

thm_2EquantHeuristics_2ESIMPLE_GUESS_FORALL_IMP_1 (TMarLetoEnW7zknPjgk1rqX9jsSHtvEfaaX)

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Definition 1 We define `c_2Emin_2E_3D` to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define `c_2Ebool_2ET` to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define `c_2Ebool_2E_21` to be $\lambda A.27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c_2Emin_2E_3D (2^{A-27a}))$

Definition 4 We define `c_2Ebool_2EF` to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define `c_2Ebool_2E_2F_5C` to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t))$

Definition 7 We define `c_2EquantHeuristics_2ESIMPLE_GUESS_EXISTS` to be $\lambda A.27a : \iota.\lambda V0v \in A.27a.\lambda V1i \in A.27a.\lambda V2P \in 2.(ap (ap (c_2Emin_2E_3D_3D_3E V2P) (ap (ap (c_2Emin_2E_3D_3D_3E$

Definition 8 We define `c_2Ebool_2E_7E` to be $(\lambda V0t \in 2.(ap (ap (c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2EF$

Definition 9 We define `c_2EquantHeuristics_2ESIMPLE_GUESS_FORALL` to be $\lambda A.27a : \iota.\lambda V0v \in A.27a.\lambda V1i \in A.27a.\lambda V2P \in 2.(ap (ap (c_2Emin_2E_3D_3D_3E (ap (c_2Ebool_2E_7E V2P)$

Assume the following.

$$True \tag{1}$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A.27a.(p V0t)) \Leftrightarrow (p V0t))) \tag{2}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow \\ & True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge ((\\ & (p V0t) \Rightarrow False) \Leftrightarrow (\neg (p V0t)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (4)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (5)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg(p\ V0t)))))) \quad (6)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (\neg((p\ V0A) \Rightarrow (p\ V1B))) \Leftrightarrow ((p\ V0A) \wedge \neg(p\ V1B)))) \quad (7)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \quad (8)$$

Assume the following.

$$(\forall V0x \in 2. (\forall V1x_27 \in 2. (\forall V2y \in 2. (\forall V3y_27 \in 2. (((p\ V0x) \Leftrightarrow (p\ V1x_27)) \wedge ((p\ V1x_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y_27)))) \Rightarrow (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x_27) \Rightarrow (p\ V3y_27)))))) \quad (9)$$

Theorem 1

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0v \in A_27a. (\forall V1i \in A_27a. (\forall V2P1 \in 2. (\forall V3P2 \in 2. ((p\ (ap\ (ap\ (c_2EquantHeuristics_2ESIMPLE_GUESS_EXISTS\ A_27a)\ V0v)\ V1i)\ V2P1)) \Rightarrow (p\ (ap\ (ap\ (c_2EquantHeuristics_2ESIMPLE_GUESS_FORALL\ A_27a)\ V0v)\ V1i)\ (ap\ (ap\ c_2Emin_2E_3D_3D_3E\ V2P1)\ V3P2))))))$$