

Let $c_2Erealax_2Etrealmul : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealmul \in (((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)))(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal) \quad (5)$$

Let $c_2Erealax_2Etrealmul : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealmul \in ((2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)})(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)) \quad (6)$$

Let $c_2Erealax_2Ereal_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_ABS_CLASS \in (ty_2Erealax_2Ereal)^{(2^{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}}) \quad (7)$$

Definition 7 We define $c_2Erealax_2Ereal_ABS$ to be $\lambda V0r \in (ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)$

Definition 8 We define $c_2Erealax_2Ereal_mul$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.\lambda V1T2 \in ty_2Erealax_2Ereal$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Elist_2Elist\ A0) \quad (8)$$

Let $c_2Epoly_2Epoly_mul : \iota$ be given. Assume the following.

$$c_2Epoly_2Epoly_mul \in (((ty_2Elist_2Elist\ ty_2Erealax_2Ereal)(ty_2Elist_2Elist\ ty_2Erealax_2Ereal)(ty_2Elist_2Elist\ ty_2Erealax_2Ereal)))(ty_2Elist_2Elist\ ty_2Erealax_2Ereal) \quad (9)$$

Let $c_2Epoly_2Epoly : \iota$ be given. Assume the following.

$$c_2Epoly_2Epoly \in ((ty_2Erealax_2Ereal^{ty_2Erealax_2Ereal})(ty_2Elist_2Elist\ ty_2Erealax_2Ereal)) \quad (10)$$

Definition 9 We define c_2Ebool_2E3F to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}).(ap\ V0P\ (ap\ (c_2Emin_2E40\ A_27a\ V0P))))$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \quad (11)$$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (12)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (13)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (14)$$

Definition 10 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num\ V0m)$

Definition 11 We define c_Ebool_EF to be $(ap (c_Ebool_E21 2) (\lambda V0t \in 2.V0t))$.

Definition 12 We define c_Ebool_E7E to be $(\lambda V0t \in 2.(ap (ap c_Emin_E3D_3D_3E V0t) c_Ebool_E21 2))$.

Let $c_Elist_ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_Elist_ENIL A_27a \in (ty_Elist_Elist A_27a) \quad (15)$$

Let $c_Eenum_EZERO_REP : \iota$ be given. Assume the following.

$$c_Eenum_EZERO_REP \in \omega \quad (16)$$

Definition 13 We define c_Eenum_E0 to be $(ap c_Eenum_EABS_num c_Eenum_EZERO_REP)$.

Definition 14 We define $c_Earithmetic_EZERO$ to be c_Eenum_E0 .

Let $c_Earithmetic_E2B : \iota$ be given. Assume the following.

$$c_Earithmetic_E2B \in ((ty_Eenum_Eenum^{ty_Eenum_Eenum})^{ty_Eenum_Eenum}) \quad (17)$$

Definition 15 We define $c_Earithmetic_EBIT1$ to be $\lambda V0n \in ty_Eenum_Eenum.(ap (ap c_Earithmetic_E2B V0n) c_Eenum_E0)$.

Definition 16 We define $c_Earithmetic_ENUMERAL$ to be $\lambda V0x \in ty_Eenum_Eenum.V0x$.

Let $c_Ereal_Ereal_of_num : \iota$ be given. Assume the following.

$$c_Ereal_Ereal_of_num \in (ty_Erealax_Ereal^{ty_Eenum_Eenum}) \quad (18)$$

Let $c_Erealax_Etrealm_neg : \iota$ be given. Assume the following.

$$c_Erealax_Etrealm_neg \in ((ty_Epair_Eprod ty_Ehreal_Ehreal ty_Ehreal_Ehreal)^{(ty_Epair_Eprod ty_Ehreal_Ehreal ty_Ehreal_Ehreal)}) \quad (19)$$

Definition 17 We define $c_Erealax_Ereal_neg$ to be $\lambda V0T1 \in ty_Erealax_Ereal.(ap c_Erealax_Ereal c_Etrealm_neg T1)$.

Let $c_Elist_ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_Elist_ECONS A_27a \in (((ty_Elist_Elist A_27a)^{(ty_Elist_Elist A_27a)})^{A_27a}) \quad (20)$$

Let $c_Epoly_Epoly_exp : \iota$ be given. Assume the following.

$$c_Epoly_Epoly_exp \in (((ty_Elist_Elist ty_Erealax_Ereal)^{ty_Eenum_Eenum})^{(ty_Elist_Elist ty_Erealax_Ereal)}) \quad (21)$$

Definition 18 We define $c_Epoly_Epoly_divides$ to be $\lambda V0p1 \in (ty_Elist_Elist ty_Erealax_Ereal).$

Definition 19 We define $c_Ebool_E2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_Ebool_E21 2) (\lambda V2t \in 2.V2t))))$.

Definition 20 We define $c_2Epoly_2Epoly_order$ to be $\lambda V0a \in ty_2Erealax_2Ereal.\lambda V1p \in (ty_2Elist_2E$

Assume the following.

$$True \tag{22}$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \tag{23}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \tag{24}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow (\forall V0f \in (A_27b^{A_27a}).(\forall V1g \in (A_27b^{A_27a}).((\forall V2x \in A_27a.((ap V0f V2x) = (ap V1g V2x)) \Rightarrow (V0f = V1g)))))) \tag{25}$$

Assume the following.

$$(\forall V0x \in ty_2Erealax_2Ereal.(\forall V1p1 \in (ty_2Elist_2Elist ty_2Erealax_2Ereal).(\forall V2p2 \in (ty_2Elist_2Elist ty_2Erealax_2Ereal).((ap (ap c_2Epoly_2Epoly (ap (ap c_2Epoly_2Epoly_mul V1p1) V2p2)) V0x) = (ap (ap c_2Erealax_2Ereal_mul (ap (ap c_2Epoly_2Epoly V1p1) V0x)) (ap (ap c_2Epoly_2Epoly V2p2) V0x))))))) \tag{26}$$

Theorem 1

$$(\forall V0p \in (ty_2Elist_2Elist ty_2Erealax_2Ereal).(\forall V1q \in (ty_2Elist_2Elist ty_2Erealax_2Ereal).(\forall V2a \in ty_2Erealax_2Ereal.(((ap c_2Epoly_2Epoly V0p) = (ap c_2Epoly_2Epoly V1q)) \Rightarrow ((ap (ap c_2Epoly_2Epoly_order V2a) V0p) = (ap (ap c_2Epoly_2Epoly_order V2a) V1q)))))))$$