

thm_2Equotient_2ERIGHT_RES_FORALL_REGULAR (TMRSYGfZvC8d23jd5wGC6RVdHVwNyGQ73GH)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$
of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E_3D (2^{A_27a}))$

Definition 4 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$
of type ι .

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2EF$

Definition 7 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t))$

Definition 8 We define c_2Ebool_2EIN to be $\lambda A_27a : \iota.(\lambda V0x \in A_27a.(\lambda V1f \in (2^{A_27a}).(ap V1f V0x)))$

Definition 9 We define $c_2Ebool_2ERES_FORALL$ to be $\lambda A_27a : \iota.(\lambda V0p \in (2^{A_27a}).(\lambda V1m \in (2^{A_27a}).(ap$

Assume the following.

$$True \tag{1}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \tag{2}$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow \neg(p V0t)) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow \neg(p V0t)))))) \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}). (\forall V1x \in \\ & A_27a. ((p (ap (ap (c_2Ebool_2EIN\ A_27a)\ V1x)\ V0P)) \Leftrightarrow (p (ap\ V0P\ V1x)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}). (\forall V1f \in \\ & (2^{A_27a}). ((p (ap (ap (c_2Ebool_2ERES_FORALL\ A_27a)\ V0P)\ V1f)) \Leftrightarrow \\ & (\forall V2x \in A_27a. ((p (ap (ap (c_2Ebool_2EIN\ A_27a)\ V2x)\ V0P)) \Rightarrow \\ & (p (ap\ V1f\ V2x))))))) \end{aligned} \quad (5)$$

Theorem 1

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}). (\forall V1R \in \\ & (2^{A_27a}). (\forall V2Q \in (2^{A_27a}). ((\forall V3x \in A_27a. ((p (\\ & ap\ V1R\ V3x)) \Rightarrow ((p (ap\ V0P\ V3x)) \Rightarrow (p (ap\ V2Q\ V3x)))))) \Rightarrow ((p (ap (c_2Ebool_2E_21 \\ & A_27a)\ V0P)) \Rightarrow (p (ap (ap (c_2Ebool_2ERES_FORALL\ A_27a)\ V1R)\ V2Q))))))) \end{aligned}$$