

thm_2Erat_2ERAT_EQ_SUB0 (TM-
MYunCPK2SvF8QyDyweGU7Vu4P3KvrN1CC)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p \Rightarrow Q)$ of type ι .

Definition 3 We define $c_2Ebool_2E_2T$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 4 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E_3D (2^{A_27a}))$

Definition 5 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t)))$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty_2Epair_2Eprod A0 A1) \tag{1}$$

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2EABS_prod A_27a A_27b \in ((ty_2Epair_2Eprod A_27a A_27b)^{(2^{A_27b})^{A_27a}}) \tag{2}$$

Definition 6 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in A_27a.\lambda V1y \in A_27b.(ap (c_2Epair_2EABS_prod$

Let $ty_2Efrac_2Efrac : \iota$ be given. Assume the following.

$$nonempty ty_2Efrac_2Efrac \tag{3}$$

Let $ty_2Einteger_2Eint : \iota$ be given. Assume the following.

$$nonempty ty_2Einteger_2Eint \tag{4}$$

Let $c_2Efrac_2Eabs_frac : \iota$ be given. Assume the following.

$$c_2Efrac_2Eabs_frac \in (ty_2Efrac_2Efrac^{(ty_2Epair_2Eprod ty_2Einteger_2Eint ty_2Einteger_2Eint)}) \tag{5}$$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \tag{6}$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{7}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \tag{8}$$

Definition 7 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 8 We define $c_2Earithmic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Einteger_2Eint_REP_CLASS : \iota$ be given. Assume the following.

$$c_2Einteger_2Eint_REP_CLASS \in ((2^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)})^{ty_2Einteger_2Eint}) \tag{9}$$

Definition 9 We define c_2Emin_2E40 to be $\lambda A.\lambda P \in 2^A$. **if** $(\exists x \in A.p\ (ap\ P\ x))$ **then** $(the\ (\lambda x.x \in A \wedge p\ of\ type\ \iota \Rightarrow \iota))$

Definition 10 We define $c_2Einteger_2Eint_REP$ to be $\lambda V0a \in ty_2Einteger_2Eint.(ap\ (c_2Emin_2E40\ (t$

Let $c_2Einteger_2Etint_neg : \iota$ be given. Assume the following.

$$c_2Einteger_2Etint_neg \in ((ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)}) \tag{10}$$

Let $c_2Einteger_2Etint_eq : \iota$ be given. Assume the following.

$$c_2Einteger_2Etint_eq \in ((2^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)})^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)}) \tag{11}$$

Let $c_2Einteger_2Eint_ABS_CLASS : \iota$ be given. Assume the following.

$$c_2Einteger_2Eint_ABS_CLASS \in (ty_2Einteger_2Eint)^{(2^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)})} \tag{12}$$

Definition 11 We define $c_2Einteger_2Eint_ABS$ to be $\lambda V0r \in (ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)$

Definition 12 We define $c_2Einteger_2Eint_neg$ to be $\lambda V0T1 \in ty_2Einteger_2Eint.(ap\ c_2Einteger_2Eint$

Let $c_2Einteger_2Etint_add : \iota$ be given. Assume the following.

$$c_2Einteger_2Etint_add \in (((ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)})^{(ty_2Epair_2Eprod\ ty_2Enum_2Enum\ ty_2Enum_2Enum)}) \tag{13}$$

Definition 13 We define $c_2Einteger_2Eint_add$ to be $\lambda V0T1 \in ty_2Einteger_2Eint.\lambda V1T2 \in ty_2Einteger$

Definition 14 We define $c_Einteger_Eint_sub$ to be $\lambda V0x \in ty_Einteger_Eint.\lambda V1y \in ty_Einteger_Eint$.

Definition 15 We define c_Ebool_EF to be $(ap (c_Ebool_E21) 2) (\lambda V0t \in 2.V0t)$.

Definition 16 We define c_Ebool_E7E to be $(\lambda V0t \in 2.(ap (ap c_Emin_E3D_3D_3E V0t) c_Ebool_E21))$.

Let $c_EEnum_EREP_num : \iota$ be given. Assume the following.

$$c_EEnum_EREP_num \in (\omega^{ty_EEnum_EEnum}) \quad (14)$$

Let $c_EEnum_ESUC_REP : \iota$ be given. Assume the following.

$$c_EEnum_ESUC_REP \in (\omega^{\omega}) \quad (15)$$

Definition 17 We define c_EEnum_ESUC to be $\lambda V0m \in ty_EEnum_EEnum.(ap c_EEnum_EABS_num)$.

Definition 18 We define c_Ebool_E3F to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap V0P (ap (c_Emin_E2E_40$

Definition 19 We define $c_Eprim_rec_E3C$ to be $\lambda V0m \in ty_EEnum_EEnum.\lambda V1n \in ty_EEnum_EEnum$.

Let $c_Earithmic_E2B : \iota$ be given. Assume the following.

$$c_Earithmic_E2B \in ((ty_EEnum_EEnum)^{ty_EEnum_EEnum})^{ty_EEnum_EEnum} \quad (16)$$

Definition 20 We define $c_Earithmic_EBIT2$ to be $\lambda V0n \in ty_EEnum_EEnum.(ap (ap c_Earithmic_E2B$

Definition 21 We define $c_Earithmic_EBIT1$ to be $\lambda V0n \in ty_EEnum_EEnum.(ap (ap c_Earithmic_E2B$

Definition 22 We define $c_Earithmic_ENUMERAL$ to be $\lambda V0x \in ty_EEnum_EEnum.V0x$.

Let $c_Einteger_Eint_of_num : \iota$ be given. Assume the following.

$$c_Einteger_Eint_of_num \in (ty_Einteger_Eint)^{ty_EEnum_EEnum} \quad (17)$$

Let $c_Einteger_Eint_lt : \iota$ be given. Assume the following.

$$c_Einteger_Eint_lt \in ((2^{(ty_Epair_Eprod ty_EEnum_EEnum ty_EEnum_EEnum)})^{(ty_Epair_Eprod ty_EEnum_EEnum)}) \quad (18)$$

Definition 23 We define $c_Einteger_Eint_lt$ to be $\lambda V0T1 \in ty_Einteger_Eint.\lambda V1T2 \in ty_Einteger_Eint$.

Let $c_Efrac_Erep_frac : \iota$ be given. Assume the following.

$$c_Efrac_Erep_frac \in ((ty_Epair_Eprod ty_Einteger_Eint ty_Einteger_Eint)^{ty_Efrac_Efrac}) \quad (19)$$

Let $c_Epair_ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_Epair_ESND A_27a A_27b \in (A_27b)^{(ty_Epair_Eprod A_27a A_27b)} \quad (20)$$

Definition 24 We define $c_2Efrac_2Efrac_dnm$ to be $\lambda V0f \in ty_2Efrac_2Efrac.(ap (c_2Epair_2ESND t$
Let $c_2Epair_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A.27a.nonempty A.27a \Rightarrow \forall A.27b.nonempty A.27b \Rightarrow c_2Epair_2EFST \\ A.27a A.27b \in (A.27a^{(ty_2Epair_2Eprod A.27a A.27b)}) \end{aligned} \quad (21)$$

Definition 25 We define $c_2Efrac_2Efrac_nmr$ to be $\lambda V0f \in ty_2Efrac_2Efrac.(ap (c_2Epair_2EFST ty$
Let $c_2Einteger_2Etint_mul : \iota$ be given. Assume the following.

$$c_2Einteger_2Etint_mul \in (((ty_2Epair_2Eprod ty_2Enum_2Enum ty_2Enum_2Enum)_{(ty_2Epair_2Eprod ty_2Enum_2Enum ty_2Enum_2Enum)})_{(ty_2Epair_2Eprod ty_2Enum_2Enum ty_2Enum_2Enum)}) \quad (22)$$

Definition 26 We define $c_2Einteger_2Eint_mul$ to be $\lambda V0T1 \in ty_2Einteger_2Eint.\lambda V1T2 \in ty_2Einteger$

Definition 27 We define $c_2Efrac_2Efrac_0$ to be $(ap c_2Efrac_2Eabs_frac (ap (ap (c_2Epair_2E_2C ty_2$

Definition 28 We define $c_2Efrac_2Efrac_1$ to be $(ap c_2Efrac_2Eabs_frac (ap (ap (c_2Epair_2E_2C ty_2$

Definition 29 We define $c_2Erat_2Erat_equiv$ to be $\lambda V0f1 \in ty_2Efrac_2Efrac.\lambda V1f2 \in ty_2Efrac_2Efrac$

Let $ty_2Erat_2Erat : \iota$ be given. Assume the following.

$$nonempty ty_2Erat_2Erat \quad (23)$$

Let $c_2Erat_2Eabs_rat_CLASS : \iota$ be given. Assume the following.

$$c_2Erat_2Eabs_rat_CLASS \in (ty_2Erat_2Erat^{(2^{ty_2Efrac_2Efrac})}) \quad (24)$$

Definition 30 We define $c_2Erat_2Eabs_rat$ to be $\lambda V0r \in ty_2Efrac_2Efrac.(ap c_2Erat_2Eabs_rat_CLASS$

Definition 31 We define $c_2Erat_2Erat_1$ to be $(ap c_2Erat_2Eabs_rat c_2Efrac_2Efrac_1)$.

Let $c_2Erat_2Erep_rat_CLASS : \iota$ be given. Assume the following.

$$c_2Erat_2Erep_rat_CLASS \in ((2^{ty_2Efrac_2Efrac})^{ty_2Erat_2Erat}) \quad (25)$$

Definition 32 We define $c_2Erat_2Erep_rat$ to be $\lambda V0a \in ty_2Erat_2Erat.(ap (c_2Emin_2E_40 ty_2Efrac$

Definition 33 We define $c_2Efrac_2Efrac_add$ to be $\lambda V0f1 \in ty_2Efrac_2Efrac.\lambda V1f2 \in ty_2Efrac_2Efrac$

Definition 34 We define $c_2Erat_2Erat_add$ to be $\lambda V0r1 \in ty_2Erat_2Erat.\lambda V1r2 \in ty_2Erat_2Erat.(ap$

Definition 35 We define $c_2Ecombin_2EK$ to be $\lambda A.27a : \iota.\lambda A.27b : \iota.(\lambda V0x \in A.27a.(\lambda V1y \in A.27b.V0x)$

Definition 36 We define $c_2Ecombin_2ES$ to be $\lambda A.27a : \iota.\lambda A.27b : \iota.\lambda A.27c : \iota.(\lambda V0f \in ((A.27c^{A.27b})^{A.27$

Definition 37 We define $c_2Ecombin_2EI$ to be $\lambda A.27a : \iota.(ap (ap (c_2Ecombin_2ES A.27a (A.27a^{A.27a}) A$

Let $c_2Earithmetic_2Enum_CASE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Earithmetic_2Enum_CASE\ A_27a \in \left((A_27a^{(A_27a^{ty_2Enum_2Enum})})_{A_27a} \right)_{ty_2Enum_2Enum} \quad (26)$$

Definition 38 We define $c_2Erat_2Erat_0$ to be $(ap\ c_2Erat_2Eabs_rat\ c_2Efrac_2Efrac_0)$.

Definition 39 We define $c_2Erelation_2EWF$ to be $\lambda A_27a : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). (ap\ (c_2Ebool_2E_21$

Let $c_2Ebool_2EARB : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ebool_2EARB\ A_27a \in A_27a \quad (27)$$

Definition 40 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A_27a. (\lambda V2t2 \in A_27a. ($

Definition 41 We define $c_2Erelation_2ERESTRICT$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0f \in (A_27b^{A_27a}). \lambda V1f \in (A_27b^{A_27a}).$

Definition 42 We define $c_2Erelation_2ETC$ to be $\lambda A_27a : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1a \in A_27a. \lambda V2b \in A_27a.$

Definition 43 We define $c_2Erelation_2Eapprox$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M \in (A_27a^{A_27a}).$

Definition 44 We define $c_2Erelation_2Ethe_fun$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M \in (A_27a^{A_27a}).$

Definition 45 We define $c_2Erelation_2EWFREC$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0R \in ((2^{A_27a})^{A_27a}). \lambda V1M \in (A_27a^{A_27a}).$

Definition 46 We define $c_2Erat_2Erat_of_num$ to be $(ap\ (ap\ (c_2Erelation_2EWFREC\ ty_2Enum_2Enum\ ty_2Enum_2Enum)))$

Definition 47 We define $c_2Efrac_2Efrac_ainv$ to be $\lambda V0f1 \in ty_2Efrac_2Efrac. (ap\ c_2Efrac_2Eabs_frac\ (ap\ (c_2Efrac_2Efrac_ainv\ V0f1)))$

Definition 48 We define $c_2Efrac_2Efrac_sub$ to be $\lambda V0f1 \in ty_2Efrac_2Efrac. \lambda V1f2 \in ty_2Efrac_2Efrac. (ap\ (c_2Efrac_2Efrac_sub\ V0f1\ V1f2))$

Definition 49 We define $c_2Erat_2Erat_sub$ to be $\lambda V0r1 \in ty_2Erat_2Erat. \lambda V1r2 \in ty_2Erat_2Erat. (ap\ (c_2Erat_2Erat_sub\ V0r1\ V1r2))$

Assume the following.

$$True \quad (28)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (29)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (30)$$

Assume the following.

$$\begin{aligned} & (\forall V0f \in ty_2Efrac_2Efrac. ((ap\ c_2Efrac_2Eabs_frac\ (ap \\ & (ap\ (c_2Epair_2E_2C\ ty_2Einteger_2Eint\ ty_2Einteger_2Eint) \\ & (ap\ c_2Efrac_2Efrac_nmr\ V0f))\ (ap\ c_2Efrac_2Efrac_dnm\ V0f))) = \\ & V0f)) \end{aligned} \quad (31)$$

Assume the following.

$$\begin{aligned}
& (\forall V0f \in ty_2Efrac_2Efrac.(p (ap (ap c_2Einteger_2Eint_lt \\
& (ap c_2Einteger_2Eint_of_num c_2Enum_2E0)) (ap c_2Efrac_2Efrac_dnm \\
& V0f))))
\end{aligned} \tag{32}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in ty_2Einteger_2Eint.(\forall V1b \in ty_2Einteger_2Eint. \\
& ((p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) V1b)) \Rightarrow ((ap c_2Efrac_2Efrac_nmr (ap c_2Efrac_2Eabs_frac \\
& (ap (ap (c_2Epair_2E_2C ty_2Einteger_2Eint ty_2Einteger_2Eint) \\
& V0a) V1b))) = V0a))))
\end{aligned} \tag{33}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in ty_2Einteger_2Eint.(\forall V1b \in ty_2Einteger_2Eint. \\
& ((p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) V1b)) \Rightarrow ((ap c_2Efrac_2Efrac_dnm (ap c_2Efrac_2Eabs_frac \\
& (ap (ap (c_2Epair_2E_2C ty_2Einteger_2Eint ty_2Einteger_2Eint) \\
& V0a) V1b))) = V1b))))
\end{aligned} \tag{34}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a1 \in ty_2Einteger_2Eint.(\forall V1b1 \in ty_2Einteger_2Eint. \\
& (\forall V2a2 \in ty_2Einteger_2Eint.(\forall V3b2 \in ty_2Einteger_2Eint. \\
& ((p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) V1b1)) \Rightarrow ((p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) V3b2)) \Rightarrow ((ap (ap c_2Efrac_2Efrac_sub (ap c_2Efrac_2Eabs_frac \\
& (ap (ap (c_2Epair_2E_2C ty_2Einteger_2Eint ty_2Einteger_2Eint) \\
& V0a1) V1b1))) (ap c_2Efrac_2Eabs_frac (ap (ap (c_2Epair_2E_2C \\
& ty_2Einteger_2Eint ty_2Einteger_2Eint) V2a2) V3b2))) = (ap c_2Efrac_2Eabs_frac \\
& (ap (ap (c_2Epair_2E_2C ty_2Einteger_2Eint ty_2Einteger_2Eint) \\
& (ap (ap c_2Einteger_2Eint_sub (ap (ap c_2Einteger_2Eint_mul \\
& V0a1) V3b2)) (ap (ap c_2Einteger_2Eint_mul V2a2) V1b1))) (ap (\\
& ap c_2Einteger_2Eint_mul V1b1) V3b2))))))))))
\end{aligned} \tag{35}$$

Assume the following.

$$\begin{aligned}
& (\forall V0a \in ty_2Einteger_2Eint.(\forall V1b \in ty_2Einteger_2Eint. \\
& ((p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) V0a)) \Rightarrow ((p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) V1b)) \Rightarrow (p (ap (ap c_2Einteger_2Eint_lt (ap c_2Einteger_2Eint_of_num \\
& c_2Enum_2E0)) (ap (ap c_2Einteger_2Eint_mul V0a) V1b))))))
\end{aligned} \tag{36}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0x \in ty_2Einteger_2Eint. ((ap (ap c_2Einteger_2Eint_mul \\
 & V0x) (ap c_2Einteger_2Eint_of_num (ap c_2Earithmic_2ENUMERAL \\
 & (ap c_2Earithmic_2EBIT1 c_2Earithmic_2EZERO)))) = V0x))
 \end{aligned}
 \tag{37}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0x \in ty_2Einteger_2Eint. ((ap (ap c_2Einteger_2Eint_mul \\
 & (ap c_2Einteger_2Eint_of_num c_2Enum_2E0)) V0x) = (ap c_2Einteger_2Eint_of_num \\
 & c_2Enum_2E0)))
 \end{aligned}
 \tag{38}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0x \in ty_2Einteger_2Eint. (\forall V1y \in ty_2Einteger_2Eint. \\
 & (((ap (ap c_2Einteger_2Eint_sub V0x) V1y) = (ap c_2Einteger_2Eint_of_num \\
 & c_2Enum_2E0)) \Leftrightarrow (V0x = V1y))))
 \end{aligned}
 \tag{39}$$

Assume the following.

$$(\forall V0r \in ty_2Erat_2Erat. ((ap\ c_2Erat_2Eabs_rat (ap\ c_2Erat_2Erep_rat V0r)) = V0r)) \quad (42)$$

Assume the following.

$$(\forall V0f1 \in ty_2Efrac_2Efrac. (\forall V1f2 \in ty_2Efrac_2Efrac. ((ap\ c_2Erat_2Eabs_rat V0f1) = (ap\ c_2Erat_2Eabs_rat V1f2)) \Leftrightarrow (p (ap (ap\ c_2Erat_2Erat_equiv V0f1) V1f2)))))) \quad (43)$$

Assume the following.

$$(\forall V0f1 \in ty_2Efrac_2Efrac. (\forall V1f2 \in ty_2Efrac_2Efrac. ((ap (ap\ c_2Erat_2Erat_sub (ap\ c_2Erat_2Eabs_rat V0f1)) (ap\ c_2Erat_2Eabs_rat V1f2)) = (ap\ c_2Erat_2Eabs_rat (ap (ap\ c_2Efrac_2Efrac_sub V0f1) V1f2)))))) \quad (44)$$

Theorem 1

$$(\forall V0r1 \in ty_2Erat_2Erat. (\forall V1r2 \in ty_2Erat_2Erat. (((ap (ap\ c_2Erat_2Erat_sub V0r1) V1r2) = (ap\ c_2Erat_2Erat_of_num\ c_2Enum_2E0)) \Leftrightarrow (V0r1 = V1r2))))))$$