

Let $c_2Epair_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2ESND \\ A_27a\ A_27b \in (A_27b^{(ty_2Epair_2Eprod\ A_27a\ A_27b)}) \end{aligned} \quad (3)$$

Let $c_2Epair_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Epair_2EFST \\ A_27a\ A_27b \in (A_27a^{(ty_2Epair_2Eprod\ A_27a\ A_27b)}) \end{aligned} \quad (4)$$

Definition 10 We define $c_2Epair_2EUNCURRY$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in ((A_27c^{A_27a})$

Definition 11 We define $c_2Equotient_pair_2E_23_23_23$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda A_27d : \iota.$

Assume the following.

$$True \quad (5)$$

Assume the following.

$$\begin{aligned} (\forall V0t \in 2.(((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (7)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ \forall V0x \in (ty_2Epair_2Eprod\ A_27a\ A_27b).(\exists V1q \in A_27a. \\ (\exists V2r \in A_27b.(V0x = (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b) \\ V1q)\ V2r)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow \forall A_27c. \\ nonempty\ A_27c \Rightarrow \forall A_27d.nonempty\ A_27d \Rightarrow (\forall V0R1 \in (\\ (2^{A_27c})^{A_27a}).(\forall V1R2 \in ((2^{A_27d})^{A_27b}).(\forall V2a \in \\ A_27a.(\forall V3b \in A_27b.(\forall V4c \in A_27c.(\forall V5d \in A_27d. \\ ((p\ (ap\ (ap\ (ap\ (ap\ (c_2Equotient_pair_2E_23_23_23\ A_27a\ A_27b \\ A_27c\ A_27d)\ V0R1)\ V1R2)\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V2a) \\ V3b))\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27c\ A_27d)\ V4c)\ V5d)))) \Leftrightarrow ((p\ (ap\ (\\ ap\ V0R1\ V2a)\ V4c)) \wedge (p\ (ap\ (ap\ V1R2\ V3b)\ V5d)))))))))) \end{aligned} \quad (9)$$

Theorem 1

$$\begin{aligned} & \forall A_{27a}.nonempty\ A_{27a} \Rightarrow \forall A_{27b}.nonempty\ A_{27b} \Rightarrow (\\ & \quad \forall V0R1 \in ((2^{A_{27a}})^{A_{27a}}).(\forall V1R2 \in ((2^{A_{27b}})^{A_{27b}}). \\ & \quad ((\forall V2x \in A_{27a}.(\forall V3y \in A_{27a}.((p\ (ap\ (ap\ V0R1\ V2x) \\ & \quad V3y)) \Leftrightarrow ((ap\ V0R1\ V2x) = (ap\ V0R1\ V3y)))))) \wedge (\forall V4x \in A_{27b}.(\forall V5y \in \\ & \quad A_{27b}.((p\ (ap\ (ap\ V1R2\ V4x)\ V5y)) \Leftrightarrow ((ap\ V1R2\ V4x) = (ap\ V1R2\ V5y)))))) \Rightarrow \\ & \quad (\forall V6x \in (ty_2Epair_2Eprod\ A_{27a}\ A_{27b}).(p\ (ap\ (ap\ (ap\ (ap \\ & \quad (c_2Equotient_pair_2E_23_23_23\ A_{27a}\ A_{27b}\ A_{27a}\ A_{27b})\ V0R1) \\ & \quad V1R2)\ V6x)\ V6x)))))) \end{aligned}$$