

thm_2Eprobability_2Ejoint__distribution__sum__mul1 (TMLTbtV1qPuLHAMTe47ikhHtwYg9s7QKv9s)

October 26, 2020

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Ebool_2E_2ET$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_2E21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E_3D (2^{A_27a}))$

Definition 4 We define $c_2Emarker_2E_2EAbbrev$ to be $\lambda V0x \in 2.V0x$.

Definition 5 We define $c_2Emin_2E_2E40$ to be $\lambda A.\lambda P \in 2^A.if (\exists x \in A.p (ap P x))$ then (the $(\lambda x.x \in A \wedge p (ap P x))$ of type $\iota \Rightarrow \iota$.

Definition 6 We define $c_2Ebool_2E_2E3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_2Emin_2E_2E40 A_27a) P))$

Let $ty_2Epair_2E_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty_2Epair_2E_2Eprod A0 A1) \tag{1}$$

Let $c_2Epair_2E_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2E_2ESND A_27a A_27b \in (A_27b^{(ty_2Epair_2E_2Eprod A_27a A_27b)}) \tag{2}$$

Let $c_2Epair_2E_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2E_2EFST A_27a A_27b \in (A_27a^{(ty_2Epair_2E_2Eprod A_27a A_27b)}) \tag{3}$$

Definition 7 We define $c_2Epair_2E_2EUNCURRY$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in ((A_27c^{A_27b}) \Rightarrow A_27a)$

Definition 8 We define $c_2Emin_2E_2E3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 9 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21\ 2) (\lambda V2t \in 2.$

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2EABS_prod \\ A_27a\ A_27b \in ((ty_2Epair_2Eprod\ A_27a\ A_27b)^{(2^{A_27b}})^{A_27a}) \end{aligned} \quad (4)$$

Definition 10 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in A_27a.\lambda V1y \in A_27b.(ap (c_2E$

Definition 11 We define c_2Ebool_2EIN to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.(\lambda V1f \in (2^{A_27a}).(ap\ V1f\ V0x)))$

Let $c_2Epred_set_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epred_set_2EGSPEC \\ A_27a\ A_27b \in ((2^{A_27a})^{(ty_2Epair_2Eprod\ A_27a\ 2)^{A_27b}}) \end{aligned} \quad (5)$$

Definition 12 We define $c_2Epred_set_2EIMAGE$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b^{A_27a}).\lambda V1s \in$

Definition 13 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21\ 2) (\lambda V0t \in 2.V0t))$.

Definition 14 We define $c_2Epred_set_2EEMPTY$ to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.c_2Ebool_2EF)$.

Definition 15 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21\ 2) (\lambda V2t \in 2.$

Definition 16 We define $c_2Epred_set_2EINSERT$ to be $\lambda A_27a : \iota.\lambda V0x \in A_27a.\lambda V1s \in (2^{A_27a}).(ap (c_2E$

Let $ty_2Erealax_2Ereal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Erealax_2Ereal \quad (6)$$

Let $c_2Emeasure_2Em_space : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow c_2Emeasure_2Em_space\ A_27a \in \\ ((2^{A_27a})^{(ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2Epair_2Eprod\ (2^{(2^{A_27a})})\ (ty_2Erealax_2Ereal^{(2^{A_27a})})))) \end{aligned} \quad (7)$$

Definition 17 We define $c_2Eprobability_2Ep_space$ to be $\lambda A_27a : \iota.(c_2Emeasure_2Em_space\ A_27a)$.

Definition 18 We define $c_2Epred_set_2EPREIMAGE$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b^{A_27a}).\lambda V$

Definition 19 We define $c_2Epred_set_2EINTER$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap (c_2E$

Let $c_2Emeasure_2Emeasure : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow c_2Emeasure_2Emeasure\ A_27a \in (\\ (ty_2Erealax_2Ereal^{(2^{A_27a})})^{(ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2Epair_2Eprod\ (2^{(2^{A_27a})})\ (ty_2Erealax_2Ereal^{(2^{A_27a})}))) \end{aligned} \quad (8)$$

Definition 20 We define $c_2Eprobability_2Eprob$ to be $\lambda A_27a : \iota.(c_2Emeasure_2Emeasure A_27a)$.

Definition 21 We define $c_2Eprobability_2Ejoint_distribution$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0p \in$

Definition 22 We define $c_2Eprobability_2Edistribution$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0p \in (ty_2Epair_2Eprod$

Definition 23 We define $c_2Epred_set_2ESUBSET$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A-27a}).\lambda V1t \in (2^{A-27a}).(ap$

Definition 24 We define $c_2Epred_set_2EPOW$ to be $\lambda A_27a : \iota.\lambda V0set \in (2^{A-27a}).(ap (c_2Epred_set_2Eprod$

Let $c_2Emeasure_2Emeasurable_sets : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty A_27a \Rightarrow c_2Emeasure_2Emeasurable_sets \\ A_27a \in & ((2^{(2^{A-27a})})^{(ty_2Epair_2Eprod (2^{A-27a}) (ty_2Epair_2Eprod (2^{(2^{A-27a})}) (ty_2Erealx_2Ereal^{(2^{A-27a})})))) \end{aligned} \quad (9)$$

Definition 25 We define $c_2Eprobability_2Eevents$ to be $\lambda A_27a : \iota.(c_2Emeasure_2Emeasurable_sets A_27a)$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (10)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty ty_2Enum_2Enum \quad (11)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (12)$$

Definition 26 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 27 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (13)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (14)$$

Definition 28 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap c_2Enum_2EABS_num$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (15)$$

Definition 29 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic$

Definition 30 We define $c_2Earithmic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $c_2Ereal_2Ereal_of_num : \iota$ be given. Assume the following.

$$c_2Ereal_2Ereal_of_num \in (ty_2Erealax_2Ereal^{ty_2Enum_2Enum}) \quad (16)$$

Definition 31 We define $c_2Epred_set_2EUNIV$ to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.c_2Ebool_2ET)$.

Definition 32 We define $c_2Epred_set_2EBIGUNION$ to be $\lambda A_27a : \iota.\lambda V0P \in (2^{(2^{A_27a})}).(ap (c_2Epred_set_2EUNIV) P)$.

Definition 33 We define $c_2Ecombin_2Eo$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in (A_27b^{A_27c}).\lambda V1g \in (A_27c^{A_27b}).(ap (c_2Ecombin_2Eo) f g)$.

Let $c_2Ereal_2Esum : \iota$ be given. Assume the following.

$$c_2Ereal_2Esum \in ((ty_2Erealax_2Ereal^{(ty_2Erealax_2Ereal^{ty_2Enum_2Enum})})^{(ty_2Epair_2Eprod ty_2Enum_2Enum)}) \quad (17)$$

Definition 34 We define c_2Ebool_2E7E to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E3D_3D_3E V0t) c_2Ebool_2ET))$.

Definition 35 We define $c_2Eprim_rec_2E3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(c_2Eprim_rec_2E3C m n)$.

Definition 36 We define $c_2Earithmic_2E3E$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(c_2Earithmic_2E3E m n)$.

Definition 37 We define $c_2Earithmic_2E3E_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(c_2Earithmic_2E3E_3D m n)$.

Let $ty_2Ehreal_2Ehreal : \iota$ be given. Assume the following.

$$nonempty\ ty_2Ehreal_2Ehreal \quad (18)$$

Let $c_2Erealax_2Ereal_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_REP_CLASS \in ((2^{(ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)})^{ty_2Erealax_2Ereal_REP_CLASS}) \quad (19)$$

Definition 38 We define $c_2Erealax_2Ereal_REP$ to be $\lambda V0a \in ty_2Erealax_2Ereal.(ap (c_2Emin_2E40 ty_2Erealax_2Ereal) a)$.

Let $c_2Erealax_2Etrealm_neg : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealm_neg \in ((ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)^{ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal}) \quad (20)$$

Let $c_2Erealax_2Etrealm_eq : \iota$ be given. Assume the following.

$$c_2Erealax_2Etrealm_eq \in ((2^{(ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)})^{ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal}) \quad (21)$$

Let $c_2Erealax_2Ereal_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Erealax_2Ereal_ABS_CLASS \in (ty_2Erealax_2Ereal^{(2^{(ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal)})}) \quad (22)$$

Definition 39 We define $c_2Erealax_2Ereal_ABS$ to be $\lambda V0r \in (ty_2Epair_2Eprod ty_2Ehreal_2Ehreal ty_2Ehreal_2Ehreal).(ap (c_2Erealax_2Ereal_ABS_CLASS) r)$.

Definition 40 We define $c_Erealax_Ereal_neg$ to be $\lambda V0T1 \in ty_Erealax_Ereal.(ap\ c_Erealax_Ereal$

Let $c_Erealax_Etrealm_add : \iota$ be given. Assume the following.

$$c_Erealax_Etrealm_add \in (((ty_Epair_Eprod\ ty_Ehreal_Ehreal\ ty_Ehreal_Ehreal)\ (ty_Epair_Eprod\ ty_Ehreal_Ehreal\ ty_Ehreal_Ehreal))\ (ty_Epair_Eprod\ ty_Ehreal_Ehreal\ ty_Ehreal_Ehreal))\ (ty_Epair_Eprod\ ty_Ehreal_Ehreal\ ty_Ehreal_Ehreal) \quad (23)$$

Definition 41 We define $c_Erealax_Ereal_add$ to be $\lambda V0T1 \in ty_Erealax_Ereal.\lambda V1T2 \in ty_Erealax_Ereal$

Definition 42 We define $c_Ereal_Ereal_sub$ to be $\lambda V0x \in ty_Erealax_Ereal.\lambda V1y \in ty_Erealax_Ereal$

Let $c_Erealax_Etrealm_lt : \iota$ be given. Assume the following.

$$c_Erealax_Etrealm_lt \in ((2\ (ty_Epair_Eprod\ ty_Ehreal_Ehreal\ ty_Ehreal_Ehreal))\ (ty_Epair_Eprod\ ty_Ehreal_Ehreal\ ty_Ehreal_Ehreal)) \quad (24)$$

Definition 43 We define $c_Erealax_Ereal_lt$ to be $\lambda V0T1 \in ty_Erealax_Ereal.\lambda V1T2 \in ty_Erealax_Ereal$

Definition 44 We define $c_Ereal_Ereal_lte$ to be $\lambda V0x \in ty_Erealax_Ereal.\lambda V1y \in ty_Erealax_Ereal$

Definition 45 We define c_Ebool_ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.$

Definition 46 We define c_Ereal_Eabs to be $\lambda V0x \in ty_Erealax_Ereal.(ap\ (ap\ (ap\ (c_Ebool_ECOND$

Let $ty_Emetric_Emetric : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_Emetric_Emetric\ A0) \quad (25)$$

Let $c_Emetric_Emetric : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Emetric_Emetric\ A_27a \in ((ty_Emetric_Emetric\ A_27a)\ (ty_Erealax_Ereal\ (ty_Epair_Eprod\ A_27a\ A_27a))) \quad (26)$$

Definition 47 We define $c_Emetric_Emr1$ to be $(ap\ (c_Emetric_Emetric\ ty_Erealax_Ereal)\ (ap\ (c_Emetric_Emetric$

Let $c_Emetric_Edist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Emetric_Edist\ A_27a \in ((ty_Erealax_Ereal\ (ty_Epair_Eprod\ A_27a\ A_27a))\ (ty_Emetric_Edist\ A_27a)) \quad (27)$$

Let $ty_Etopology_Etopology : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_Etopology_Etopology\ A0) \quad (28)$$

Let $c_Etopology_Etopology : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Etopology_Etopology\ A_27a \in ((ty_Etopology_Etopology\ A_27a)\ (2^{(2^{A_27a})})) \quad (29)$$

Definition 48 We define $c_Emetric_Emtop$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_Emetric_Emetric\ A_27a).(ap\ (c_Emetric_Emr1$

Let $c_2Enets_2Etends : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Enets_2Etends \\ & A_27a\ A_27b \in (((2^{(ty_2Epair_2Eprod\ (ty_2Etopology_2Etopology\ A_27a)\ (2^{A_27b})^{A_27b})}))_{A_27a})_{(A_27a)^{A_27b}} \end{aligned} \quad (30)$$

Definition 49 We define $c_2Eseq_2E_2D_2D_2E$ to be $\lambda V0x \in (ty_2Erealx_2Ereal^{ty_2Enum_2Enum}).\lambda V1x$

Definition 50 We define c_2Eseq_2Esums to be $\lambda V0f \in (ty_2Erealx_2Ereal^{ty_2Enum_2Enum}).\lambda V1s \in ty_2$

Definition 51 We define $c_2Epred_set_2EDISJOINT$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap$

Definition 52 We define $c_2Epred_set_2EFUNSET$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0P \in (2^{A_27a}).\lambda V1Q \in (2^{A_27b})$

Definition 53 We define $c_2Emeasure_2Ecountably_additive$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod$

Definition 54 We define $c_2Emeasure_2Epositive$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2$

Let $c_2Emeasure_2Esubsets : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow c_2Emeasure_2Esubsets\ A_27a \in (\\ & (2^{(2^{A_27a})})_{(ty_2Epair_2Eprod\ (2^{A_27a})\ (2^{(2^{A_27a})}))} \end{aligned} \quad (31)$$

Definition 55 We define $c_2Epred_set_2EINJ$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b)^{A_27a}.\lambda V1s \in (2^{A_27a})$

Definition 56 We define $c_2Epred_set_2Ecountable$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).(ap\ (c_2Ebool_2E_3F$

Definition 57 We define $c_2Epred_set_2EUNION$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap\ (c$

Let $c_2Emeasure_2Espace : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow c_2Emeasure_2Espace\ A_27a \in ((2^{A_27a})_{(ty_2Epair_2Eprod\ (2^{A_27a})\ (2^{(2^{A_27a})}))} \end{aligned} \quad (32)$$

Definition 58 We define $c_2Epred_set_2EDIFF$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1t \in (2^{A_27a}).(ap\ (c_2$

Definition 59 We define $c_2Emeasure_2Esubset_class$ to be $\lambda A_27a : \iota.\lambda V0sp \in (2^{A_27a}).\lambda V1sts \in (2^{(2^{A_27a})})$

Definition 60 We define $c_2Emeasure_2Ealgebra$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (2^{(2^{A_27a})})$

Definition 61 We define $c_2Emeasure_2Esigma_algebra$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (2^{(2^{A_27a})})$

Definition 62 We define $c_2Emeasure_2Emeasure_space$ to be $\lambda A_27a : \iota.\lambda V0m \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2$

Definition 63 We define $c_2Eprobability_2Eprob_space$ to be $\lambda A_27a : \iota.\lambda V0p \in (ty_2Epair_2Eprod\ (2^{A_27a})\ (ty_2$

Let $c_2Erealx_2Etrealmul : \iota$ be given. Assume the following.

$$\begin{aligned} & c_2Erealx_2Etrealmul \in (((ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal \\ & ty_2Ehreal_2Ehreal)_{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal\ ty_2Ehreal_2Ehreal)}_{(ty_2Epair_2Eprod\ ty_2Ehreal_2Ehreal)} \end{aligned} \quad (33)$$

Definition 64 We define $c_2Erealax_2Ereal_mul$ to be $\lambda V0T1 \in ty_2Erealax_2Ereal.\lambda V1T2 \in ty_2Erealax_2Ereal$

Definition 65 We define $c_2Epred_set_2ECROSS$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0P \in (2^{A_27a}).\lambda V1Q \in (2^{A_27b})$

Let $c_2Epred_set_2EITSET : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epred_set_2EITSET \\ A_27a\ A_27b \in (((A_27b^{A_27b})^{(2^{A_27a})})^{((A_27b^{A_27b})^{A_27a})}) \end{aligned} \quad (34)$$

Definition 66 We define $c_2Ereal_sigma_2EREAL_SUM_IMAGE$ to be $\lambda A_27a : \iota.\lambda V0f \in (ty_2Erealax_2Ereal)$

Definition 67 We define $c_2Epred_set_2EFINITE$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).(ap\ (c_2Ebool_2E21\ 2))$

Assume the following.

$$True \quad (35)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in \\ A_27a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \end{aligned} \quad (36)$$

Assume the following.

$$\begin{aligned} (\forall V0t \in 2.(((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (37)$$

Assume the following.

$$\begin{aligned} (\forall V0t \in 2.(((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow \\ True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge ((\\ (p\ V0t) \Rightarrow False) \Leftrightarrow (\neg (p\ V0t)))))) \end{aligned} \quad (38)$$

Assume the following.

$$\begin{aligned} ((\forall V0t \in 2.((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge \\ ((\neg False) \Leftrightarrow True))) \end{aligned} \quad (39)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.(V0x = V0x)) \quad (40)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (41)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in \\ A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \end{aligned} \quad (42)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0f \in (A_27b^{A_27a}).(\forall V1g \in (A_27b^{A_27a}).((V0f = \\ V1g) \Leftrightarrow (\forall V2x \in A_27a.((ap\ V0f\ V2x) = (ap\ V1g\ V2x)))))) \end{aligned} \quad (43)$$

Assume the following.

$$\begin{aligned} (\forall V0t \in 2.(((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg(\\ p\ V0t)))))) \end{aligned} \quad (44)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0Q \in 2.(\forall V1P \in (\\ 2^{A_27a}).((\forall V2x \in A_27a.((p\ (ap\ V1P\ V2x)) \vee (p\ V0Q))) \Leftrightarrow ((\forall V3x \in \\ A_27a.(p\ (ap\ V1P\ V3x)) \vee (p\ V0Q)))))) \end{aligned} \quad (45)$$

Assume the following.

$$\begin{aligned} (\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p\ V0t1) \Rightarrow \\ ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \end{aligned} \quad (46)$$

Assume the following.

$$\begin{aligned} (\forall V0x \in 2.(\forall V1x_27 \in 2.(\forall V2y \in 2.(\forall V3y_27 \in \\ 2.(((p\ V0x) \Leftrightarrow (p\ V1x_27)) \wedge ((p\ V1x_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y_27)))))) \Rightarrow \\ (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x_27) \Rightarrow (p\ V3y_27)))))) \end{aligned} \quad (47)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0x \in (ty_2Epair_2Eprod\ A_27a\ A_27b).(\exists V1q \in A_27a. \\ (\exists V2r \in A_27b.(V0x = (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b) \\ V1q)\ V2r)))))) \end{aligned} \quad (48)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0x \in (ty_2Epair_2Eprod\ A_27a\ A_27b).((ap\ (ap\ (c_2Epair_2E_2C \\ A_27a\ A_27b)\ (ap\ (c_2Epair_2EFST\ A_27a\ A_27b)\ V0x))\ (ap\ (c_2Epair_2ESND \\ A_27a\ A_27b)\ V0x)) = V0x)) \end{aligned} \quad (49)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0x \in A_27a.(\forall V1y \in A_27b.((ap\ (c_2Epair_2EFST\ A_27a \\ A_27b)\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V0x)\ V1y)) = V0x))) \end{aligned} \quad (50)$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow \forall A.27c. \\
& \quad nonempty\ A.27c \Rightarrow (\forall V0f \in ((A.27c^{A.27b})^{A.27a}). (\forall V1x \in \\
& \quad A.27a. (\forall V2y \in A.27b. ((ap\ (ap\ (c.2Epair_2EUNCURRY\ A.27a \\
& \quad A.27b\ A.27c)\ V0f)\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a\ A.27b)\ V1x)\ V2y))) = \\
& \quad (ap\ (ap\ V0f\ V1x)\ V2y))))))
\end{aligned} \tag{51}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow (\\
& \quad \forall V0s \in (2^{A.27a}). ((p\ (ap\ (c.2Epred_set_2EFINITE\ A.27a) \\
& \quad V0s)) \Rightarrow (\forall V1f \in (A.27b^{A.27a}). (p\ (ap\ (c.2Epred_set_2EFINITE \\
& \quad A.27b)\ (ap\ (ap\ (c.2Epred_set_2EIMAGE\ A.27a\ A.27b)\ V1f)\ V0s))))))
\end{aligned} \tag{52}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow (\\
& \quad \forall V0x \in A.27a. (\forall V1y \in A.27b. ((ap\ (ap\ (c.2Epred_set_2ECROSS \\
& \quad A.27a\ A.27b)\ (ap\ (ap\ (c.2Epred_set_2EINSERT\ A.27a)\ V0x)\ (c.2Epred_set_2EEMPTY \\
& \quad A.27a))))\ (ap\ (ap\ (c.2Epred_set_2EINSERT\ A.27b)\ V1y)\ (c.2Epred_set_2EEMPTY \\
& \quad A.27b)))) = (ap\ (ap\ (c.2Epred_set_2EINSERT\ (ty_2Epair_2Eprod \\
& \quad A.27a\ A.27b))\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a\ A.27b)\ V0x)\ V1y))\ (c.2Epred_set_2EEMPTY \\
& \quad (ty_2Epair_2Eprod\ A.27a\ A.27b))))))
\end{aligned} \tag{53}$$

Assume the following.

$$\begin{aligned}
& \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow \forall A.27c. \\
& \quad nonempty\ A.27c \Rightarrow (\forall V0p \in (ty_2Epair_2Eprod\ (2^{A.27a})\ (ty_2Epair_2Eprod \\
& \quad (2^{(2^{A.27a})})\ (ty_2Erealax_2Ereal^{(2^{A.27a})}))). (\forall V1X \in \\
& \quad (A.27b^{A.27a}). (\forall V2Y \in (A.27c^{A.27a}). (\forall V3a \in (2^{A.27b}). \\
& \quad (((p\ (ap\ (c.2Eprobability_2Eprob_space\ A.27a)\ V0p)) \wedge ((p\ (ap \\
& \quad (c.2Epred_set_2EFINITE\ A.27a)\ (ap\ (c.2Eprobability_2Ep_space \\
& \quad A.27a)\ V0p))) \wedge ((ap\ (c.2Eprobability_2Eevents\ A.27a)\ V0p) = (ap \\
& \quad (c.2Epred_set_2EPOW\ A.27a)\ (ap\ (c.2Eprobability_2Ep_space \\
& \quad A.27a)\ V0p)))))) \Rightarrow ((ap\ (ap\ (ap\ (c.2Eprobability_2Edistribution \\
& \quad A.27b\ A.27a)\ V0p)\ V1X)\ V3a) = (ap\ (ap\ (c.2Ereal_sigma_2EREAL_SUM_IMAGE \\
& \quad A.27c)\ (\lambda V4x \in A.27c. (ap\ (ap\ (ap\ (ap\ (c.2Eprobability_2Ejoint_distribution \\
& \quad A.27b\ A.27c\ A.27a)\ V0p)\ V1X)\ V2Y)\ (ap\ (ap\ (c.2Epred_set_2ECROSS \\
& \quad A.27b\ A.27c)\ V3a)\ (ap\ (ap\ (c.2Epred_set_2EINSERT\ A.27c)\ V4x)\ (\\
& \quad c.2Epred_set_2EEMPTY\ A.27c))))))\ (ap\ (ap\ (c.2Epred_set_2EIMAGE \\
& \quad A.27a\ A.27c)\ V2Y)\ (ap\ (c.2Eprobability_2Ep_space\ A.27a)\ V0p)))))))))
\end{aligned} \tag{54}$$

Assume the following.

$$\begin{aligned}
& (\forall V0x \in ty_2Erealax_2Ereal. (\forall V1y \in ty_2Erealax_2Ereal. \\
& ((ap\ (ap\ c.2Erealax_2Ereal_mul\ V0x)\ V1y) = (ap\ (ap\ c.2Erealax_2Ereal_mul \\
& \quad V1y)\ V0x))))
\end{aligned} \tag{55}$$

Assume the following.

$$\begin{aligned} & \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0P \in (2^{A_{.27a}}).((p\ (ap \\ & (c_{.2}Epred_set_2EFINITE\ A_{.27a})\ V0P)) \Rightarrow (\forall V1f \in (ty_{.2}Erealax_{.2}Ereal^{A_{.27a}}). \\ & (\forall V2c \in ty_{.2}Erealax_{.2}Ereal.((ap\ (ap\ (c_{.2}Ereal_sigma_2EREAL_SUM_IMAGE \\ & A_{.27a})\ (\lambda V3x \in A_{.27a}.(ap\ (ap\ c_{.2}Erealax_{.2}Ereal_mul\ V2c)\ (ap \\ & V1f\ V3x))))\ V0P) = (ap\ (ap\ c_{.2}Erealax_{.2}Ereal_mul\ V2c)\ (ap\ (ap\ (c_{.2}Ereal_sigma_2EREAL_SUM_IMAGE \\ & A_{.27a})\ V1f)\ V0P)))))) \end{aligned} \quad (56)$$

Assume the following.

$$\begin{aligned} & \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow (\\ & \forall V0s \in (2^{A_{.27a}}).(\forall V1s_{.27} \in (2^{A_{.27b}}).(\forall V2f \in \\ & ((ty_{.2}Erealax_{.2}Ereal^{A_{.27b}})^{A_{.27a}}).(((p\ (ap\ (c_{.2}Epred_set_2EFINITE \\ & A_{.27a})\ V0s)) \wedge (p\ (ap\ (c_{.2}Epred_set_2EFINITE\ A_{.27b})\ V1s_{.27}))) \Rightarrow \\ & ((ap\ (ap\ (c_{.2}Ereal_sigma_2EREAL_SUM_IMAGE\ A_{.27a})\ (\lambda V3x \in \\ & A_{.27a}.(ap\ (ap\ (c_{.2}Ereal_sigma_2EREAL_SUM_IMAGE\ A_{.27b})\ (ap \\ & V2f\ V3x))\ V1s_{.27})))\ V0s) = (ap\ (ap\ (c_{.2}Ereal_sigma_2EREAL_SUM_IMAGE \\ & (ty_{.2}Epair_{.2}Eprod\ A_{.27a}\ A_{.27b}))\ (\lambda V4x \in (ty_{.2}Epair_{.2}Eprod \\ & A_{.27a}\ A_{.27b}).(ap\ (ap\ V2f\ (ap\ (c_{.2}Epair_{.2}EFST\ A_{.27a}\ A_{.27b})\ V4x))) \\ & (ap\ (c_{.2}Epair_{.2}ESND\ A_{.27a}\ A_{.27b})\ V4x))))\ (ap\ (ap\ (c_{.2}Epred_set_2ECROSS \\ & A_{.27a}\ A_{.27b})\ V0s)\ V1s_{.27})))))) \end{aligned} \quad (57)$$

Assume the following.

$$(\forall V0t \in 2.((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \quad (58)$$

Assume the following.

$$(\forall V0A \in 2.((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \quad (59)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2.(\forall V1B \in 2.(((\neg((p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\ & (((p\ V0A) \Rightarrow False) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))))) \end{aligned} \quad (60)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2.(\forall V1B \in 2.(((\neg((\neg(p\ V0A)) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\ & ((p\ V0A) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))))) \end{aligned} \quad (61)$$

Assume the following.

$$(\forall V0A \in 2.(((\neg(p\ V0A)) \Rightarrow False) \Rightarrow (((p\ V0A) \Rightarrow False) \Rightarrow False))) \quad (62)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2.(\forall V1q \in 2.(\forall V2r \in 2.(((p\ V0p) \Leftrightarrow (\\ & (p\ V1q) \Leftrightarrow (p\ V2r))) \Leftrightarrow (((p\ V0p) \vee ((p\ V1q) \vee (p\ V2r))) \wedge (((p\ V0p) \vee ((\neg \\ & p\ V2r)) \vee (\neg(p\ V1q)))) \wedge (((p\ V1q) \vee ((\neg(p\ V2r)) \vee (\neg(p\ V0p)))) \wedge ((p\ V2r) \vee \\ & ((\neg(p\ V1q)) \vee (\neg(p\ V0p)))))))))) \end{aligned} \quad (63)$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p \vee 0p) \Leftrightarrow (\\
& (p \vee 1q) \vee (p \vee 2r))) \Leftrightarrow (((p \vee 0p) \vee \neg(p \vee 1q)) \wedge ((p \vee 0p) \vee \neg(p \vee 2r))) \wedge \\
& ((p \vee 1q) \vee ((p \vee 2r) \vee \neg(p \vee 0p))))))))))
\end{aligned} \tag{64}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p \vee 0p) \Leftrightarrow (\\
& (p \vee 1q) \Rightarrow (p \vee 2r))) \Leftrightarrow (((p \vee 0p) \vee (p \vee 1q)) \wedge ((p \vee 0p) \vee \neg(p \vee 2r))) \wedge ((\\
& \neg(p \vee 1q) \vee ((p \vee 2r) \vee \neg(p \vee 0p))))))))))
\end{aligned} \tag{65}$$

Assume the following.

$$\begin{aligned}
& (\forall V0p \in 2. (\forall V1q \in 2. (((p \vee 0p) \Leftrightarrow \neg(p \vee 1q))) \Leftrightarrow (((p \vee 0p) \vee \\
& (p \vee 1q)) \wedge (\neg(p \vee 1q) \vee \neg(p \vee 0p))))))
\end{aligned} \tag{66}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p \vee 0p) \Rightarrow (p \vee 1q))) \Rightarrow (p \vee 0p))) \tag{67}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p \vee 0p) \Rightarrow (p \vee 1q))) \Rightarrow \neg(p \vee 1q))) \tag{68}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p \vee 0p) \vee (p \vee 1q))) \Rightarrow \neg(p \vee 0p))) \tag{69}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p \vee 0p) \vee (p \vee 1q))) \Rightarrow \neg(p \vee 1q))) \tag{70}$$

Assume the following.

$$(\forall V0p \in 2. (\neg(\neg(p \vee 0p))) \Rightarrow (p \vee 0p)) \tag{71}$$

Theorem 1

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow \forall A_{.27c}. \\
& nonempty\ A_{.27c} \Rightarrow (\forall V0p \in (ty_2Epair_2Eprod\ (2^{A_{.27a}})\ (ty_2Epair_2Eprod \\
& \quad (2^{(2^{A_{.27a}})})\ (ty_2Erealax_2Ereal^{(2^{A_{.27a}})}))) . (\forall V1X \in \\
& (A_{.27b}^{A_{.27a}}) . (\forall V2Y \in (A_{.27c}^{A_{.27a}}) . (\forall V3f \in (ty_2Erealax_2Ereal^{A_{.27b}}) . \\
& \quad (((p\ (ap\ (c_2Eprobability_2Eprob_space\ A_{.27a})\ V0p)) \wedge ((p\ (ap \\
& \quad (c_2Epred_set_2EFINITE\ A_{.27a})\ (ap\ (c_2Eprobability_2Ep_space \\
& \quad A_{.27a})\ V0p)))) \wedge ((ap\ (c_2Eprobability_2Eevents\ A_{.27a})\ V0p) = (ap \\
& \quad (c_2Epred_set_2EPOW\ A_{.27a})\ (ap\ (c_2Eprobability_2Ep_space \\
& \quad A_{.27a})\ V0p)))))) \Rightarrow ((ap\ (ap\ (c_2Ereal_sigma_2EREAL_SUM_IMAGE \\
& \quad (ty_2Epair_2Eprod\ A_{.27b}\ A_{.27c}))\ (ap\ (c_2Epair_2EUNCURRY\ A_{.27b} \\
& \quad A_{.27c}\ ty_2Erealax_2Ereal)\ (\lambda V4x \in A_{.27b} . (\lambda V5y \in A_{.27c} . (\\
& \quad ap\ (ap\ c_2Erealax_2Ereal_mul\ (ap\ (ap\ (ap\ (ap\ (c_2Eprobability_2Ejoint_distribution \\
& \quad A_{.27b}\ A_{.27c}\ A_{.27a})\ V0p)\ V1X)\ V2Y)\ (ap\ (ap\ (c_2Epred_set_2EINSERT \\
& \quad (ty_2Epair_2Eprod\ A_{.27b}\ A_{.27c}))\ (ap\ (ap\ (c_2Epair_2E_2C\ A_{.27b} \\
& \quad A_{.27c})\ V4x)\ V5y))\ (c_2Epred_set_2EEMPTY\ (ty_2Epair_2Eprod\ A_{.27b} \\
& \quad A_{.27c}))))))\ (ap\ V3f\ V4x))))))\ (ap\ (ap\ (c_2Epred_set_2ECROSS\ A_{.27b} \\
& \quad A_{.27c})\ (ap\ (ap\ (c_2Epred_set_2EIMAGE\ A_{.27a}\ A_{.27b})\ V1X)\ (ap\ (c_2Eprobability_2Ep_space \\
& \quad A_{.27a})\ V0p)))\ (ap\ (ap\ (c_2Epred_set_2EIMAGE\ A_{.27a}\ A_{.27c})\ V2Y) \\
& \quad (ap\ (c_2Eprobability_2Ep_space\ A_{.27a})\ V0p)))))) = (ap\ (ap\ (c_2Ereal_sigma_2EREAL_SUM_IMAGE \\
& \quad A_{.27b})\ (\lambda V6x \in A_{.27b} . (ap\ (ap\ c_2Erealax_2Ereal_mul\ (ap\ (ap \\
& \quad (ap\ (c_2Eprobability_2Edistribution\ A_{.27b}\ A_{.27a})\ V0p)\ V1X)\ (ap \\
& \quad (ap\ (c_2Epred_set_2EINSERT\ A_{.27b})\ V6x)\ (c_2Epred_set_2EEMPTY \\
& \quad A_{.27b}))))\ (ap\ V3f\ V6x))))\ (ap\ (ap\ (c_2Epred_set_2EIMAGE\ A_{.27a} \\
& \quad A_{.27b})\ V1X)\ (ap\ (c_2Eprobability_2Ep_space\ A_{.27a})\ V0p)))))))))
\end{aligned}$$