

Definition 10 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.$ **if** $(\exists x \in A.p (ap P x))$ **then** (the $(\lambda x.x \in A \wedge p (ap P x))$ of type $\iota \Rightarrow \iota$).

Definition 11 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_40$

Definition 12 We define $c_2Epred_set_2EBIGUNION$ to be $\lambda A_27a : \iota.\lambda V0P \in (2^{(2^{A_27a})}).(ap (c_2Epred_set_2EBIGUNION$

Assume the following.

$$True \tag{4}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A_27a.(p V0t)) \Leftrightarrow (p V0t))) \tag{5}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \tag{6}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0P \in (2^{A_27a}).(\forall V1Q \in (2^{A_27a}).((\exists V2x \in A_27a.((p (ap V0P V2x)) \vee (p (ap V1Q V2x)))) \Leftrightarrow ((\exists V3x \in A_27a.(p (ap V0P V3x))) \vee (\exists V4x \in A_27a.(p (ap V1Q V4x)))))))) \tag{7}$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(\forall V2C \in 2.(((p V0A) \wedge ((p V1B) \vee (p V2C))) \Leftrightarrow (((p V0A) \wedge (p V1B)) \vee ((p V0A) \wedge (p V2C))))))) \tag{8}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0s \in (2^{A_27a}).(\forall V1t \in (2^{A_27a}).((V0s = V1t) \Leftrightarrow (\forall V2x \in A_27a.((p (ap (ap (c_2Ebool_2EIN A_27a) V2x) V0s)) \Leftrightarrow (p (ap (ap (c_2Ebool_2EIN A_27a) V2x) V1t))))))) \tag{9}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0s \in (2^{A_27a}).(\forall V1t \in (2^{A_27a}).(\forall V2x \in A_27a.((p (ap (ap (c_2Ebool_2EIN A_27a) V2x) (ap (ap (c_2Epred_set_2EUNION A_27a) V0s) V1t))) \Leftrightarrow ((p (ap (ap (c_2Ebool_2EIN A_27a) V2x) V0s)) \vee (p (ap (ap (c_2Ebool_2EIN A_27a) V2x) V1t))))))) \tag{10}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1sos \in (2^{(2^{A_27a})}).((p (ap (ap (c_2Ebool_2EIN A_27a) V0x) (ap (c_2Epred_set_2EBIGUNION A_27a) V1sos))) \Leftrightarrow (\exists V2s \in (2^{A_27a}).((p (ap (ap (c_2Ebool_2EIN A_27a) V0x) V2s)) \wedge (p (ap (ap (c_2Ebool_2EIN (2^{A_27a}) V2s) V1sos))))))) \tag{11}$$

Theorem 1

$$\begin{aligned} & \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0s1 \in (2^{(2^A-27a)}). (\\ & \quad \forall V1s2 \in (2^{(2^A-27a)}). ((ap\ (c.2Epred_set_2EBIGUNION \\ & \quad A.27a)\ (ap\ (ap\ (c.2Epred_set_2EUNION\ (2^A-27a))\ V0s1)\ V1s2)) = \\ & (ap\ (ap\ (c.2Epred_set_2EUNION\ A.27a)\ (ap\ (c.2Epred_set_2EBIGUNION \\ & \quad A.27a)\ V0s1))\ (ap\ (c.2Epred_set_2EBIGUNION\ A.27a)\ V1s2)))) \end{aligned}$$