

thm_2Epred_set_EPSUBSET_TRANS (TMSbrdD8D7LKAw24LBfS8tpGv44bbvUVP8s)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E_3D (2^{A_27a}))$

Definition 4 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2EF$

Definition 7 We define c_2Ebool_2EIN to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.(\lambda V1f \in (2^{A_27a}).(ap V1f V0x)))$

Definition 8 We define $c_2Epred_set_2ESUBSET$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap (c$

Definition 9 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2$

Definition 10 We define $c_2Epred_set_2EPSUBSET$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p V0t))) \tag{1}$$

Assume the following.

$$(\forall V0t \in 2.((\neg(p V0t)) \Rightarrow ((p V0t) \Rightarrow False))) \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty A_27a \Rightarrow (\forall V0s \in (2^{A_27a}).(\forall V1t \in \\ & (2^{A_27a}).(\forall V2u \in (2^{A_27a}).(((p (ap (ap (c_2Epred_set_2ESUBSET \\ & A_27a) V0s) V1t)) \wedge (p (ap (ap (c_2Epred_set_2ESUBSET A_27a) V1t) \\ & V2u))) \Rightarrow (p (ap (ap (c_2Epred_set_2ESUBSET A_27a) V0s) V2u)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0s \in (2^{A_{.27a}}).(\forall V1t \in \\ & (2^{A_{.27a}}).(((p\ (ap\ (ap\ (c_{.2Epred_set_2ESUBSET}\ A_{.27a})\ V0s)\ V1t)) \wedge \\ & (p\ (ap\ (ap\ (c_{.2Epred_set_2ESUBSET}\ A_{.27a})\ V1t)\ V0s))) \Rightarrow (V0s = V1t)))) \end{aligned} \quad (4)$$

Theorem 1

$$\begin{aligned} & \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0s \in (2^{A_{.27a}}).(\forall V1t \in \\ & (2^{A_{.27a}}).(\forall V2u \in (2^{A_{.27a}}).(((p\ (ap\ (ap\ (c_{.2Epred_set_2EPSUBSET}\ A_{.27a})\ V0s)\ V1t)) \wedge (p\ (ap\ (ap\ (c_{.2Epred_set_2EPSUBSET}\ A_{.27a})\ V1t)\ V2u))) \Rightarrow (p\ (ap\ (ap\ (c_{.2Epred_set_2EPSUBSET}\ A_{.27a})\ V0s)\ V2u)))))) \end{aligned}$$