



**Definition 8** We define  $c\_2Epair\_2EUNCURRY$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda A\_27c : \iota.\lambda V0f \in ((A\_27c)^{A\_27b})$ . Let  $c\_2Epred\_set\_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epred\_set\_2EGSPEC\ A\_27a\ A\_27b \in ((2^{A\_27a})^{((ty\_2Epair\_2Eprod\ A\_27a\ 2)^{A\_27b})}) \quad (5)$$

Assume the following.

$$True \quad (6)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow True)) \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow \forall A\_27c. \\ & \quad nonempty\ A\_27c \Rightarrow (\forall V0f \in ((A\_27c)^{A\_27b})^{A\_27a}).(\forall V1x \in \\ & \quad A\_27a.(\forall V2y \in A\_27b.((ap\ (ap\ (c\_2Epair\_2EUNCURRY\ A\_27a \\ & \quad A\_27b\ A\_27c)\ V0f)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ A\_27a\ A\_27b)\ V1x)\ V2y))) = \\ & \quad (ap\ (ap\ V0f\ V1x)\ V2y)))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in (2^{A\_27a}).(\forall V1x \in A\_27a.((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a)\ V1x)\ V0P)) \Leftrightarrow (p\ (ap\ V0P\ V1x)))))) \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0P \in ((2^{A\_27b})^{A\_27a}).((ap\ (c\_2Epred\_set\_2EGSPEC\ ( \\ & \quad ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)\ (ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)) \\ & \quad (ap\ (c\_2Epair\_2EUNCURRY\ A\_27a\ A\_27b\ (ty\_2Epair\_2Eprod\ (ty\_2Epair\_2Eprod \\ & \quad A\_27a\ A\_27b)\ 2))\ (\lambda V1x \in A\_27a.(\lambda V2y \in A\_27b.(ap\ (ap\ (c\_2Epair\_2E\_2C \\ & \quad (ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)\ 2)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ A\_27a \\ & \quad A\_27b)\ V1x)\ V2y))\ (ap\ (ap\ V0P\ V1x)\ V2y)))))) = (ap\ (c\_2Epair\_2EUNCURRY \\ & \quad A\_27a\ A\_27b\ 2)\ V0P))) \end{aligned} \quad (10)$$

**Theorem 1**

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0x \in A\_27a.(\forall V1y \in A\_27b.(\forall V2P \in ((2^{A\_27b})^{A\_27a}). \\ & \quad ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Epair\_2Eprod\ A\_27a\ A\_27b))\ (ap \\ & \quad (ap\ (c\_2Epair\_2E\_2C\ A\_27a\ A\_27b)\ V0x)\ V1y))\ (ap\ (c\_2Epred\_set\_2EGSPEC \\ & \quad (ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)\ (ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)) \\ & \quad (ap\ (c\_2Epair\_2EUNCURRY\ A\_27a\ A\_27b\ (ty\_2Epair\_2Eprod\ (ty\_2Epair\_2Eprod \\ & \quad A\_27a\ A\_27b)\ 2))\ (\lambda V3x \in A\_27a.(\lambda V4y \in A\_27b.(ap\ (ap\ (c\_2Epair\_2E\_2C \\ & \quad (ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)\ 2)\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ A\_27a \\ & \quad A\_27b)\ V3x)\ V4y))\ (ap\ (ap\ V2P\ V3x)\ V4y)))))) \Leftrightarrow (p\ (ap\ (ap\ V2P\ V0x) \\ & \quad V1y)))))) \end{aligned}$$