

thm_2Erelation_2EIN__RRANGE (TMbCuk4hDtfM46yqfXXvX9EqiPbtbfC7JZN)

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Definition 1 We define `c_2Emin_2E_3D` to be $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj_o } (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define `c_2Ebool_2EIN` to be $\lambda A. 27a : \iota. (\lambda V0x \in A. 27a. (\lambda V1f \in (2^{A-27a}). (\text{ap } V1f \ V0x)))$

Definition 3 We define `c_2Ebool_2EET` to be $(\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 4 We define `c_2Emin_2E_40` to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p (\text{ap } P \ x)) \text{ then } (\text{the } (\lambda x. x \in A \wedge p (\text{ap } P \ x)))$ of type $\iota \Rightarrow \iota$.

Definition 5 We define `c_2Ebool_2E_3F` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } V0P (\text{ap } (\text{c_2Emin_2E_40 } A \ V0P))))$

Definition 6 We define `c_2Ebool_2E_21` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^{A-27a}) \ V0P))))$

Definition 7 We define `c_2Erelation_2ERRANGE` to be $\lambda A. 27a : \iota. \lambda A. 27b : \iota. \lambda V0R \in ((2^{A-27b})^{A-27a}). \lambda V1y \in A. 27b. (\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^{A-27a}) \ V0R) \ V1y))$

Assume the following.

$$\text{True} \tag{1}$$

Assume the following.

$$\forall A. 27a. \text{nonempty } A. 27a \Rightarrow (\forall V0x \in A. 27a. ((V0x = V0x) \Leftrightarrow \text{True})) \tag{2}$$

Theorem 1

$$\forall A. 27a. \text{nonempty } A. 27a \Rightarrow \forall A. 27b. \text{nonempty } A. 27b \Rightarrow (\forall V0y \in A. 27a. (\forall V1R \in ((2^{A-27a})^{A-27b}). ((p (\text{ap } (\text{ap } (\text{c_2Ebool_2EIN } A. 27a) \ V0y) (\text{ap } (\text{c_2Erelation_2ERRANGE } A. 27b \ A. 27a) \ V1R))) \Leftrightarrow (\exists V2x \in A. 27b. (p (\text{ap } (\text{ap } V1R \ V2x) \ V0y)))))))$$