ (ap\ (\\
& \quad ap\ (c_2Ebool_2ECOND\ (ty_2Eoption_2Eoption\ A_27a))\ V0P)\ (c_2Eoption_2ENONE \\
& \quad A_27a))\ (ap\ (c_2Eoption_2ESOME\ A_27a)\ V1x)) = (c_2Eoption_2ENONE \\
& \quad A_27a)) \Leftrightarrow (p\ V0P)) \wedge (((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ (ty_2Eoption_2Eoption \\
& \quad A_27a))\ V0P)\ (ap\ (c_2Eoption_2ESOME\ A_27a)\ V1x))\ (c_2Eoption_2ENONE \\
& \quad A_27a)) = (ap\ (c_2Eoption_2ESOME\ A_27a)\ V2y)) \Leftrightarrow ((p\ V0P) \wedge (V1x = V2y))) \wedge \\
& \quad (((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ (ty_2Eoption_2Eoption\ A_27a)) \\
& \quad V0P)\ (c_2Eoption_2ENONE\ A_27a))\ (ap\ (c_2Eoption_2ESOME\ A_27a) \\
& \quad V1x)) = (ap\ (c_2Eoption_2ESOME\ A_27a)\ V2y)) \Leftrightarrow ((\neg(p\ V0P)) \wedge (V1x = \\
& \quad V2y)))))))))
\end{aligned} \tag{57}$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad \forall V0x \in A_27a. (\forall V1y \in A_27b. (\forall V2a \in A_27a. (\forall V3b \in \\ & \quad A_27b. (((ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V0x)\ V1y) = (ap\ (ap \\ & \quad (c_2Epair_2E_2C\ A_27a\ A_27b)\ V2a)\ V3b)) \Leftrightarrow ((V0x = V2a) \wedge (V1y = V3b))))))))) \end{aligned} \quad (58)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad \forall V0x \in (ty_2Epair_2Eprod\ A_27a\ A_27b). (\exists V1q \in A_27a. \\ & \quad (\exists V2r \in A_27b. (V0x = (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ \\ & \quad V1q)\ V2r)))))) \end{aligned} \quad (59)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad \forall V0x \in A_27a. (\forall V1y \in A_27b. ((ap\ (c_2Epair_2EFST\ A_27a \\ & \quad A_27b)\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V0x)\ V1y)) = V0x))) \end{aligned} \quad (60)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c. \\ & \quad nonempty\ A_27c \Rightarrow (\forall V0f \in ((A_27c^{A_27b})^{A_27a}). (\forall V1x \in \\ & \quad A_27a. (\forall V2y \in A_27b. ((ap\ (ap\ (c_2Epair_2EUNCURRY\ A_27a \\ & \quad A_27b\ A_27c)\ V0f)\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V1x)\ V2y)) = \\ & \quad (ap\ (ap\ V0f\ V1x)\ V2y)))))) \end{aligned} \quad (61)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad (\forall V0a \in (ty_2Epath_2Epath\ A_27a\ A_27b). ((ap\ (c_2Epath_2EtoPath \\ & \quad A_27a\ A_27b)\ (ap\ (c_2Epath_2EfromPath\ A_27a\ A_27b)\ V0a)) = V0a)) \wedge \\ & \quad (\forall V1r \in (ty_2Epair_2Eprod\ A_27a\ (ty_2Ellist_2Ellist\ (ty_2Epair_2Eprod \\ & \quad A_27b\ A_27a))). ((ap\ (c_2Epath_2EfromPath\ A_27a\ A_27b)\ (ap\ (c_2Epath_2EtoPath \\ & \quad A_27a\ A_27b)\ V1r)) = V1r))) \end{aligned} \quad (62)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad \forall V0p \in (ty_2Epath_2Epath\ A_27a\ A_27b). ((\exists V1x \in A_27a. \\ & \quad (V0p = (ap\ (c_2Epath_2Estopped_at\ A_27a\ A_27b)\ V1x))) \vee (\exists V2x \in \\ & \quad A_27a. (\exists V3r \in A_27b. (\exists V4q \in (ty_2Epath_2Epath\ A_27a \\ & \quad A_27b). (V0p = (ap\ (ap\ (ap\ (c_2Epath_2Epcons\ A_27a\ A_27b)\ V2x)\ V3r \\ & \quad V4q)))))))))) \end{aligned} \quad (63)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& (\forall V0x \in A_27a. ((ap\ (c_2Epath_2Efirst\ A_27a\ A_27b)\ (ap\ (c_2Epath_2Estopped_at \\
& \quad A_27a\ A_27b)\ V0x)) = V0x)) \wedge (\forall V1x \in A_27a. (\forall V2r \in A_27b. \\
& \quad (\forall V3p \in (ty_2Epath_2Epath\ A_27a\ A_27b). ((ap\ (c_2Epath_2Efirst \\
& \quad A_27a\ A_27b)\ (ap\ (ap\ (ap\ (c_2Epath_2Epcons\ A_27a\ A_27b)\ V1x)\ V2r) \\
& \quad \quad V3p)) = V1x)))))) \\
& \hspace{15em} (64)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0x \in A_27a. (\forall V1r \in A_27b. (\forall V2p \in (ty_2Epath_2Epath \\
& \quad A_27a\ A_27b). ((ap\ (c_2Epath_2Etail\ A_27a\ A_27b)\ (ap\ (ap\ (ap\ (c_2Epath_2Epcons \\
& \quad \quad A_27a\ A_27b)\ V0x)\ V1r)\ V2p)) = V2p)))))) \\
& \hspace{15em} (65)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0x \in A_27a. (\forall V1r \in A_27b. (\forall V2p \in (ty_2Epath_2Epath \\
& \quad A_27a\ A_27b). ((ap\ (c_2Epath_2Efirst_label\ A_27a\ A_27b)\ (ap\ (\\
& \quad \quad ap\ (ap\ (c_2Epath_2Epcons\ A_27a\ A_27b)\ V0x)\ V1r)\ V2p)) = V1r)))))) \\
& \hspace{15em} (66)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad (\forall V0x \in A_27a. ((ap\ (c_2Epath_2Elabels\ A_27a\ A_27b)\ (ap\ (\\
& \quad \quad c_2Epath_2Estopped_at\ A_27a\ A_27b)\ V0x)) = (c_2Elist_2ELNIL \\
& \quad \quad A_27b))) \wedge (\forall V1x \in A_27a. (\forall V2r \in A_27b. (\forall V3p \in \\
& \quad (ty_2Epath_2Epath\ A_27a\ A_27b). ((ap\ (c_2Epath_2Elabels\ A_27a \\
& \quad A_27b)\ (ap\ (ap\ (ap\ (c_2Epath_2Epcons\ A_27a\ A_27b)\ V1x)\ V2r)\ V3p)) = \\
& \quad \quad (ap\ (ap\ (c_2Elist_2ELCONS\ A_27b)\ V2r)\ (ap\ (c_2Epath_2Elabels \\
& \quad \quad \quad A_27a\ A_27b)\ V3p))))))))) \\
& \hspace{15em} (67)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c. \\
& \quad nonempty\ A_27c \Rightarrow \forall A_27d.nonempty\ A_27d \Rightarrow ((\forall V0x \in A_27a. \\
& \quad ((p\ (ap\ (c_2Epath_2Eis_stopped\ A_27a\ A_27b)\ (ap\ (c_2Epath_2Estopped_at \\
& \quad \quad A_27a\ A_27b)\ V0x))) \Leftrightarrow True)) \wedge (\forall V1x \in A_27c. (\forall V2r \in \\
& \quad A_27d. (\forall V3p \in (ty_2Epath_2Epath\ A_27c\ A_27d). ((p\ (ap\ (c_2Epath_2Eis_stopped \\
& \quad \quad A_27c\ A_27d)\ (ap\ (ap\ (ap\ (c_2Epath_2Epcons\ A_27c\ A_27d)\ V1x)\ V2r) \\
& \quad \quad \quad V3p))) \Leftrightarrow False)))))) \\
& \hspace{15em} (68)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0R \in (((2^{A_27a})^{A_27b})^{A_27a}).((\forall V1x \in A_27a.(\\
p\ (ap\ (ap\ (c_2Epath_2Eokpath\ A_27a\ A_27b)\ V0R)\ (ap\ (c_2Epath_2Estopped_at \\
& \quad A_27a\ A_27b)\ V1x)))) \wedge (\forall V2x \in A_27a.(\forall V3r \in A_27b. \\
& \quad (\forall V4p \in (ty_2Epath_2Epath\ A_27a\ A_27b).((p\ (ap\ (ap\ (c_2Epath_2Eokpath \\
& \quad A_27a\ A_27b)\ V0R)\ (ap\ (ap\ (ap\ (c_2Epath_2Epcons\ A_27a\ A_27b)\ V2x) \\
& \quad V3r)\ V4p)))) \Leftrightarrow ((p\ (ap\ (ap\ (ap\ V0R\ V2x)\ V3r)\ (ap\ (c_2Epath_2Efirst\ A_27a \\
& \quad A_27b)\ V4p)))) \wedge (p\ (ap\ (ap\ (c_2Epath_2Eokpath\ A_27a\ A_27b)\ V0R)\ V4p))))))))) \\
& \hspace{15em} (69)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c. \\
& \quad nonempty\ A_27c \Rightarrow (\forall V0proj \in (A_27b^{A_27a}).(\forall V1f \in (\\
& \quad (ty_2Eoption_2Eoption\ (ty_2Epair_2Eprod\ A_27a\ A_27c))^{A_27a}). \\
& \quad (\forall V2s \in A_27a.((ap\ (c_2Epath_2Elabels\ A_27b\ A_27c)\ (ap\ (\\
& \quad ap\ (ap\ (c_2Epath_2Eunfold\ A_27b\ A_27c\ A_27a)\ V0proj)\ V1f)\ V2s)) = \\
& \quad (ap\ (ap\ (c_2Elist_2ELUNFOLD\ A_27c\ A_27a)\ V1f)\ V2s)))))) \\
& \hspace{15em} (70)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c. \\
& \quad nonempty\ A_27c \Rightarrow (\forall V0P \in (2^{A_27a}).(\forall V1m \in (((2^{A_27b})^{A_27c})^{A_27b}). \\
& \quad (\forall V2proj \in (A_27b^{A_27a}).(\forall V3f \in ((ty_2Eoption_2Eoption \\
& \quad (ty_2Epair_2Eprod\ A_27a\ A_27c))^{A_27a}).(\forall V4s \in A_27a.(\\
& \quad ((p\ (ap\ V0P\ V4s)) \wedge ((\forall V5s \in A_27a.(\forall V6s_27 \in A_27a. \\
& \quad (\forall V7l \in A_27c.(((p\ (ap\ V0P\ V5s)) \wedge ((ap\ V3f\ V5s) = (ap\ (c_2Eoption_2ESOME \\
& \quad (ty_2Epair_2Eprod\ A_27a\ A_27c))\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27a \\
& \quad A_27c)\ V6s_27)\ V7l)))) \Rightarrow (p\ (ap\ V0P\ V6s_27)))))) \wedge (\forall V8s \in A_27a. \\
& \quad (\forall V9s_27 \in A_27a.(\forall V10l \in A_27c.(((p\ (ap\ V0P\ V8s)) \wedge \\
& \quad ((ap\ V3f\ V8s) = (ap\ (c_2Eoption_2ESOME\ (ty_2Epair_2Eprod\ A_27a \\
& \quad A_27c))\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27c)\ V9s_27)\ V10l)))) \Rightarrow \\
& \quad (p\ (ap\ (ap\ (ap\ V1m\ (ap\ V2proj\ V8s))\ V10l)\ (ap\ V2proj\ V9s_27))))))))) \Rightarrow \\
& \quad (p\ (ap\ (ap\ (c_2Epath_2Eokpath\ A_27b\ A_27c)\ V1m)\ (ap\ (ap\ (ap\ (c_2Epath_2Eunfold \\
& \quad A_27b\ A_27c\ A_27a)\ V2proj)\ V3f)\ V4s))))))))) \\
& \hspace{15em} (71)
\end{aligned}$$

Assume the following.

$$(\forall V0t \in 2.((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \quad (72)$$

Assume the following.

$$(\forall V0A \in 2.((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \quad (73)$$

Assume the following.

$$\begin{aligned}
& (\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\
& \quad (((p\ V0A) \Rightarrow False) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))))) \\
& \hspace{15em} (74)
\end{aligned}$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((\neg(\neg(p V0A)) \vee (p V1B))) \Rightarrow False) \Leftrightarrow (p V0A) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))) \quad (75)$$

Assume the following.

$$(\forall V0A \in 2.(((\neg(p V0A)) \Rightarrow False) \Rightarrow (((p V0A) \Rightarrow False) \Rightarrow False))) \quad (76)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (p V1q) \Leftrightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee ((p V1q) \vee (p V2r))) \wedge (((p V0p) \vee (\neg(p V2r)) \vee (\neg(p V1q)))) \wedge (((p V1q) \vee (\neg(p V2r)) \vee (\neg(p V0p)))) \wedge ((p V2r) \vee ((\neg(p V1q)) \vee (\neg(p V0p)))))))))) \quad (77)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (p V1q) \wedge (p V2r)) \Leftrightarrow (((p V0p) \vee (\neg(p V1q)) \vee (\neg(p V2r)))) \wedge (((p V1q) \vee (\neg(p V0p))) \wedge ((p V2r) \vee (\neg(p V0p)))))))) \quad (78)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (p V1q) \vee (p V2r)) \Leftrightarrow (((p V0p) \vee (\neg(p V1q))) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge ((p V1q) \vee ((p V2r) \vee (\neg(p V0p)))))))))) \quad (79)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p V0p) \Leftrightarrow (p V1q) \Rightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge ((\neg(p V1q)) \vee ((p V2r) \vee (\neg(p V0p)))))))))) \quad (80)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((p V0p) \Leftrightarrow (\neg(p V1q))) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge ((\neg(p V1q)) \vee (\neg(p V0p)))))) \quad (81)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (p V0p)))) \quad (82)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (\neg(p V1q)))))) \quad (83)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.(((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V0p)))))) \quad (84)$$

Assume the following.

$$(\forall V0p \in 2.(\forall V1q \in 2.((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V1q)))))) \quad (85)$$

Assume the following.

$$(\forall V0p \in 2.((\neg(\neg(p V0p))) \Rightarrow (p V0p))) \quad (86)$$

Theorem 1

$$\begin{aligned} & \forall A.27a.nonempty \ A.27a \Rightarrow \forall A.27b.nonempty \ A.27b \Rightarrow \forall A.27c. \\ & \quad nonempty \ A.27c \Rightarrow (\forall V0R \in ((2^{A.27b})^{A.27a}).(\forall V1M1 \in \\ & \quad ((2^{A.27a})^{A.27c})^{A.27a}).(\forall V2M2 \in ((2^{A.27b})^{A.27c})^{A.27b}). \\ & \quad (\forall V3p \in (ty_2Epath_2Epath \ A.27a \ A.27c).(\forall V4t_init \in \\ & \quad A.27b.(((\forall V5s1 \in A.27a.(\forall V6l \in A.27c.(\forall V7s2 \in \\ & \quad A.27a.(\forall V8t1 \in A.27b.(((p \ (ap \ (ap \ V0R \ V5s1) \ V8t1)) \wedge (p \ (ap \\ & \quad (ap \ (ap \ V1M1 \ V5s1) \ V6l) \ V7s2))) \Rightarrow (\exists V9t2 \in A.27b.((p \ (ap \ (ap \\ & \quad V0R \ V7s2) \ V9t2)) \wedge (p \ (ap \ (ap \ (ap \ V2M2 \ V8t1) \ V6l) \ V9t2)))))))))) \wedge ((\\ & \quad p \ (ap \ (ap \ (c.2Epath_2Eokpath \ A.27a \ A.27c) \ V1M1) \ V3p)) \wedge (p \ (ap \ (ap \\ & \quad V0R \ (ap \ (c.2Epath_2Efirst \ A.27a \ A.27c) \ V3p)) \ V4t_init)))))) \Rightarrow (\exists V10q \in \\ & \quad (ty_2Epath_2Epath \ A.27b \ A.27c).((p \ (ap \ (ap \ (c.2Epath_2Eokpath \\ & \quad A.27b \ A.27c) \ V2M2) \ V10q)) \wedge (((ap \ (c.2Epath_2Elabels \ A.27a \ A.27c) \\ & \quad V3p) = (ap \ (c.2Epath_2Elabels \ A.27b \ A.27c) \ V10q)) \wedge ((ap \ (c.2Epath_2Efirst \\ & \quad A.27b \ A.27c) \ V10q) = V4t_init)))))))))) \end{aligned}$$