

thm\_2Equotient\_list\_2ELENGTH\_RSP  
(TMW5RTL $\text{YiYk6zFkn}p3ckXNzEqXZ1T4UmGdT$ )

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**Definition 1** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A. \lambda x \in A. \lambda y \in A. inj\_o (x = y)$  of type  $\iota \rightarrow \iota$ .

**Definition 2** We define  $c_2Emin_2E_3D_3D_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p\ P \Rightarrow p\ Q)$  of type  $\iota$ .

**Definition 3** We define  $c\_Ebool\_2ET$  to be  $(ap \ (ap \ (c\_Emin\_2E\_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x))$

**Definition 4** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.27a : \iota.( \lambda V0P \in (2^A\_{27a}).(ap\ ap\ (c\_2Emin\_2E\_3D\ (2^A\_{27a}\_21\ V) P) ) )$

**Definition 5** We define  $c_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap(c_2Ebool\_2E_21 2))(\lambda V2t \in 2.$

**Definition 6** We define  $c\_2Equotient\_2EQUOTIENT$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0R \in ((2^{A\_27a})^{A\_27a}).\lambda V$

**Definition 7** We define  $c\_2Ebool\_2EE$  to be  $(ap\ (c\_2Ebool\_2E\ 21\ 2)\ (\lambda V0t\in 2.V0t))$ .

**Definition 8** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2.(ap\ (ap\ c\_2Emin\_2E\_3D\_3D\_3D\ 7E\ t)\ 0))$

Let  $c\_2Enum\_2EZERO\_REP : \iota$  be given. Assume the following.

*c\_2Enum\_2EZERO REP*  $\in \omega$

$m : t$  be given. Assume the following

*nonempty*:  $\exists E \mathsf{enum} . \exists E \mathsf{enum}$

must be given. Assume the following

$$2E_{\text{kin}} - 2E_{\text{ABC}} \leq \varepsilon \left( t_0 + 2E_{\text{kin}} - 2E_{\text{ABC}} \right) \eta mea$$

$$2|W_1| \cdot 1/6 = 2\Gamma_1 = 2\Gamma_2 + 1/6 = 2\Gamma_3 = 2\Gamma_4 \text{ D.G.} = 2\Gamma_5$$

Let  $t = 2E_1 + 2E_2$ , and we have  $\Delta_t = t$  with the following:

For example, if  $\sigma$  is a standard deviation, then  $\sigma/\sqrt{n}$  is the standard error of the mean.

Let  $c\_2Elist\_2ELENGTH : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a. nonempty\ A\_27a \Rightarrow c\_2Elist\_2ELENGTH\ A\_27a \in (ty\_2Enum\_2Enum^{(ty\_2Elist\_2Elist\ A\_27a)}) \quad (5)$$

Let  $c\_2Elist\_2ECONS : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a. nonempty\ A\_27a \Rightarrow c\_2Elist\_2ECONS\ A\_27a \in (((ty\_2Elist\_2Elist\ A\_27a)^{(ty\_2Elist\_2Elist\ A\_27a)})^{A\_27a}) \quad (6)$$

Let  $c\_2Elist\_2ENIL : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a. nonempty\ A\_27a \Rightarrow c\_2Elist\_2ENIL\ A\_27a \in (ty\_2Elist\_2Elist\ A\_27a) \quad (7)$$

Let  $c\_2Elist\_2ELIST\_REL : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a. nonempty\ A\_27a \Rightarrow \forall A\_27b. nonempty\ A\_27b \Rightarrow c\_2Elist\_2ELIST\_REL\ A\_27a\ A\_27b \in (((2^{(ty\_2Elist\_2Elist\ A\_27b)})^{(ty\_2Elist\_2Elist\ A\_27a)})^{((2^{A\_27b})^{A\_27a})}) \quad (8)$$

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \quad (9)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega}) \quad (10)$$

**Definition 10** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum. (ap\ c\_2Enum\_2EABS\_num$

Assume the following.

$$True \quad (11)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow False) \Leftrightarrow (\neg(p\ V0t))))))) \quad (12)$$

Assume the following.

$$\forall A\_27a. nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (13)$$

Assume the following.

$$\begin{aligned} \forall A\_27a. nonempty\ A\_27a \Rightarrow & (((ap\ (c\_2Elist\_2ELENGTH\ A\_27a) \\ & (c\_2Elist\_2ENIL\ A\_27a)) = c\_2Enum\_2E0) \wedge (\forall V0h \in A\_27a. ( \\ & \forall V1t \in (ty\_2Elist\_2Elist\ A\_27a). ((ap\ (c\_2Elist\_2ELENGTH\ A\_27a) \\ & (ap\ (ap\ (c\_2Elist\_2ECONS\ A\_27a)\ V0h)\ V1t)) = (ap\ c\_2Enum\_2ESUC \\ & (ap\ (c\_2Elist\_2ELENGTH\ A\_27a)\ V1t))))))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned}
 & \forall A_{27a}.nonempty A_{27a} \Rightarrow (\forall V0P \in (2^{(ty\_2Elist\_2Elist A_{27a})}). \\
 & (((p (ap V0P (c_2Elist_2ENIL A_{27a}))) \wedge (\forall V1t \in (ty\_2Elist\_2Elist \\
 & A_{27a}).((p (ap V0P V1t)) \Rightarrow (\forall V2h \in A_{27a}.(p (ap V0P (ap (ap \\
 & c\_2Elist\_2ECONS A_{27a}) V2h) V1t)))))) \Rightarrow (\forall V3l \in (ty\_2Elist\_2Elist \\
 & A_{27a}).(p (ap V0P V3l)))))) \\
 & (15)
 \end{aligned}$$

Assume the following.

$$\begin{aligned}
 & \forall A_{27a}.nonempty A_{27a} \Rightarrow \forall A_{27b}.nonempty A_{27b} \Rightarrow ( \\
 & \forall V0R \in ((2^{A_{27b}})^{A_{27a}}).(\forall V1a \in A_{27a}.(\forall V2as \in \\
 & (ty\_2Elist\_2Elist A_{27a}).(\forall V3b \in A_{27b}.(\forall V4bs \in \\
 & (ty\_2Elist\_2Elist A_{27b}).(((p (ap (ap (c_2Elist\_2ELIST\_REL \\
 & A_{27a} A_{27b}) V0R) (c_2Elist\_2ENIL A_{27a})) (c_2Elist\_2ENIL A_{27b}))) \Leftrightarrow \\
 & True) \wedge (((p (ap (ap (c_2Elist\_2ELIST\_REL A_{27a} A_{27b}) V0R) \\
 & (ap (ap (c_2Elist\_2ECONS A_{27a}) V1a) V2as)) (c_2Elist\_2ENIL A_{27b}))) \Leftrightarrow \\
 & False) \wedge (((p (ap (ap (c_2Elist\_2ELIST\_REL A_{27a} A_{27b}) V0R) \\
 & (c_2Elist\_2ENIL A_{27a})) (ap (ap (c_2Elist\_2ECONS A_{27b}) V3b) V4bs)) \Leftrightarrow \\
 & False) \wedge ((p (ap (ap (c_2Elist\_2ELIST\_REL A_{27a} A_{27b}) V0R) \\
 & (ap (ap (c_2Elist\_2ECONS A_{27a}) V1a) V2as)) (ap (ap (c_2Elist\_2ECONS \\
 & A_{27b}) V3b) V4bs)) \Leftrightarrow ((p (ap (ap V0R V1a) V3b)) \wedge (p (ap (ap (c_2Elist\_2ELIST\_REL \\
 & A_{27a} A_{27b}) V0R) V2as) V4bs)))))))))) \\
 & (16)
 \end{aligned}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0m \in ty\_2Enum\_2Enum.(\forall V1n \in ty\_2Enum\_2Enum. \\
 & ((ap c_2Enum\_2ESUC V0m) = (ap c_2Enum\_2ESUC V1n)) \Leftrightarrow (V0m = V1n))) \\
 & (17)
 \end{aligned}$$

### Theorem 1

$$\begin{aligned}
 & \forall A_{27a}.nonempty A_{27a} \Rightarrow \forall A_{27b}.nonempty A_{27b} \Rightarrow ( \\
 & \forall V0R \in ((2^{A_{27a}})^{A_{27a}}).(\forall V1abs \in (A_{27b})^{A_{27a}}). \\
 & (\forall V2rep \in (A_{27a})^{A_{27b}}).((p (ap (ap (ap (c_2Equotient\_2EQUOTIENT \\
 & A_{27a} A_{27b}) V0R) V1abs) V2rep)) \Rightarrow (\forall V3l1 \in (ty\_2Elist\_2Elist \\
 & A_{27a}).(\forall V4l2 \in (ty\_2Elist\_2Elist A_{27a}).((p (ap (ap (ap \\
 & (c_2Elist\_2ELIST\_REL A_{27a} A_{27b}) V0R) V3l1) V4l2)) \Rightarrow ((ap (c_2Elist\_2ELENGTH \\
 & A_{27a}) V3l1) = (ap (c_2Elist\_2ELENGTH A_{27a}) V4l2))))))) \\
 &
 \end{aligned}$$