

thm_2Erelation_2ERTC__ALT__DEF
(TMWynHCrnjD9ZFzG2gCq24nMj2H6q8psjAT)

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Definition 1 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p\ P \Rightarrow p\ Q)$ of type ι .

Definition 2 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 4 We define $c \in \text{Ebool} \rightarrow \text{Emin} \rightarrow \text{E3D}$ to be $\lambda A. \text{Zeta} : \iota. (\lambda V0P \in (2^{A \rightarrow 27a}).(ap (ap (c \in \text{Emin} \rightarrow \text{E3D}) (2^{A \rightarrow 27a}) (V0P)))$

Definition 5 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in 2.\dots)))$

Definition 6 We define c_2Ebool_2EF to be $(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V0t \in 2.V0t))$.

Definition 7 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap(c_2Ebool_2E_21 2))(\lambda V2t \in 2.$

Definition 8 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A$.if $(\exists x \in A.p (ap P x))$ then $(the (\lambda x.x \in A \wedge p$ of type $\iota \rightarrow \iota$.

Definition 9 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A_27a. (\lambda V2t2 \in A_27a. (a$

Definition 10 We define c_2Eb00_2E7E to be $(\lambda V0t \in 2.(ap\ (ap\ c_2Emin_2E3D_3D_3E\ V0t)\ c_2Eb00_2E7E))$

Definition 11 We define a 2Erelation 2ERTC to be $\lambda A. \exists \vec{a} : \lambda V0R \in ((2^{A-27a})^A)^{A-27a}$, $\lambda V1a \in A \exists \vec{a}$, $\lambda V2$

Assume the following

$$True \quad (1)$$

Assume the following

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p\ V0t1) \Rightarrow (p\ V1t2)) \Rightarrow (((p\ V1t2) \Rightarrow (p\ V0t1)) \Rightarrow ((p\ V0t1) \Leftrightarrow (p\ V1t2)))))) \quad (2)$$

Assume the following

$$(\forall V \exists t \in 2^{\omega} \text{ } (False \Rrightarrow (p \vee V \otimes t))) \quad (3)$$

Assume the following.

$$(\forall V0t \in 2.((p V0t) \vee (\neg(p V0t)))) \quad (4)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty A_{27a} \Rightarrow & \forall A_{27b}.nonempty A_{27b} \Rightarrow \\ & \forall V0f \in (A_{27b}^{A_{27a}}).(\forall V1y \in A_{27a}.((ap (\lambda V2x \in \\ & A_{27a}.(ap V0f V2x)) V1y) = (ap V0f V1y))) \end{aligned} \quad (5)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge \\ ((\neg False) \Leftrightarrow True))) \quad (6)$$

Assume the following.

$$\forall A_{27a}.nonempty A_{27a} \Rightarrow (\forall V0x \in A_{27a}.((V0x = V0x) \Leftrightarrow \\ True)) \quad (7)$$

Assume the following.

$$\forall A_{27a}.nonempty A_{27a} \Rightarrow (\forall V0x \in A_{27a}.(\forall V1y \in \\ A_{27a}.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (8)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow \\ (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p \\ V0t))))))) \quad (9)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty A_{27a} \Rightarrow & (\forall V0t1 \in A_{27a}.(\forall V1t2 \in \\ A_{27a}.((ap (ap (ap (c_{2Ebool_2ECOND} A_{27a}) c_{2Ebool_2ET}) V0t1) \\ V1t2) = V0t1) \wedge ((ap (ap (ap (c_{2Ebool_2ECOND} A_{27a}) c_{2Ebool_2EF}) \\ V0t1) V1t2) = V1t2))) \end{aligned} \quad (10)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow \\ ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3))))) \quad (11)$$

Assume the following.

$$\begin{aligned} \forall A_{27a}.nonempty A_{27a} \Rightarrow & (\forall V0P \in 2.(\forall V1Q \in 2. \\ & (\forall V2x \in A_{27a}.(\forall V3x_{27} \in A_{27a}.(\forall V4y \in A_{27a}. \\ & (\forall V5y_{27} \in A_{27a}.(((p V0P) \Leftrightarrow (p V1Q)) \wedge (((p V1Q) \Rightarrow (V2x = V3x_{27})) \wedge \\ & ((\neg(p V1Q)) \Rightarrow (V4y = V5y_{27}))) \Rightarrow ((ap (ap (ap (c_{2Ebool_2ECOND} A_{27a}) \\ V0P) V2x) V4y) = (ap (ap (ap (c_{2Ebool_2ECOND} A_{27a}) V1Q) V3x_{27}) \\ & V5y_{27})))))))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). \\
& ((\forall V1x \in A_{27a}. (p (ap (ap (ap (c_2Erelation_2ERTC A_{27a}) \\
& V0R) V1x) V1x))) \wedge (\forall V2x \in A_{27a}. (\forall V3y \in A_{27a}. (\forall V4z \in \\
& A_{27a}. (((p (ap (ap V0R V2x) V3y)) \wedge (p (ap (ap (ap (c_2Erelation_2ERTC \\
& A_{27a}) V0R) V3y) V4z)))) \Rightarrow (p (ap (ap (ap (c_2Erelation_2ERTC A_{27a}) \\
& V0R) V2x) V4z))))))) \\
\end{aligned} \tag{13}$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). \\
& (\forall V1x \in A_{27a}. (p (ap (ap (ap (c_2Erelation_2ERTC A_{27a}) V0R) \\
& V1x) V1x)))) \\
\end{aligned} \tag{14}$$

Theorem 1

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). \\
& (\forall V1a \in A_{27a}. (\forall V2b \in A_{27a}. ((p (ap (ap (ap (c_2Erelation_2ERTC \\
& A_{27a}) V0R) V1a) V2b)) \Leftrightarrow (\forall V3Q \in (2^{A_{27a}}). (((p (ap V3Q V2b)) \wedge \\
& (\forall V4x \in A_{27a}. (\forall V5y \in A_{27a}. (((p (ap (ap V0R V4x) V5y)) \wedge \\
& (p (ap V3Q V5y)))) \Rightarrow (p (ap V3Q V4x))))))) \Rightarrow (p (ap V3Q V1a))))))) \\
\end{aligned}$$