

# thm\_2EpatternMatches\_2EPMATCH\_ROWS\_DROP\_REDUNDA (TMcRnGw98kKVB1ghpp3bDj6F28e94Zh2Vqc)

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**Definition 1** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 2** We define  $c\_2Ebool\_2E\_2T$  to be  $(ap (ap (c\_2Emin\_2E\_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

**Definition 3** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A\_27a : \iota.(\lambda V0P \in (2^{A\_27a}).(ap (ap (c\_2Emin\_2E\_3D (2^{A\_27a}))$

**Definition 4** We define  $c\_2Ebool\_2E\_2F$  to be  $(ap (c\_2Ebool\_2E\_21 2) (\lambda V0t \in 2.V0t))$ .

**Definition 5** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p P \Rightarrow p Q)$  of type  $\iota$ .

**Definition 6** We define  $c\_2Ebool\_2E\_27E$  to be  $(\lambda V0t \in 2.(ap (ap c\_2Emin\_2E\_3D\_3D\_3E V0t) c\_2Ebool\_2E\_2F$

Let  $ty\_2Eoption\_2Eoption : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty\_2Eoption\_2Eoption A0) \quad (1)$$

Let  $ty\_2Elist\_2Elist : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty\_2Elist\_2Elist A0) \quad (2)$$

Let  $c\_2EpatternMatches\_2EPMATCH : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow \forall A\_27b.nonempty A\_27b \Rightarrow c\_2EpatternMatches\_2EPMATCH A\_27a A\_27b \in ((A\_27a^{(ty\_2Elist\_2Elist ((ty\_2Eoption\_2Eoption A\_27a)^{A\_27b}))})^{A\_27b}) \quad (3)$$

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty ty\_2Enum\_2Enum \quad (4)$$

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \quad (5)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega^{\omega}}) \quad (6)$$

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{\omega^{\omega}}) \quad (7)$$

**Definition 7** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum. (ap\ c\_2Enum\_2EABS\_num)$

Let  $c\_2Elist\_2ETAKE : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Elist\_2ETAKE\ A\_27a \in (((ty\_2Elist\_2Elist\ A\_27a)^{(ty\_2Elist\_2Elist\ A\_27a)})^{ty\_2Enum\_2Enum}) \quad (8)$$

Let  $c\_2Eoption\_2EIS\_SOME : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Eoption\_2EIS\_SOME\ A\_27a \in (2^{(ty\_2Eoption\_2Eoption\ A\_27a)}) \quad (9)$$

Let  $c\_2Elist\_2ELIST\_TO\_SET : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Elist\_2ELIST\_TO\_SET\ A\_27a \in ((2^{A\_27a})^{(ty\_2Elist\_2Elist\ A\_27a)}) \quad (10)$$

**Definition 8** We define  $c\_2Ebool\_2EIN$  to be  $\lambda A\_27a : \iota. (\lambda V0x \in A\_27a. (\lambda V1f \in (2^{A\_27a}). (ap\ V1f\ V0x)))$

**Definition 9** We define  $c\_2Ebool\_2E2F\_5C$  to be  $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap\ (c\_2Ebool\_2E21\ 2)\ (\lambda V2t \in 2))))$

**Definition 10** We define  $c\_2Emin\_2E40$  to be  $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. P\ x) \text{ then } (the\ (\lambda x. x \in A) \text{ of type } \iota \Rightarrow \iota).$

**Definition 11** We define  $c\_2Ebool\_2E3F$  to be  $\lambda A\_27a : \iota. (\lambda V0P \in (2^{A\_27a}). (ap\ V0P\ (ap\ (c\_2Emin\_2E40))))$

**Definition 12** We define  $c\_2EpatternMatches\_2EPMATCH\_EQUIV\_ROWS$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0v \in A\_27a. \lambda V1rows1 \in (ty\_2Elist\_2Elist\ ((ty\_2Eoption\_2Eoption\ A\_27b)^{A\_27a}))$

Let  $c\_2Elist\_2EEL : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Elist\_2EEL\ A\_27a \in ((A\_27a)^{(ty\_2Elist\_2Elist\ A\_27a)})^{ty\_2Enum\_2Enum} \quad (11)$$

Let  $c\_2Elist\_2ELENGTH : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow c\_2Elist\_2ELENGTH\ A\_27a \in (ty\_2Enum\_2Enum)^{(ty\_2Elist\_2Elist\ A\_27a)} \quad (12)$$

**Definition 13** We define  $c\_2Eprim\_rec\_2E3C$  to be  $\lambda V0m \in ty\_2Enum\_2Enum. \lambda V1n \in ty\_2Enum\_2Enum$

Assume the following.

$$True \quad (13)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \wedge True) \Leftrightarrow \\ & (p \ V0t)) \wedge (((False \wedge (p \ V0t)) \Leftrightarrow False) \wedge (((p \ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p \ V0t) \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)))))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p \ V0t)) \wedge (((False \Leftrightarrow (p \ V0t)) \Leftrightarrow \neg(p \ V0t)) \wedge (((p \ V0t) \Leftrightarrow False) \Leftrightarrow \neg( \\ & p \ V0t)))))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty \ A\_27a \Rightarrow \forall A\_27b.nonempty \ A\_27b \Rightarrow ( \\ & \forall V0v \in A\_27a.(\forall V1rows1 \in (ty\_2Elist\_2Elist \ ((ty\_2Eoption\_2Eoption \\ & A\_27b)^{A\_27a})).(\forall V2rows2 \in (ty\_2Elist\_2Elist \ ((ty\_2Eoption\_2Eoption \\ & A\_27b)^{A\_27a})).((p \ (ap \ (ap \ (ap \ (c\_2EpatternMatches\_2EPMATCH\_EQUIV\_ROWS \\ & A\_27a \ A\_27b) \ V0v) \ V1rows1) \ V2rows2)) \Rightarrow ((ap \ (ap \ (c\_2EpatternMatches\_2EPMATCH \\ & A\_27b \ A\_27a) \ V0v) \ V1rows1) = (ap \ (ap \ (c\_2EpatternMatches\_2EPMATCH \\ & A\_27b \ A\_27a) \ V0v) \ V2rows2)))))) \end{aligned} \quad (16)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty \ A\_27a \Rightarrow \forall A\_27b.nonempty \ A\_27b \Rightarrow ( \\ & \forall V0v \in A\_27a.(\forall V1rows \in (ty\_2Elist\_2Elist \ ((ty\_2Eoption\_2Eoption \\ & A\_27b)^{A\_27a})).(\forall V2n \in ty\_2Enum\_2Enum.(((p \ (ap \ (ap \ c\_2Eprim\_rec\_2E\_3C \\ & V2n) \ (ap \ (c\_2Elist\_2ELENGTH \ ((ty\_2Eoption\_2Eoption \ A\_27b)^{A\_27a})) \\ & V1rows))) \wedge (p \ (ap \ (c\_2Eoption\_2EIS\_SOME \ A\_27b) \ (ap \ (ap \ (ap \ (c\_2Elist\_2EEL \\ & ((ty\_2Eoption\_2Eoption \ A\_27b)^{A\_27a})) \ V2n) \ V1rows) \ V0v)))) \Rightarrow ( \\ & p \ (ap \ (ap \ (ap \ (c\_2EpatternMatches\_2EPMATCH\_EQUIV\_ROWS \ A\_27a \\ & A\_27b) \ V0v) \ V1rows) \ (ap \ (ap \ (c\_2Elist\_2ETAKE \ ((ty\_2Eoption\_2Eoption \\ & A\_27b)^{A\_27a})) \ (ap \ c\_2Enum\_2ESUC \ V2n)) \ V1rows)))))) \end{aligned} \quad (17)$$

### Theorem 1

$$\begin{aligned} & \forall A\_27a.nonempty \ A\_27a \Rightarrow \forall A\_27b.nonempty \ A\_27b \Rightarrow ( \\ & \forall V0v \in A\_27a.(\forall V1rows \in (ty\_2Elist\_2Elist \ ((ty\_2Eoption\_2Eoption \\ & A\_27b)^{A\_27a})).(\forall V2n \in ty\_2Enum\_2Enum.(((p \ (ap \ (ap \ c\_2Eprim\_rec\_2E\_3C \\ & V2n) \ (ap \ (c\_2Elist\_2ELENGTH \ ((ty\_2Eoption\_2Eoption \ A\_27b)^{A\_27a})) \\ & V1rows))) \wedge (p \ (ap \ (c\_2Eoption\_2EIS\_SOME \ A\_27b) \ (ap \ (ap \ (ap \ (c\_2Elist\_2EEL \\ & ((ty\_2Eoption\_2Eoption \ A\_27b)^{A\_27a})) \ V2n) \ V1rows) \ V0v)))) \Rightarrow ( \\ & (ap \ (ap \ (c\_2EpatternMatches\_2EPMATCH \ A\_27b \ A\_27a) \ V0v) \ V1rows) = \\ & (ap \ (ap \ (c\_2EpatternMatches\_2EPMATCH \ A\_27b \ A\_27a) \ V0v) \ (ap \ (ap \\ & (c\_2Elist\_2ETAKE \ ((ty\_2Eoption\_2Eoption \ A\_27b)^{A\_27a})) \ (ap \ c\_2Enum\_2ESUC \\ & V2n)) \ V1rows)))))) \end{aligned}$$